

math

MAMMOTH

Grade 3-B Worktext South African Version

Place value with thousands

Geometry

Measuring

Division

Fractions



L
i
g
h
t
B
l
u
e
S
e
r
i
e
s

Contents

Foreword	5
Chapter 6: Place Value with Thousands	
Introduction	7
Thousands	9
Four-Digit Numbers and Place Value	13
Which Number Is Greater?	17
Mental Adding and Subtracting	19
Add 4-Digit Numbers with Regrouping	23
Subtract 4-Digit Numbers with Regrouping	25
Rounding to the Nearest Hundred	29
Estimating	32
Word Problems	35
Mixed Revision, Chapters 1 - 6	38
Revision, Chapter 6	40
Chapter 7: Geometry	
Introduction	42
Shapes	46
Some Special Quadrilaterals	50
Perimeter	53
Problems with Perimeter	56
Getting Started with Area	59
More about Area	61
Multiplying by Whole Tens	65
Area Units and Problems	69
Area and Perimeter Problems	72
More Area and Perimeter Problems	74
Solids	77
Mixed Revision, Chapters 1 - 7.....	79
Geometry Revision	81

Chapter 8: Measuring

Introduction	83
Centimetres and Millimetres	85
Line Plots and More Measuring	89
Metres and Kilometres	92
Grams and Kilograms.....	94
Millilitres and Litres	98
Mixed Revision, Chapters 1 - 8	100
Revision, Chapter 8	102

Chapter 9: Division

Introduction	104
Division as Making Groups	107
Division and Multiplication	111
Division and Multiplication Facts	115
Dividing Evenly into Groups	118
Division Word Problems	122
Zero in Division	125
When Division Is Not Exact	128
More Practice with the Remainder	131
Mixed Revision, Chapters 1 - 9	133
Revision, Chapter 9	135

Chapter 10: Fractions

Introduction	138
Understanding Fractions	142
Fractions on a Number Line	144
Mixed Numbers	148
Equivalent Fractions	152
Comparing Fractions 1	155
Comparing Fractions 2	158
Mixed Revision, Chapters 1 - 10	160
Fractions Revision	162

Foreword

Math Mammoth Grade 3-A and Grade 3-B worktexts comprise a complete maths curriculum for the third grade mathematics studies. This South African version has been **customized to South Africa** in the following manners:

- The names used are South African names (instead of Jack and Jill, there are Ansie and Mampho).
- The currency used in word problems is rand. The money chapter teaches both rand and cents.
- The material is “all metric.” In other words, the US customary measuring units are not used.
- Spelling is British English instead of American English.
- Paper size is A4.
- Geographic locations used emphasize South African locations (such as Pretoria, Johannesburg).

Please note that the curriculum is not following the South African official syllabus for 3rd grade maths. Instead, it simply is a copy of the US version of Math Mammoth Grade 3, aligned to the US Common Core Standards. This decision was made because of the great amount of work that would be involved in writing new lessons and reorganizing old ones to match all the standards in the South African syllabus. For the most part, Math Mammoth is exceeding South African standards. Some standards may not be covered.

Third grade is a time for learning and mastering two (mostly new) operations: multiplication and division within 100. The student also deepens his understanding of addition and subtraction, and uses those in many different contexts, such as with money, time, and geometry.

The main areas of study in Math Mammoth Grade 3 are:

1. Students develop an understanding of multiplication and division of whole numbers through problems involving equal-sized groups, arrays, and area models. They learn the relationship between multiplication and division, and solve many word problems involving multiplication and division (chapters 2, 3, and 9).
2. Students develop an understanding of fractions, beginning with unit fractions. They use visual fraction models and study fractions on a number line. Students also compare fractions by using visual fraction models and strategies based on noticing equal numerators or denominators (chapter 10).
3. Students learn the concepts of area and perimeter. They relate area to multiplication and to addition, recognize perimeter as a linear measure (in contrast with area), and solve problems involving area and perimeter (chapter 7).
4. Students fluently add and subtract within 1 000, both mentally and in columns (with regrouping). They learn to add and subtract 4-digit numbers, and use addition and subtraction in problem solving (chapters 1 and 6).

Additional topics we study are time (chapter 4), money (chapter 5), measuring (chapter 8), and bar graphs and picture graphs (in various chapters).

This book, 3-B, covers place value and 4-digit numbers (chapter 6), geometry (chapter 7), measuring (chapter 8), division (chapter 9), and fractions (chapter 10). The rest of the topics are covered in the 3-A student worktext.

When you use these two books as your only or main mathematics curriculum, they are like a “framework,” but you still have a lot of liberty in planning your child's studies. While multiplication and

division chapters are best studied in the order they are presented, feel free to go through the geometry, clock, measuring, and fraction sections in a different order. For the geometry chapter, the student should already know the multiplication tables. This might even be advisable if your child is “stuck” on some concept, or is getting bored. Sometimes the brain “mulls it over” in the background, and the concept the student was stuck on can become clear after a break.

Math Mammoth aims to concentrate on a few major topics at a time, and study them in depth. This is totally opposite to the continually spiralling step-by-step curricula, in which each lesson typically is about a different topic from the previous or next lesson, and includes a lot of revision problems from past topics.

This does not mean that your child would not need an occasional revision. However, when each major topic is presented in its own chapter, this gives you more freedom to plan the course of study *and* choose the revision times yourself. In fact, I totally encourage you to plan your mathematics school year as a set of certain topics, instead of a certain book or certain pages from a book.

For revision, the download version includes an html page called *Make_extra_worksheets_grade3.htm* that you can use to make additional worksheets for computation or for number charts. You can simply reprint some previously studied pages.

I wish you success in your maths teaching!

Maria Miller, the author

Chapter 6: Place Value with Thousands

Introduction

This chapter of *Math Mammoth Grade 3 South African Version* covers 4-digit numbers (numbers with thousands), and adding and subtracting them. We also study rounding and estimating, which are very important skills for everyday life.

First, children learn 4-digit numbers, place value—breaking numbers such as 3 498 into thousands, hundreds, tens, and ones—and comparing 4-digit numbers. Next, they practise some mental addition and subtraction with 4-digit numbers. The lesson stresses the similarities between adding and subtracting 4-digit numbers and adding and subtracting smaller numbers. Practising mental maths also helps to build number sense.

We also study regrouping in addition and subtraction, using 4-digit numbers. If you purchased the download version, you can make more worksheets for addition and subtraction using the accompanying worksheet maker.

The last major topics in this chapter are rounding numbers to the nearest hundred and estimating. Students also get to do some more word problems in one lesson.

The Lessons

	page	span
Thousands	9	4 pages
Four-Digit Numbers and Place Value	13	4 pages
Which Number is Greater?	17	2 pages
Mental Adding and Subtracting	19	4 pages
Add 4-Digit Numbers with Regrouping	23	2 pages
Subtract 4-Digit Numbers with Regrouping	25	4 pages
Rounding to the Nearest Hundred	29	3 pages
Estimating	32	3 pages
Word Problems	35	3 pages
Mixed Revision, Chapters 1 - 6	38	2 pages
Revision, Chapter 6	40	2 pages

Helpful Resources on the Internet

Use these free online resources to supplement the “bookwork” as you see fit.

Disclaimer: These links were valid at the time of the writing of this book, and to the best of our knowledge we believe these websites to have what is described. However, we cannot guarantee that the links have not changed. Parental supervision is recommended.

Base Blocks from National Library of Virtual Manipulatives

Place enough thousand cubes, hundred-flats, ten-sticks, and one-blocks in the work area to show the given numbers. Choose “Columns = 4” to restrict the program to four-digit numbers.

http://nlvm.usu.edu/en/nav/frames_asid_152_g_1_t_1.html?from=category_g_1_t_1.html

Maths Teacher's Toolkit

Use the place value calculator for this level to practise place value with 4-digit numbers. Some of the other tools are too easy for the focus of this chapter.

<http://www.crick.northants.sch.uk/Flash%20Studio/cfsmaths/Toolkit/Toolkit.htm>

Cookie Dough

Practise naming big numbers.

<http://www.funbrain.com/numwords/index.html>

Can you say really big numbers?

Enter a really big number, try to say it out loud, and see it written.

<http://www.mathcats.com/explore/reallybignumbers.html>

Line Dry Game

Fill in a missing number on the clothesline based on different skip-counting patterns.

<http://www.fuelthebrain.com/Game/play.php?ID=15>

Maximum Capacity

Drag as many gorillas as you can into the elevator without exceeding the weight capacity of the elevator. You will have to use your quick addition, estimation, and number sense skills.

<http://www.mrnussbaum.com/maximumcapacity.htm>

Place value puzzler

Place value or rounding game. Choose “easy” place value or “easy” rounding for this level. You will need to click on the required place value in a number, or type in the answer for rounding.

<http://www.funbrain.com/tens/index.html>

Rounding Sharks

You will be asked to round numbers in the thousands to the nearest hundred. Click on the shark that has the number rounded correctly.

<http://www.aaamath.com/B/est.htm>

This page left blank intentionally.

Four-Digit Numbers and Place Value

Here the numbers 2 467, 1 090, and 5 602 are written as a *sum* of their different place values.

It is like writing each part of the number out in full: the thousands, the hundreds, the tens, and the ones. **Notice the zeros!** When there are *no* hundreds, or tens, or ones, we write a zero.

thou- sands	hund- reds	tens	ones
2	4	6	7
2 000 + 400 + 60 + 7			

thou- sands	hund- reds	tens	ones
1	0	9	0
1 000 + 0 + 90 + 0			

thou- sands	hund- reds	tens	ones
5	6	0	2
5 000 + 600 + 0 + 2			

1. Fill in the blanks, and write the numbers as a sum of the different place values.

a. 1 034 = ___ thousand ___ hundreds ___ tens ___ ones
 = 1 000 + 0 + 30 + 4

b. 5 670 = ___ thousand ___ hundreds ___ tens ___ ones
 = 5 000 + _____ + _____ + _____

c. 3 508 = ___ thousand ___ hundreds ___ tens ___ ones
 = _____ + _____ + _____ + _____

d. 8 389 = ___ thousand ___ hundreds ___ tens ___ ones
 = _____ + _____ + _____ + _____

e. 9 007 = ___ thousand ___ hundreds ___ tens ___ ones
 = _____ + _____ + _____ + _____

f. 7 214 = ___ thousand ___ hundreds ___ tens ___ ones
 = _____ + _____ + _____ + _____

2. Fill in the table.

<p>a. Five thousand nine hundred and ninety</p> <p>T H T O</p> <table border="1" style="width: 100%; text-align: center;"> <tr> <td style="width: 25px; height: 25px;"></td> </tr> </table>					<p>b. Six thousand and sixteen</p> <p>T H T O</p> <table border="1" style="width: 100%; text-align: center;"> <tr> <td style="width: 25px; height: 25px;"></td> </tr> </table>					<p>c. Six thousand three hundred and three</p> <p>T H T O</p> <table border="1" style="width: 100%; text-align: center;"> <tr> <td style="width: 25px; height: 25px;"></td> </tr> </table>										
<p>d. Eight thousand seven hundred</p> <p>T H T O</p> <table border="1" style="width: 100%; text-align: center;"> <tr> <td style="width: 25px; height: 25px;"></td> </tr> </table>					<p>e. Nine thousand two hundred and forty-five</p> <p>T H T O</p> <table border="1" style="width: 100%; text-align: center;"> <tr> <td style="width: 25px; height: 25px;"></td> </tr> </table>					<p>f. Ten thousand</p> <p>ten thou- sands</p> <table border="1" style="width: 100%; text-align: center;"> <tr> <td style="width: 25px; height: 25px;"></td> </tr> <tr> <td>1</td> <td>0</td> <td>0</td> <td>0</td> <td>0</td> </tr> </table>						1	0	0	0	0
1	0	0	0	0																

3. These numbers are written as sums. Write them in the normal way.

<p>a. $2\,000 + 90 =$ _____</p> <p>$3\,000 + 200 =$ _____</p>	<p>b. $8\,000 + 5 =$ _____</p> <p>$1\,000 + 80 + 7 =$ _____</p>
<p>c. $8\,000 + 200 + 20 =$ _____</p> <p>$2\,000 + 500 + 90 + 8 =$ _____</p>	<p>d. $4\,000 + 50 =$ _____</p> <p>$2\,000 + 800 + 7 =$ _____</p>

4. What part of these numbers is missing?

<p>a. $5\,000 + 80 +$ _____ $= 5\,083$</p>	<p>b. $7\,000 +$ _____ $+ 5 = 7\,605$</p>
<p>c. _____ $+ 3\,000 = 3\,050$</p>	<p>d. _____ $+ 700 + 1 = 2\,701$</p>

5. Write the numbers immediately after and before the given number.

a. _____ , 6 049 , _____

b. _____ , 2 324 , _____

c. _____ , 1 800 , _____

d. _____ , 8 809 , _____

e. _____ , 7 385 , _____

f. _____ , 9 244 , _____

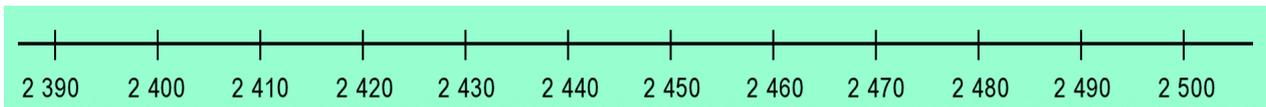
6. These numbers are written as sums, but in a scrambled order! Write them as normal numbers.

a. $4\,000 + 900 + 7 =$ _____	b. $80 + 500 + 8\,000 + 6 =$ _____
c. 2 thousand 7 ones 4 tens	d. 2 tens 6 hundred 4 thousand
e. 7 thousand 8 hundred 8 ones	f. 5 thousand 6 tens
g. 3 thousand 4 ones	h. 5 hundred 9 thousand

7. What part of these numbers is missing?

a. $900 + 2 +$ _____ $= 8\,902$	b. $5\,000 + 40 +$ _____ $= 5\,046$
c. _____ $+ 6\,000 + 40 = 6\,540$	d. _____ $+ 4\,000 + 300 = 4\,340$

8. Here is a number line from 2 390 to 2 500 with tick-marks for every 10.



Mark these numbers on the number line (approximately):

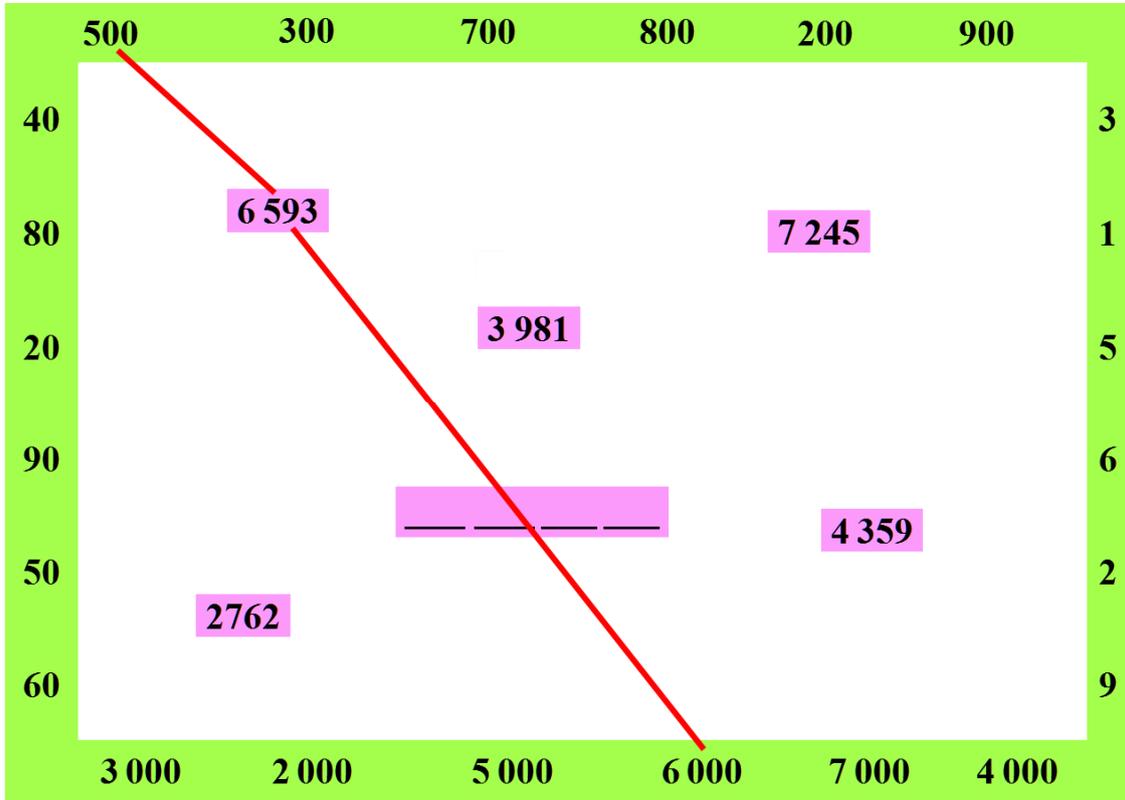
2 415 2 398 2 441 2 476 2 483 2 499.

9. Draw a number line from 7 650 to 7 800 with tick marks at every 10.

Mark these numbers on the number line (approximately):

7 659, 7 672, 7 745, 7 758, 7 777, 7 796

10. Connect each number inside the puzzle to its whole thousands, hundreds, tens, and ones that it contains. For example, 6 593 is connected to 6 000 and to 500 (for starters). Add the unused numbers from the border to form the missing number inside.



11. Solve the puzzle. Think of breaking the numbers into thousands, hundreds, tens, and ones.

	+		+		+		=	5 206
+		+		+		+		
	+		+		+		=	3 078
+		+		+		+		
	+		+		+		=	1 925
+		+		+		+		
	+		+		+		=	432
=		=		=		=		
5 022		3 235		1 408		976		

This page left blank intentionally.

Chapter 7: Geometry

Introduction

The seventh chapter of *Math Mammoth Grade 3 South African Version* deals with geometry. The emphasis is on two new concepts: area and perimeter.

First, we study and revise shapes in one lesson where the student divides shapes into new ones, and also encounters some tilings (also known as tessellations). Next, we study in more detail about some quadrilaterals, namely squares, rectangles, and rhombi (plural of rhombus).

Then comes the focus of this chapter: perimeter and area. Students find perimeters of polygons, including finding the perimeter when the side lengths are given, and finding an unknown side length when the perimeter is given.

They learn about area, and how to measure it in square centimetres, square metres, or in just square units if no unit of length is specified.

Students also relate area to the operations of multiplication and addition. They learn to find the area of a rectangle by multiplying the side lengths, and to find the area of rectilinear figures by dividing them into rectangles and adding the areas.

We also study the distributive property “in disguise.” This means using an area model to represent $a \times (b + c)$ as being equal to $a \times b$ plus $a \times c$. The expression $a \times (b + c)$ is the area of a rectangle with side lengths a and $(b + c)$, which is equal to the areas of two rectangles, one with sides a and b , and the other with sides a and c .

Multiplying by Whole Tens is a lesson about multiplication such as 3×40 or 90×7 . It is put here so that students can then use their multiplication skills to calculate areas of bigger rectangles.

Then we solve many area and perimeter problems. That is necessary so that students are able to distinguish between these two concepts. They also get to see rectangles with the same perimeter and different areas or with the same area and different perimeters.

Lastly, we touch on solids, such as cubes, rectangular prisms, pyramids, cones, and cylinders, and study their faces, edges, and vertices. You can make paper models for them from the printouts provided in the download version of the curriculum. Alternatively you can buy them, usually made in plastic. Search on the internet for “geometric solids.”

The Lessons

	page	span
Shapes	46	4 pages
Some Special Quadrilaterals	50	3 pages
Perimeter	53	3 pages
Problems with Perimeter	56	3 pages
Getting Started with Area	59	2 pages
More About Area	61	4 pages
Multiplying by Whole Tens	65	4 pages
Area Units and Problems	69	4 pages
Area and Perimeter Problems	72	2 pages
More Area and Perimeter Problems	74	3 pages
Solids	77	2 pages
Mixed Revision, Chapters 1 - 7	79	2 pages
Geometry Revision	81	2 pages

Helpful Resources on the Internet

Use these online resources as you see fit to supplement the main text.

Disclaimer: These links were valid at the time of the writing of this book, and to the best of our knowledge we believe these websites to have what is described. However, we cannot guarantee that the links have not changed. Parental supervision is recommended.

SHAPES

Shape Cutter

Draw any shape (polygon), cut it, and manipulate the cut pieces. You can have the computer mix them up, and then try to recreate the original shape.

<http://illuminations.nctm.org/ActivityDetail.aspx?ID=72>

Patch Tool

An online activity where the student designs a pattern using geometric shapes.

<http://illuminations.nctm.org/ActivityDetail.aspx?ID=27>

Polygon Playground

Drag various colourful polygons to the work area to make your own creations!

<http://www.mathcats.com/explore/polygons.html>

Interactive Quadrilaterals

Drag the corners to play with squares, rectangles, rhombi, and more.

<http://www.mathsisfun.com/geometry/quadrilaterals-interactive.html>

Shapes Identification Quiz from ThatQuiz.org

An online quiz in a multiple-choice format, asking to identify common two-dimensional shapes. You can modify the quiz parameters to your liking.

www.thatquiz.org/tq-f/math/shapes/

Sample worksheet from

www.mathmammoth.com

Tangram puzzles for kids

Use the seven pieces of the Tangram to form the given puzzle. Complete the puzzle by moving and rotating the seven shapes.

<http://www.abcya.com/tangrams.htm>

Interactive Tangram Puzzle

Place the tangram pieces so they form the given shape.

http://nlvm.usu.edu/en/nav/frames_asid_112_g_2_t_1.html

Tangram set

Cut out your Tangram set by folding paper.

<http://tangrams.ca/fold-set>

Interactivate! Tessellate

An online, interactive tool for creating your own tessellations. Choose a shape, then edit its corners or edges. The program automatically changes the shape so that it will tessellate (tile) the plane. Then push the tessellate button to see your creation!

<http://www.shodor.org/interactivate/activities/Tessellate>

Online Kaleidoscope

Create your own kaleidoscope creation with this interactive tool.

http://www.zefrank.com/dtoy_vs_byokal/

AREA AND PERIMETER

Everything you wanted to know about area and perimeter

Short explanations of how to find the perimeter of simple shapes and the area of rectangles, followed by quizzes on three levels. In perimeter, level two, some side lengths are not given. In level three, you calculate the perimeter of compound shapes. In area of rectangles, level 1 has just rectangles, and levels 2 and 3 have compound shapes made of rectangles.

www.bgfl.org/custom/resources_ftp/client_ftp/ks2/maths/perimeter_and_area/index.html

Shape Explorer

Find the perimeter and area of odd shapes on a rectangular grid.

<http://www.shodor.org/interactivate/activities/ShapeExplorer/>

Math Playground: Measuring the Area and Perimeter of Rectangles

Amy and her brother, Ben, explain how to find the area and perimeter of rectangles and show you how changing the perimeter of a rectangle affects its area. After the lesson, you will use an interactive ruler to measure the length and width of 10 rectangles, and to calculate the perimeter and area of each.

http://www.mathplayground.com/area_perimeter.html

Math Playground: Party Designer

You need to design areas for the party, such as a crafts table, food table, seesaw, and so on, so that they have the given perimeters and areas.

<http://www.mathplayground.com/PartyDesigner/PartyDesigner.html>

BBC Bitesize - Perimeter

A simple revision “bite” for perimeter that includes short explanations and a few quiz questions.

<http://www.bbc.co.uk/schools/ks3bitesize/maths/measures/perimeter/revise1.shtml>

Sample worksheet from

www.mathmammoth.com

BBC Bitesize - Area

Brief revision “bites”, including a few interactive questions, about area: counting squares, area of rectangles, area of triangles, parallelograms, and of compound shapes. Includes an activity and a test.
<http://www.bbc.co.uk/schools/ks3bitesize/maths/measures/area/revise1.shtml>

Geometry Area/Perimeter Quiz from ThatQuiz.org

An online quiz, asking either the area or perimeter of rectangles, triangles, and circles. You can modify the quiz parameters to your liking, for example to omit the circle, or instead of solving for area, you solve for an unknown side when the perimeter/area is given.
<http://www.thatquiz.org/tq-4/?-j201v-lc-m2kc0-na-p0>

Perimeter Game from Cyram.org

A simple online quiz for finding the perimeter of rectangles, triangles, or compound rectangles where not all side lengths are given.
<http://www.cyram.org/Projects/perimetergame/index.html>

FunBrain: Shape Surveyor Geometry Game

A simple and easy game that practises finding either the perimeter or area of rectangles.
<http://www.funbrain.com/poly/index.html>

Area of Rectangle

Drag the corners of the rectangle and see how the side lengths and areas change.
<http://illuminations.nctm.org/ActivityDetail.aspx?ID=46>

XP Math: Find Perimeters of Parallelograms

This online quiz shows you parallelograms and rectangles, and you need to calculate the perimeter, including typing in the right unit, and not using the altitude of the parallelogram.
<http://www.xpmath.com/forums/arcade.php?do=play&gameid=10>

SOLIDS

Identify Solids

Select the name and drop it on the correct solid.
<http://www.softschools.com/math/geometry/shapes/solids/games/>

Geometric Solids

Manipulate various geometric solids. Colour in the solid to investigate properties such as the number of faces, edges, and vertices.
<http://illuminations.nctm.org/ActivityDetail.aspx?ID=70>

2-D and 3-D Shapes

Learn about different solids and see them rotate.
http://www.bgfl.org/bgfl/custom/resources_ftp/client_ftp/ks2/maths/3d/index.htm

Identify solids

Click to identify the partially buried 3-dimensional shapes.
<http://www.primaryresources.co.uk/online/longshape3d.html>

Space Blocks

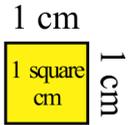
Build with blocks to illustrate three-dimensional shapes.
http://nlvm.usu.edu/en/nav/frames_asid_195_g_2_t_2.html

Sample worksheet from
www.mathmammoth.com

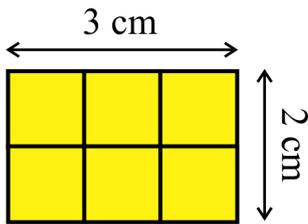
This page left blank intentionally.

Area Units and Problems

Area is always measured in squares of some size. To find the area of a shape, we check how many squares are needed to cover the shape.



Each side of this square measures 1 centimetre. It is a special square. It is called **a square centimetre**. We can use it to measure areas of other shapes.



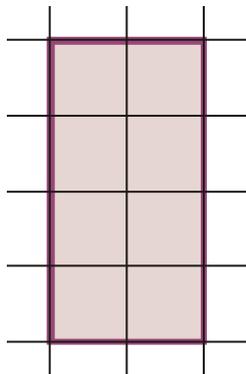
We need 6 square centimetres to cover this rectangle. So, its area is just that: 6 square centimetres. We abbreviate this as 6 cm^2 .

The elevated ² indicates the “squaring.”

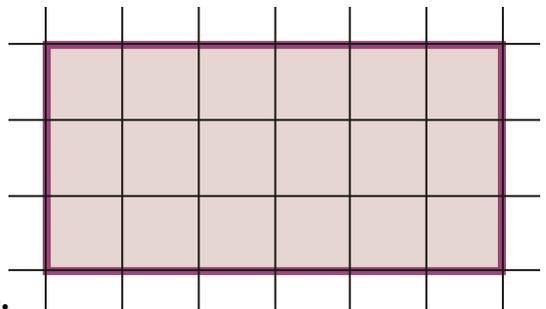
We can also use *multiplication* to find the area:

$$3 \text{ cm} \times 2 \text{ cm} = 6 \text{ cm}^2$$

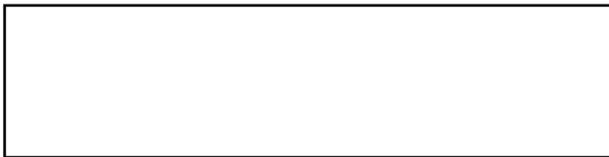
1. Write a multiplication for the area of each rectangle. Measure the sides of the rectangles in centimetres using a ruler. Do not forget the units (cm and cm^2)!



A = _____ cm \times _____ cm = _____ cm^2



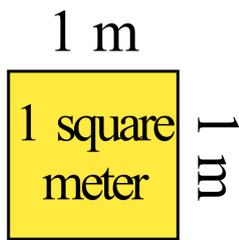
A = _____ cm \times _____ cm = _____ cm^2



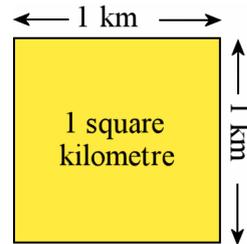
A = _____



A = _____



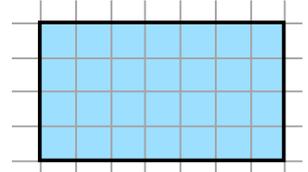
This is one square metre, or 1 m^2 .
(The picture is *not* to scale.)



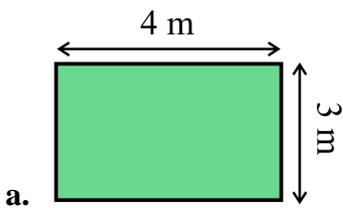
This is one square kilometre, or 1 km^2 .
(The picture is *not* to scale.)

If no particular unit of length is given for the sides of a rectangle, we just use the word “unit.”

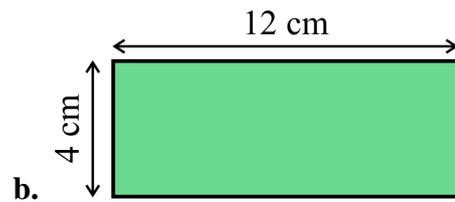
The sides are 7 and 4 units, and the area is 28 *square units*.



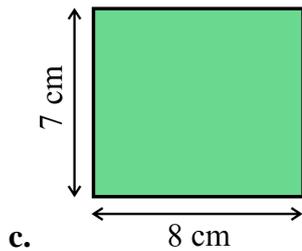
2. Find the areas of the rectangles. Be very careful about the unit you need to use, whether square centimetres (cm^2), square metres (m^2), or square units.



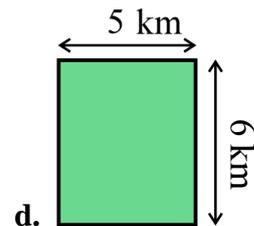
A = _____



A = _____

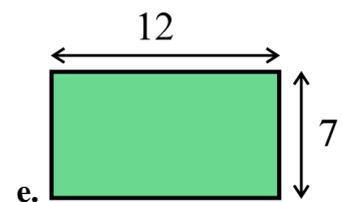


A = _____

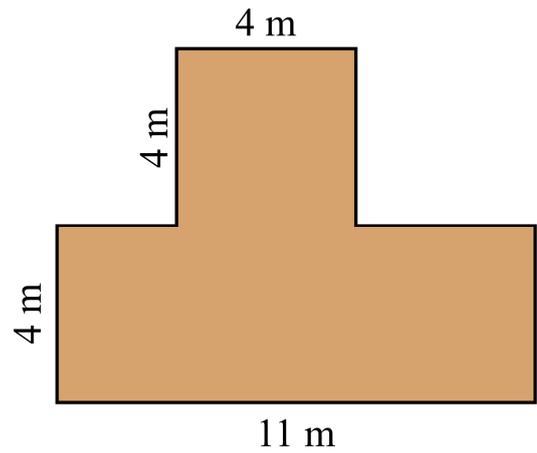


A = _____

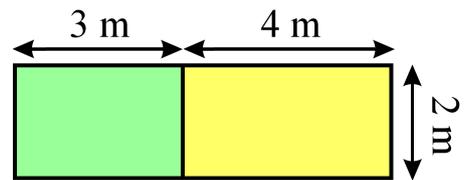
A = _____



3. Find the area of this children's playground.



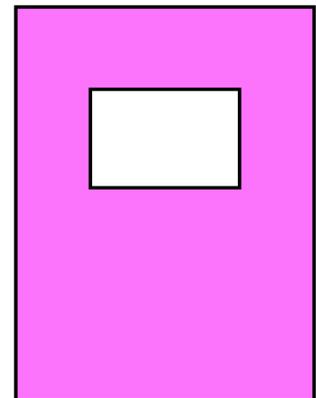
4. Find the area of Mary's garden.



5. Daniel's room measures 4 m by 4 m. His brother Jali's room is 5 m by 3 m. Whose room is bigger in area? How much bigger?

6. A notebook measures 15 cm by 20 cm. On its cover is a white square. The white square is 7 cm by 5 cm. How many square centimetres is the white square?

How many square centimetres is the shaded (pink) area?



This page left blank intentionally.

Chapter 8: Measuring

Introduction

The eighth chapter of *Math Mammoth Grade 3 South African Version* covers measuring-related topics.

If you have the downloadable version of this book (PDF file), you need to print this file as 100%, not “shrink to fit,” “print to fit,” or similar. If you print “shrink to fit,” some exercises about measuring in centimetres will not come out right, but will be “shrunk” compared to reality.

First, children learn about units of length in the metric system. Then, in the following lesson, they measure using centimetres and millimetres.

Later, students study line plots and get more practice measuring objects at home or in the classroom.

The next lesson helps students become familiar with metres and kilometres—the units for measuring medium and long distances.

Then it is time to measure weight. The lesson deals with grams and kilograms. It is very helpful if you can use a kitchen scale for this lesson, perhaps borrowing one if you do not own one.

Lastly, we study the metric units of liquid volume (litre and millilitre). The emphasis is on becoming familiar with measuring volume in millilitres.

Many of the lessons in this chapter also have an optional section about conversions between measuring units, such as changing three metres into centimetres. Converting between units is beyond the Common Core standards for third grade (it is actually included in the 4th and 5th grade standards), but I have included some easy conversion problems here because I feel many third graders are ready for them.

We all use various measuring units in our everyday lives, and using them is the key to remembering what they are, how big they are, and what the conversion factors are. The units your child is not using are likely to be forgotten easily. So encourage the student(s) to have free play time with measuring devices such as a scale, measuring cups, measuring tapes, and rulers.

The Lessons

	page	span
Centimetres and Millimetres	85	4 pages
Line Plots and More Measuring	89	3 pages
Metres and Kilometres	92	2 pages
Grams and Kilograms	94	4 pages
Millilitres and Litres	98	2 pages
Mixed Revision, Chapters 1 - 8	100	2 pages
Revision, Chapter 8	102	2 pages

Helpful Resources on the Internet

Use these online resources as you see fit to supplement the main text.

Disclaimer: These links were valid at the time of the writing of this book, and to the best of our knowledge we believe these websites to have what is described. However, we cannot guarantee that the links have not changed. Parental supervision is recommended.

Measure It!

Practise measuring lines with either centimetres or inches. Multiple choice questions.

<http://www.funbrain.com/measure>

Sal's Sub Shop

Customers order subs, and you need to cut them to the given measurements - sometimes in metric units, sometimes in inches.

<http://www.mrnussbaum.com/sal.htm>

Measurement Game for Kids

Measure the length and weight of various parcels using the interactive scale and ruler so you can give them a stamp with the correct postage rate. Uses grams and centimetres.

<http://www.kidsmathgamesonline.com/geometry/measurement.html>

Reading Scales

You can illustrate a variety of measuring devices, such as scales, measuring cup, thermometer, and speedometer, and how to read them. Generate examples using different scales on different devices at the press of a button.

<http://www.teacherled.com/2008/01/28/reading-scales>

Reading Scales

Weigh objects on this virtual balance scale, using weights of 10 g, 50 g, 250 g, and 500 g.

<http://www.teacherled.com/resources/oldscales/oldscalesload.html>

Measures

An online activity about metric measuring units and how to read scales, a measuring cup, and a ruler. Uses British spelling.

http://www.bgfl.org/bgfl/custom/resources_ftp/client_ftp/ks2/maths/measures

Chapter 8: Measuring

Introduction

The eighth chapter of *Math Mammoth Grade 3 South African Version* covers measuring-related topics.

If you have the downloadable version of this book (PDF file), you need to print this file as 100%, not “shrink to fit,” “print to fit,” or similar. If you print “shrink to fit,” some exercises about measuring in centimetres will not come out right, but will be “shrunk” compared to reality.

First, children learn about units of length in the metric system. Then, in the following lesson, they measure using centimetres and millimetres.

Later, students study line plots and get more practice measuring objects at home or in the classroom.

The next lesson helps students become familiar with metres and kilometres—the units for measuring medium and long distances.

Then it is time to measure weight. The lesson deals with grams and kilograms. It is very helpful if you can use a kitchen scale for this lesson, perhaps borrowing one if you do not own one.

Lastly, we study the metric units of liquid volume (litre and millilitre). The emphasis is on becoming familiar with measuring volume in millilitres.

Many of the lessons in this chapter also have an optional section about conversions between measuring units, such as changing three metres into centimetres. Converting between units is beyond the Common Core standards for third grade (it is actually included in the 4th and 5th grade standards), but I have included some easy conversion problems here because I feel many third graders are ready for them.

We all use various measuring units in our everyday lives, and using them is the key to remembering what they are, how big they are, and what the conversion factors are. The units your child is not using are likely to be forgotten easily. So encourage the student(s) to have free play time with measuring devices such as a scale, measuring cups, measuring tapes, and rulers.

The Lessons

	page	span
Centimetres and Millimetres	85	4 pages
Line Plots and More Measuring	89	3 pages
Metres and Kilometres	92	2 pages
Grams and Kilograms	94	4 pages
Millilitres and Litres	98	2 pages
Mixed Revision, Chapters 1 - 8	100	2 pages
Revision, Chapter 8	102	2 pages

Helpful Resources on the Internet

Use these online resources as you see fit to supplement the main text.

Disclaimer: These links were valid at the time of the writing of this book, and to the best of our knowledge we believe these websites to have what is described. However, we cannot guarantee that the links have not changed. Parental supervision is recommended.

Measure It!

Practise measuring lines with either centimetres or inches. Multiple choice questions.

<http://www.funbrain.com/measure>

Sal's Sub Shop

Customers order subs, and you need to cut them to the given measurements - sometimes in metric units, sometimes in inches.

<http://www.mrnussbaum.com/sal.htm>

Measurement Game for Kids

Measure the length and weight of various parcels using the interactive scale and ruler so you can give them a stamp with the correct postage rate. Uses grams and centimetres.

<http://www.kidsmathgamesonline.com/geometry/measurement.html>

Reading Scales

You can illustrate a variety of measuring devices, such as scales, measuring cup, thermometer, and speedometer, and how to read them. Generate examples using different scales on different devices at the press of a button.

<http://www.teacherled.com/2008/01/28/reading-scales>

Reading Scales

Weigh objects on this virtual balance scale, using weights of 10 g, 50 g, 250 g, and 500 g.

<http://www.teacherled.com/resources/oldscales/oldscalesload.html>

Measures

An online activity about metric measuring units and how to read scales, a measuring cup, and a ruler. Uses British spelling.

http://www.bgfl.org/bgfl/custom/resources_ftp/client_ftp/ks2/maths/measures

Chapter 8: Measuring

Introduction

The eighth chapter of *Math Mammoth Grade 3 South African Version* covers measuring-related topics.

If you have the downloadable version of this book (PDF file), you need to print this file as 100%, not “shrink to fit,” “print to fit,” or similar. If you print “shrink to fit,” some exercises about measuring in centimetres will not come out right, but will be “shrunk” compared to reality.

First, children learn about units of length in the metric system. Then, in the following lesson, they measure using centimetres and millimetres.

Later, students study line plots and get more practice measuring objects at home or in the classroom.

The next lesson helps students become familiar with metres and kilometres—the units for measuring medium and long distances.

Then it is time to measure weight. The lesson deals with grams and kilograms. It is very helpful if you can use a kitchen scale for this lesson, perhaps borrowing one if you do not own one.

Lastly, we study the metric units of liquid volume (litre and millilitre). The emphasis is on becoming familiar with measuring volume in millilitres.

Many of the lessons in this chapter also have an optional section about conversions between measuring units, such as changing three metres into centimetres. Converting between units is beyond the Common Core standards for third grade (it is actually included in the 4th and 5th grade standards), but I have included some easy conversion problems here because I feel many third graders are ready for them.

We all use various measuring units in our everyday lives, and using them is the key to remembering what they are, how big they are, and what the conversion factors are. The units your child is not using are likely to be forgotten easily. So encourage the student(s) to have free play time with measuring devices such as a scale, measuring cups, measuring tapes, and rulers.

The Lessons

	page	span
Centimetres and Millimetres	85	4 pages
Line Plots and More Measuring	89	3 pages
Metres and Kilometres	92	2 pages
Grams and Kilograms	94	4 pages
Millilitres and Litres	98	2 pages
Mixed Revision, Chapters 1 - 8	100	2 pages
Revision, Chapter 8	102	2 pages

Helpful Resources on the Internet

Use these online resources as you see fit to supplement the main text.

Disclaimer: These links were valid at the time of the writing of this book, and to the best of our knowledge we believe these websites to have what is described. However, we cannot guarantee that the links have not changed. Parental supervision is recommended.

Measure It!

Practise measuring lines with either centimetres or inches. Multiple choice questions.

<http://www.funbrain.com/measure>

Sal's Sub Shop

Customers order subs, and you need to cut them to the given measurements - sometimes in metric units, sometimes in inches.

<http://www.mrnussbaum.com/sal.htm>

Measurement Game for Kids

Measure the length and weight of various parcels using the interactive scale and ruler so you can give them a stamp with the correct postage rate. Uses grams and centimetres.

<http://www.kidsmathgamesonline.com/geometry/measurement.html>

Reading Scales

You can illustrate a variety of measuring devices, such as scales, measuring cup, thermometer, and speedometer, and how to read them. Generate examples using different scales on different devices at the press of a button.

<http://www.teacherled.com/2008/01/28/reading-scales>

Reading Scales

Weigh objects on this virtual balance scale, using weights of 10 g, 50 g, 250 g, and 500 g.

<http://www.teacherled.com/resources/oldscales/oldscalesload.html>

Measures

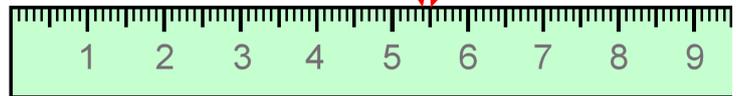
An online activity about metric measuring units and how to read scales, a measuring cup, and a ruler. Uses British spelling.

http://www.bgfl.org/bgfl/custom/resources_ftp/client_ftp/ks2/maths/measures

Centimetres and Millimetres

This ruler measures in centimetres.
The numbers signify whole centimetres.
All the shorter lines between those are for *millimetres*.

The distance from one short line to the next line is *1 millimetre*. We write 1 mm.
Millimetres are very tiny!



Look at the ruler: **there are 10 millimetres in each centimetre.**

Measuring lines: First see how many whole centimetres long the line is.
Then count how many little millimetre-lines beyond that it reaches.



This line is 2 cm 3 mm long. At the same time, it is 23 mm long. Why?

Each centimetre is 10 mm, so 2 cm is 20 mm. That means 2 cm 3 mm makes 23 mm in total.



This line is 4 cm 8 mm long. At the same time, it is 48 mm long.

1. Measure the lines using the ruler, first in whole centimetres and millimetres. Then write their lengths using millimetres only.

a. _____ cm _____ mm = _____ mm

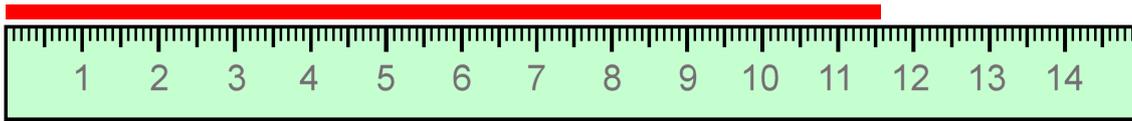


b. _____ cm _____ mm = _____ mm

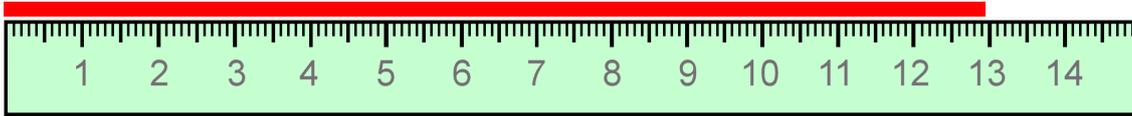


c. _____ cm _____ mm = _____ mm

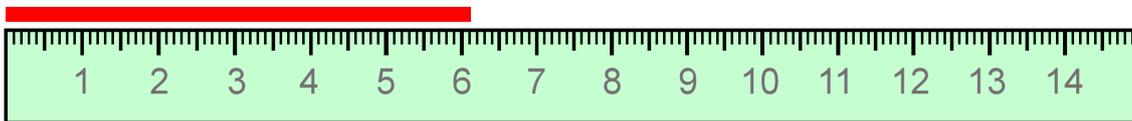




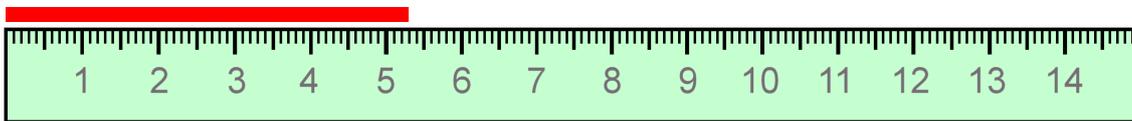
d. _____ cm _____ mm = _____ mm



e. _____ cm _____ mm = _____ mm



f. _____ cm _____ mm = _____ mm



g. _____ cm _____ mm = _____ mm

2. Draw lines using a ruler.

a. 7 cm 8 mm

b. 10 cm 5 mm

c. 14 mm

d. 55 mm

e. 126 mm

3. Measure items you can find at home, using a centimetre-millimetre ruler.
If the item is not exactly as long as the markers on the ruler, choose the nearest mark.

Item	Length

4. Change between centimetres and millimetres.

a.	b.	c.
1 cm = _____ mm	1 cm 1 mm = <u>11</u> mm	4 cm 5 mm = _____ mm
2 cm = _____ mm	1 cm 2 mm = _____ mm	2 cm 5 mm = _____ mm
5 cm = _____ mm	1 cm 8 mm = _____ mm	7 cm 8 mm = _____ mm
8 cm = _____ mm	2 cm 3 mm = _____ mm	10 cm 4 mm = _____ mm

5. Change between millimetres and centimetres.

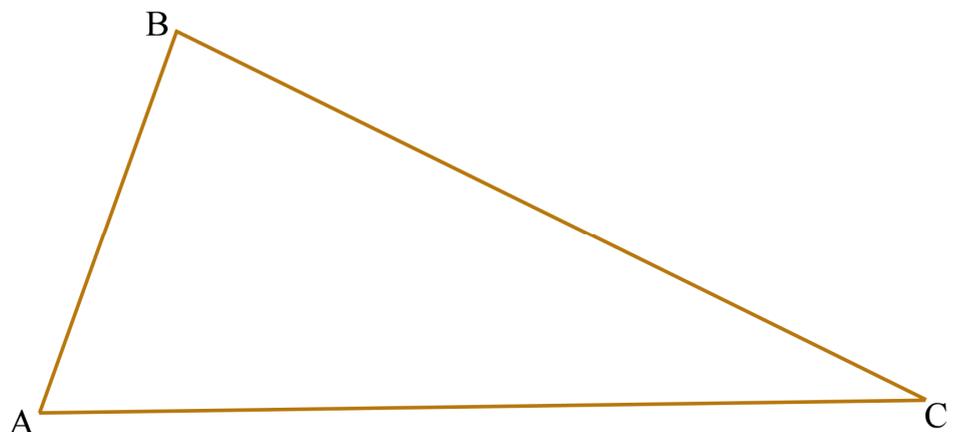
a.	b.	c.
70 mm = _____ cm	12 mm = ____ cm ____ mm	89 mm = ____ cm ____ mm
100 mm = _____ cm	45 mm = ____ cm ____ mm	102 mm = ____ cm ____ mm

6. Measure the sides of this triangle in millimetres.

Side AB _____ mm

Side BC _____ mm

Side CA _____ mm



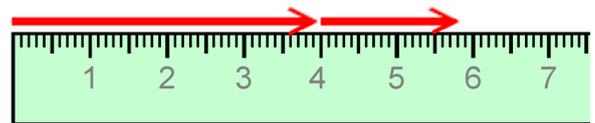
7. Find the perimeter of the triangle in the previous exercise.

8. Draw the third side of this triangle.
Then measure its sides.
Lastly, find its perimeter in millimetres.



The first arrow is 4 cm. The second arrow is 1 cm 8 mm. How long are they together?
Add, giving your answer in millimetres.

$$4 \text{ cm} + 1 \text{ cm } 8 \text{ mm} = 5 \text{ cm } 8 \text{ mm} = 58 \text{ mm}$$



Add centimetres with centimetres, and millimetres with millimetres.
Remember that 10 millimetres makes 1 centimetre.

$$9 \text{ mm} + 6 \text{ cm} + 2 \text{ mm} = 6 \text{ cm } 11 \text{ mm} = 7 \text{ cm } 1 \text{ mm} = 71 \text{ mm}$$

If you have both millimetres and centimetres, change the centimetres to millimetres first:

$$84 \text{ mm} + \underline{3 \text{ cm}} + 9 \text{ mm} = 84 \text{ mm} + \underline{30 \text{ mm}} + 9 \text{ mm} = 123 \text{ mm} \text{ (which is also } 12 \text{ cm } 3 \text{ mm)}$$

9. Work out these “line additions.” Give your answers in millimetres.

a. 1 cm 5 mm + 5 mm	b. 28 mm + 7 cm
c. 5 mm + 5 cm 8 mm	d. 2 cm 4 mm + 4 cm 5 mm
e. 52 mm + 2 cm 4 mm	f. 6 cm + 8 mm + 17 mm
g. 9 mm + 17 mm + 2 cm	h. 139 mm + 50 cm + 2 mm

This page left blank intentionally.

Chapter 9: Division

Introduction

The ninth chapter of *Math Mammoth Grade 3 South African Version* covers the concept of division, basic division facts that are based on the multiplication tables, and the concept of remainder. The aim is to lay a good foundation for the concept of division, cementing the link between multiplication and division.

The concept of division in itself is not difficult—after all, it is like backwards multiplication. The student needs to know the multiplication tables well as a prerequisite for this chapter. The student can start studying the lessons in this chapter even if he still needs some practice with the multiplication tables, but if he is a long way from mastering them, he should not study this chapter yet.

There are basically two ways to illustrate division with concrete objects. The first way is equal sharing: we divide or share items equally among people. For example, the problem $12 \div 3$ would mean, “If you share 12 bananas equally among 3 people, how many bananas does each one get?”

The second way has to do with grouping. The problem $12 \div 3$ would be, “If you have 12 items, how many groups of three items can you make?” These two interpretations of division are important to understand so that the student can solve real-life and mathematical problems involving division.

We also study division by zero. From studying that lesson, students should recognize that division by zero “does not work.” I realize that in higher forms of mathematics, division by zero may be defined (such as $1 \div 0 = \text{infinity}$). For now, this is the understanding that a third grader should get.

Lastly, students study the concept of remainder, or division that is not exact. We start by letting the students find the remainder using visual models (you could also use manipulatives). Then they learn how to find the remainder by calculating. This concept will be studied again in fourth grade.

The Lessons

	page	span
Division as Making Groups	107	4 pages
Division and Multiplication	111	4 pages
Division and Multiplication Facts	115	3 pages
Dividing Evenly into Groups	118	4 pages
Division Word Problems	122	3 pages
Zero in Division	125	3 pages
When Division Is Not Exact	128	3 pages
More Practice with the Remainder	131	2 pages
Mixed Revision, Chapters 1 - 9	133	2 pages
Revision, Chapter 9	135	2 pages

Helpful Resources on the Internet

Use these online resources as you see fit to supplement the main text.

Disclaimer: These links were valid at the time of the writing of this book, and to the best of our knowledge we believe these websites to have what is described. However, we cannot guarantee that the links have not changed. Parental supervision is recommended.

Rectangle Division

Practise division with remainders using a rectangle model.

http://nlvm.usu.edu/en/nav/frames_asid_193_g_2_t_1.html

Mr. Martini's Classroom: Multiplication and Division Inequalities

Compare expressions involving basic multiplication and division. The first number from the left (below the screen) lets you control the maximum number in the problems.

<http://www.thegreatmartinicompany.com/inequalities/multiplicationdivinequality.html>

Mystery Picture Game

Using division and addition.

<http://www.dositey.com/2008/math/m/mystery2AD.htm>

Fun 4 the Brain

Practise your basic facts with these simple games that appeal to students.

<http://www.fun4thebrain.com/division.html>

Math Magician Games

Flashcard problems in all four operations. Answer 20 questions in one minute.

<http://www.oswego.org/ocsd-web/games/Mathmagician/cathymath.html>

Cross the Swamp

Help Little Ron move from log to log across the swamp and practise multiplication/division or addition/subtraction.

<http://www.bbc.co.uk/schools/starship/maths/crosstheswamp.shtml>

Arithme-Tiles

Use the four operations and numbers on neighbouring tiles to make target numbers.

<http://www.primarygames.com/math/arithmetiles/index.htm>

Math Games at Sheppard Software

A bunch of different games to practise addition, subtraction, multiplication, and division facts: Fruit Shoot, Pop Up Math, Math MahJong, Matching games, Make 24, and many more. The site also has games for place value, coins, fractions, and other topics.

<http://www.sheppardsoftware.com/math.htm>

Arcademic Skill Builders

Website with fun, arcade-type games to practise the four basic operations. Both single- and multi-user games.

<http://www.arcademicskillbuilders.com>

MathCar Racing

Keep ahead of the computer car by thinking logically, and practise any of the four operations at the same time.

<http://www.funbrain.com/osa/index.html>

Sample worksheet from

www.mathmammoth.com

Tux Math

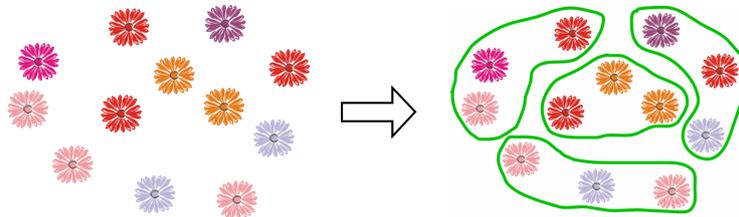
A free software. This is a versatile arcade game for maths facts with many options. Includes all operations. You need to shoot falling comets that can damage penguins' igloos.

<http://sourceforge.net/projects/tuxmath>

Read also my review at <http://homeschoolmath.blogspot.com/2011/05/tux-math.html>

Division as Making Groups

There are 12 daisies. Make groups of 3.



How many groups? Four groups.

How many 3's are there in 12? Four.

1. Divide into groups.

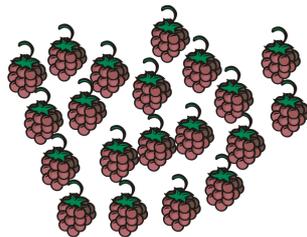
a. There are 15 carrots.
Make groups of 5.



How many groups? _____

How many 5's are there in 15? _____

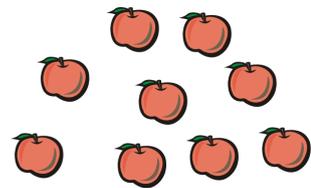
b. There are _____ berries.
Make groups of 4.



How many groups? _____

How many 4's are there in _____? _____

c. There are _____ apples.
Make groups of 3.



How many groups? _____

How many 3's are there in _____? _____

d. There are _____ fish.
Make groups of 2.



How many groups? _____

How many 2's are there in _____? _____

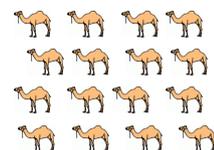
e. There are _____ daisies.
Make groups of 6.



How many groups? _____

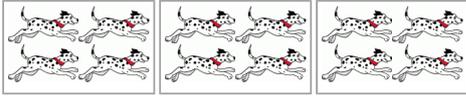
How many 6's are there in _____? _____

f. There are _____ camels.
Make groups of 4.



How many groups? _____

How many 4's are there in _____? _____



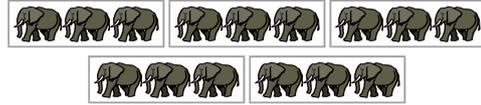
DIVIDE... 12 dogs into groups of four.

How many groups? Three

How many 4's in 12? _____

$$12 \div 4 = 3$$

“Twelve divided by four is three.”



DIVIDE... 15 elephants into groups of three.

How many groups? _____

How many 3's in 15? _____

$$15 \div 3 = 5$$

“Fifteen divided by three is five.”

18 ÷ 6 = ? *Think: If you DIVIDE 18 into groups of six, how many groups are there? How many groups of six are there in 18? How many sixes are there in 18?*

Since $6 + 6 + 6 = 18$, there are **THREE** sixes in 18. So, $18 \div 6 = 3$

2. Write a division sentence to fit the pictures in exercise 1.

a. _____ ÷ _____ = _____	b. _____ ÷ _____ = _____	c. _____ ÷ _____ = _____
d. _____ ÷ _____ = _____	e. _____ ÷ _____ = _____	f. _____ ÷ _____ = _____

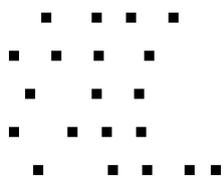
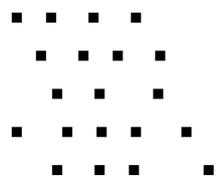
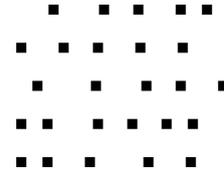
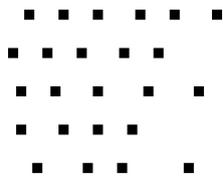
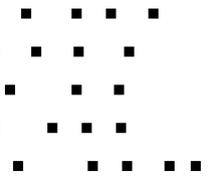
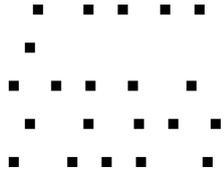
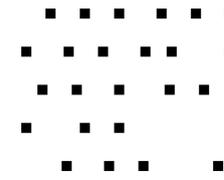
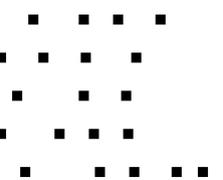
3. Make a division sentence.

<p>a. Divide 10 rams into groups of two. How many groups?</p> <p>_____ ÷ _____ = _____</p>	<p>b. Divide _____ camels into groups of four. How many groups?</p> <p>_____ ÷ _____ = _____</p>	<p>c. Divide _____ apples into groups of six. How many groups?</p> <p>_____ ÷ _____ = _____</p>
<p>d. Divide _____ books into groups of three. How many groups?</p> <p>_____ ÷ _____ = _____</p>	<p>e. Divide _____ pairs of scissors into groups of five. How many groups?</p> <p>_____ ÷ _____ = _____</p>	<p>f. Divide _____ crosses into groups of three. How many groups?</p> <p>_____ ÷ _____ = _____</p>

4. Draw sticks. Divide them into groups to fit the division sentence.

a. $18 \div 3 = \underline{\hspace{2cm}}$	b. $24 \div 2 = \underline{\hspace{2cm}}$
c. $21 \div 3 = \underline{\hspace{2cm}}$	d. $25 \div 5 = \underline{\hspace{2cm}}$
e. $15 \div 5 = \underline{\hspace{2cm}}$	f. $24 \div 8 = \underline{\hspace{2cm}}$

5. Make groups by circling dots and write a division sentence.

<p>a. Make groups of 4</p>  <p>$\underline{\hspace{2cm}} \div 4 = \underline{\hspace{2cm}}$</p>	<p>b. Make groups of 2</p>  <p>$\underline{\hspace{2cm}} \div 2 = \underline{\hspace{2cm}}$</p>	<p>c. Make groups of 6</p>  <p>$\underline{\hspace{2cm}} \div 6 = \underline{\hspace{2cm}}$</p>	<p>d. Make groups of 3</p>  <p>$\underline{\hspace{2cm}} \div 3 = \underline{\hspace{2cm}}$</p>
<p>e. Make groups of 5</p>  <p>$\underline{\hspace{2cm}} \div 5 = \underline{\hspace{2cm}}$</p>	<p>f. Make groups of 7</p>  <p>$\underline{\hspace{2cm}} \div 7 = \underline{\hspace{2cm}}$</p>	<p>g. Make groups of 6</p>  <p>$\underline{\hspace{2cm}} \div 6 = \underline{\hspace{2cm}}$</p>	<p>h. Make groups of 10</p>  <p>$\underline{\hspace{2cm}} \div 10 = \underline{\hspace{2cm}}$</p>

6. Solve the word problems. Write a division or a multiplication for each problem.

The box is for the \times or \div symbol.

<p>a. The class has 20 children. Each minibus will hold five children. How many minibuses are needed for the class?</p> <p>_____ <input type="checkbox"/> _____ = _____</p>	<p>b. Kgotso placed 30 marbles in rows of 5. How many rows did he get?</p> <p>_____ <input type="checkbox"/> _____ = _____</p>
<p>c. Erika packed hairpins in bags. She put 20 pins in each bag and filled four bags. How many pins were there?</p> <p>_____ <input type="checkbox"/> _____ = _____</p>	<p>d. Karen packed 28 T-shirts in bags. She put four shirts in each bag. How many bags did she use?</p> <p>_____ <input type="checkbox"/> _____ = _____</p>
<p>e. Bonga has 16 poster boards. He needs four of them to make a big poster. How many big ones can he make?</p> <p>_____ <input type="checkbox"/> _____ = _____</p>	<p>f. Moipone studied three hours each day for seven days. How many hours did she spend studying in total?</p> <p>_____ <input type="checkbox"/> _____ = _____</p>

7. Solve. You can draw to help. Can you find a pattern?

<p>a.</p> <p>4 \div 2 = _____</p> <p>6 \div 2 = _____</p> <p>8 \div 2 = _____</p> <p>10 \div 2 = _____</p> <p>12 \div 2 = _____</p> <p>14 \div 2 = _____</p> <p>16 \div 2 = _____</p> <p>_____ \div 2 = _____</p> <p>_____ \div 2 = _____</p>	<p>b.</p> <p>20 \div 10 = _____</p> <p>30 \div 10 = _____</p> <p>40 \div 10 = _____</p> <p>50 \div 10 = _____</p> <p>_____ \div 10 = _____</p>	<p>c.</p> <p>10 \div 5 = _____</p> <p>15 \div 5 = _____</p> <p>20 \div 5 = _____</p> <p>25 \div 5 = _____</p> <p>_____ \div 5 = _____</p>
---	--	---

This page left blank intentionally.

Chapter 10: Fractions

Introduction

The last chapter of *Math Mammoth Grade 3 South African Version* deals with a few elementary fraction concepts: the concepts of a fraction and of a mixed number, fractions on a number line, equivalent fractions, and comparing fractions.

First, the child learns to identify fractions in visual models, and to draw “pie models” for some common fractions. You can also use manipulatives or the fraction cut-outs provided. In the download version, they are found in their separate folder, and in the printed version, they are appended to the answer key.

Next, students represent fractions on a number-line diagram by partitioning the interval from 0 to 1 into equal parts. They also study fractions on number lines that go up to 3 and learn to write whole numbers as fractions.

The lesson about mixed numbers relies on visual models and number lines. I strongly feel that students first need to understand fraction operations and concepts with the help of visual models or manipulatives, and not introducing the various rules for calculations too soon. Students match fractions and mixed numbers, and even convert mixed numbers back into fractions using visual models. The actual rule for the conversion is not introduced on this level.

Next, we study equivalent fractions. Students recognise and generate simple equivalent fractions using visual models and number lines.

Lastly, students compare fractions in special cases, such as when they have the same numerator or the same denominator, or when the comparison can be made from visual models. They also learn that comparisons are valid only when the two fractions refer to the same whole.

The Lessons

	page	span
Understanding Fractions	142	4 pages
Fractions on a Number Line	144	4 pages
Mixed Numbers	148	4 pages
Equivalent Fractions	152	3 pages
Comparing Fractions 1	155	3 pages
Comparing Fractions 2	158	2 pages
Mixed Revision, Chapters 1 - 10	160	2 pages
Fractions Revision	162	3 pages

Helpful Resources on the Internet

Use these online resources as you see fit to supplement the main text.

Disclaimer: These links were valid at the time of the writing of this book, and to the best of our knowledge we believe these websites to have what is described. However, we cannot guarantee that the links have not changed. Parental supervision is needed.

Conceptua Fractions: Identify Fractions

A visual tool that shows fractions or mixed numbers using a pie, a bar, dots, and a number line.

<http://www.conceptuamath.com/fractions.html#IdentifyingFractions>

Visualizing Fractions

This tool shows you a fraction, and you divide the pie and colour the pieces.

http://nlvm.usu.edu/en/nav/frames_asid_103_g_2_t_1.html

Pattern Blocks - Parts as Wholes

Click on the “Activities” in the top menu, and click on arrows until you find the “Parts as Wholes” activity.

http://nlvm.usu.edu/en/nav/frames_asid_170_g_2_t_3.html

Fraction Model

Adjust the the numerator and the denominator, and the applet shows the fraction as a pie/rectangle/set model, as a decimal, and as a percent.

<http://illuminations.nctm.org/ActivityDetail.aspx?ID=44>

Clara Fraction's Ice Cream Shop

Convert improper fractions into mixed numbers and scoop the right amount of ice cream flavours onto the cone.

<http://www.mrnussbaum.com/icecream/index.html>

Equivalent Fractions from National Library of Virtual Manipulatives (NLVM)

See the equivalency of two fractions as the applet divides the whole into more pieces.

http://nlvm.usu.edu/en/nav/frames_asid_105_g_2_t_1.html

Equivalent Fractions

Construct two other, equivalent fractions to the given fraction using a circle or a square. Use the sliders to divide your shape into a certain amount of parts, then click on the parts to colour in some of them. Click the check mark to check if you got the equivalent fractions right. The fractions are also shown on the number line.

<http://illuminations.nctm.org/ActivityDetail.aspx?ID=80>

Conceptua Math: Equivalent Fractions

A visual tool to illustrate the equivalency of fractions. You can use pie, rectangular, or number line model. Divide each shape into parts using the sliders. Click on parts to colour in or remove the colour from them. Use two or three fractions. Free registration required.

<http://www.conceptuamath.com/fractions/equivalent-fractions.html>

Conceptua Math: Order Fractions on a Number Line

First create fractions using the button on the top right, then lock them. Use the “dot” button to see them placed on the number line. Then you can use the buttons on the left to see the fractions represented in different ways. Lastly, drag the fractions under the number line dots, and press the check mark.

<http://www.conceptuamath.com/fractions/ordering-fractions-number-line.html>

Sample worksheet from
www.mathmammoth.com

Fraction Games at Sheppard Software

Many games for fraction maths. For this level, use the first four games: simple fractions matching, mixed fractions matching, equivalent fractions matching, and comparing fractions balloon pop.

<http://www.sheppardsoftware.com/math.htm#fractions>

Visual Fractions

Great site for studying all aspects of fractions: identifying, renaming, comparing, addition, subtraction, multiplication, division. Each topic is illustrated by either a number line or a circle with a Java applet. Also a couple of games, for example: make cookies for Grampy.

<http://www.visualfractions.com/>

Who Wants pizza?

Explains the concept of a fraction, teaches addition and multiplication with a pizza example, then has some interactive exercises.

<http://math.rice.edu/~lanius/fractions/index.html>

Fractioncity

Make “fraction streets” and help students with comparing fractions, equivalent fractions, addition of fractions of like and unlike denominators while they drive toy cars on the streets. This is not an online activity but has instructions of how to do it at home or at school.

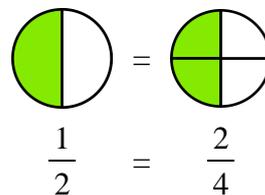
<http://www.teachnet.com/lesson/math/fractioncity.html>

This page left blank intentionally.

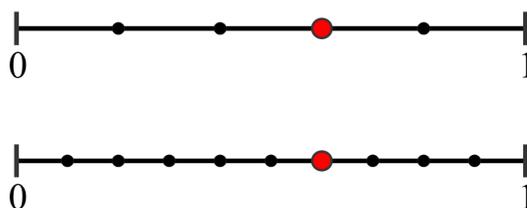
Equivalent Fractions

If you eat half of a pizza, or $\frac{2}{4}$ of a pizza, you have eaten the same amount. The two fractions are *equivalent*.

We write an equal sign between them: $\frac{1}{2} = \frac{2}{4}$.



The dot for $\frac{3}{5}$ is in the same place on the number line as the dot for $\frac{6}{10}$. Again, the two fractions are *equivalent*. We can write $\frac{3}{5} = \frac{6}{10}$.



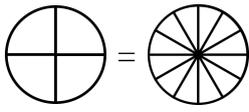
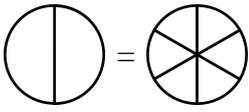
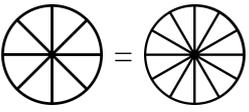
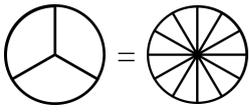
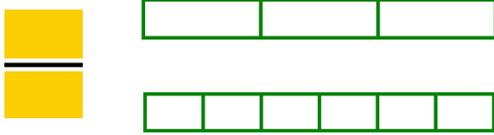
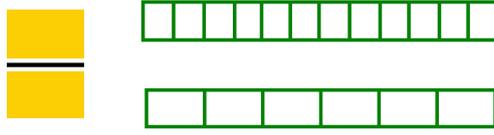
1. Write the equivalent fractions.

 $\frac{1}{4} = \frac{2}{8}$	 $\frac{2}{3} = \frac{4}{6}$	 $\frac{3}{6} = \frac{1}{2}$	 $\frac{3}{5} = \frac{2}{3}$
<p>a. $\frac{\quad}{\quad} = \frac{\quad}{\quad}$</p>	<p>b. $\frac{\quad}{\quad} = \frac{\quad}{\quad}$</p>	<p>c. $\frac{\quad}{\quad} = \frac{\quad}{\quad}$</p>	<p>d. $\frac{\quad}{\quad} = \frac{\quad}{\quad}$</p>
<p>e. $\frac{\quad}{\quad} = \frac{\quad}{\quad}$</p>	<p>f. $\frac{\quad}{\quad} = \frac{\quad}{\quad}$</p>		

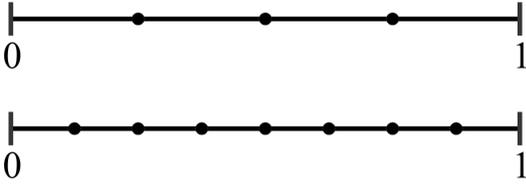
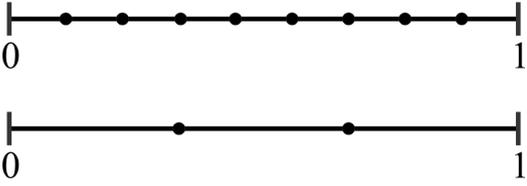
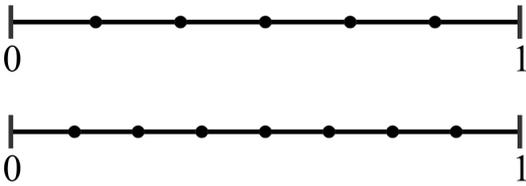
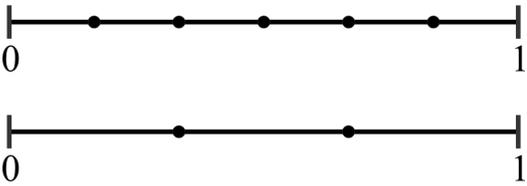
2. Write the equivalent fractions.

 <p>a. $\frac{\quad}{\quad} = \frac{\quad}{\quad}$</p>	 <p>b. $\frac{\quad}{\quad} = \frac{\quad}{\quad}$</p>
---	---

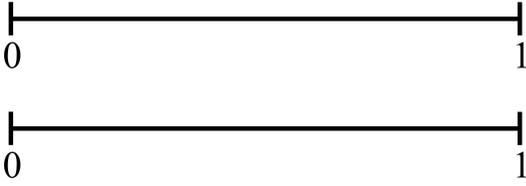
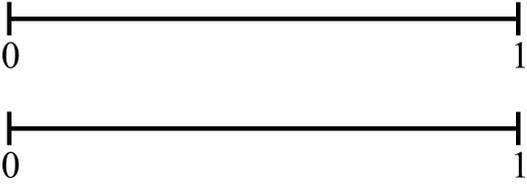
3. Shade the parts for the first fraction. Shade the same *amount* in the second picture. Write the second fraction.

 <p>a. $\frac{1}{4} =$</p>	 <p>b. $\frac{1}{2} =$</p>	 <p>c. $\frac{6}{8} =$</p>	 <p>d. $\frac{2}{3} =$</p>
<p>e. $\frac{1}{3} =$</p> 	<p>f. $\frac{8}{12} =$</p> 		

4. Mark the equivalent fractions on the number lines.

 <p>a. $\frac{3}{4} = \frac{6}{8}$</p>	 <p>b. $\frac{3}{9} = \frac{1}{3}$</p>
 <p>c. $\frac{3}{6} =$</p> 	 <p>d. $\frac{2}{6} =$</p> 

5. Mark the equivalent fractions on the number lines. This time, you need to first divide each number line into equal parts.

 <p>a. $\frac{2}{4} = \frac{1}{2}$</p>	 <p>b. $\frac{2}{3} = \frac{4}{6}$</p>
--	---

6. Colour in and write many fractions that are equivalent to the first fraction.

<p>a.</p> <div style="display: flex; align-items: center; margin-bottom: 10px;"> <div style="border: 1px solid black; width: 100px; height: 20px; margin-right: 10px;"></div> <div style="text-align: center;">$\frac{1}{3}$</div> </div> <div style="display: flex; align-items: center; margin-bottom: 10px;"> <div style="border: 1px solid black; width: 100px; height: 20px; margin-right: 10px;"></div> <div style="width: 20px; height: 20px; background-color: yellow; margin-right: 10px;"></div> <div style="border-top: 1px solid black; width: 100%;"></div> </div> <div style="display: flex; align-items: center; margin-bottom: 10px;"> <div style="border: 1px solid black; width: 100px; height: 20px; margin-right: 10px;"></div> <div style="width: 20px; height: 20px; background-color: yellow; margin-right: 10px;"></div> <div style="border-top: 1px solid black; width: 100%;"></div> </div> <div style="display: flex; align-items: center;"> <div style="border: 1px solid black; width: 100px; height: 20px; margin-right: 10px;"></div> <div style="width: 20px; height: 20px; background-color: yellow; margin-right: 10px;"></div> <div style="border-top: 1px solid black; width: 100%;"></div> </div>	<p>b.</p> <div style="display: flex; align-items: center; margin-bottom: 10px;"> <div style="border: 1px solid black; width: 100px; height: 20px; margin-right: 10px;"></div> <div style="text-align: center;">$\frac{1}{4}$</div> </div> <div style="display: flex; align-items: center; margin-bottom: 10px;"> <div style="border: 1px solid black; width: 100px; height: 20px; margin-right: 10px;"></div> <div style="width: 20px; height: 20px; background-color: yellow; margin-right: 10px;"></div> <div style="border-top: 1px solid black; width: 100%;"></div> </div> <div style="display: flex; align-items: center; margin-bottom: 10px;"> <div style="border: 1px solid black; width: 100px; height: 20px; margin-right: 10px;"></div> <div style="width: 20px; height: 20px; background-color: yellow; margin-right: 10px;"></div> <div style="border-top: 1px solid black; width: 100%;"></div> </div> <div style="display: flex; align-items: center;"> <div style="border: 1px solid black; width: 100px; height: 20px; margin-right: 10px;"></div> <div style="width: 20px; height: 20px; background-color: yellow; margin-right: 10px;"></div> <div style="border-top: 1px solid black; width: 100%;"></div> </div>
--	--

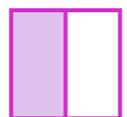
7. Four children have a chocolate bar to share. Lerato says, "Let's divide it into four equal pieces, and everybody gets one piece." Ansie says, "No, let's divide it into twelve equal pieces and everybody gets three pieces."



Whose idea lets everybody get a fair share?

8. Draw a picture to show that $\frac{1}{2} = \frac{4}{8}$.

9. a. Half of the pie is left. Show in the picture how three persons can share it equally.



b. What two equivalent fractions can you write from your "cutting"?

10. Are $\frac{5}{5}$ and $\frac{4}{4}$ equivalent fractions?
Why or why not?

Puzzle Corner

Which is longer, a line that is $3\frac{1}{2}$ centimetres long or a line that is $3\frac{1}{4}$ centimetres long?
How much longer is it?