Use your judgment in grading. You can give points or partial points for partial answers.

| Question \# | Max. points | Student score |
| :---: | :---: | :---: |
| Exponents and Scientific Notation |  |  |
| 1 | 8 points |  |
| 2 | 9 points |  |
| 3 | 4 points |  |
| 4 | 2 points |  |
| 5 | 2 points |  |
|  | subtotal | / 25 |
| Irrational Numbers |  |  |
| 6 | 5 points |  |
| 7 | 5 points |  |
| 8 | 3 points |  |
| 9 | 2 points |  |
|  | subtotal | / 15 |
| Geometry |  |  |
| 10 | 3 points |  |
| 11 | 2 points |  |
| 12 | 3 points |  |
| 13 | 2 points |  |
| 14a | 3 points |  |
| 14b | 3 points |  |
| 15 | 3 points |  |
| 16 | 3 points |  |
|  | subtotal | / 22 |
| Linear Equations |  |  |
| 17 | 4 points |  |
| 18 | 4 points |  |
| 19 | 6 points |  |
| 20 | 2 points |  |
| 21 | 2 points |  |
| 22 | 3 points |  |
|  | subtotal | /21 |
| Functions |  |  |
| 23 | 2 points |  |
| 24a | 1 point |  |
| 24b | 2 points |  |
| 24c | 2 points |  |


| Question \# | Max. points | Student score |
| :---: | :---: | :---: |
| Functions |  |  |
| 25a | 1 point |  |
| 25b | 1 point |  |
| 25c | 1 point |  |
| 25d | 1 point |  |
| 25e | 1 point |  |
| 26a | 2 points |  |
| 26b | 1 point |  |
| 26c | 1 point |  |
| 26d | 1 point |  |
|  | subtotal | /17 |
| Graphing Linear Equations |  |  |
| 27a | 1 point |  |
| 27b | 1 point |  |
| 27c | 2 points |  |
| 28 | 3 points |  |
| 29 | 3 points |  |
| 30 | 3 points |  |
|  | subtotal | /13 |
| The Pythagorean Theorem |  |  |
| 31 | 4 points |  |
| 32 | 3 points |  |
| 33 | 3 points |  |
|  | subtotal | /10 |
| Systems of Linear Equations |  |  |
| 34 | 6 points |  |
| 35 | 3 points |  |
| 36 | 3 points |  |
| 37 | 3 points |  |
|  | subtotal | /15 |
| Bivariate Data |  |  |
| 38 | 3 points |  |
| 39 | 3 points |  |
| 40 | 3 points |  |
| 41 | 5 points |  |
|  | subtotal | /14 |
|  | TOTAL | /152 |

## Exponents and Scientific Notation

1. a. -16
b. 16
c. $1 / 49$
d. 36
e. 0.031
f. 110,000
g. $-8 / 27$
h. 64
2. 

| a. $-8 s^{3}$ | b. $144 x^{2}$ | c. $y^{15}$ |
| :--- | :--- | :--- |
| d. $-6 x^{8}$ | e. $\frac{1}{y^{6}}$ | f. $\frac{1}{4 v^{2}}$ |
| g. $\frac{49 x^{2}}{9 y^{2}}$ | h. $\frac{-x^{3}}{125}$ | i. $\frac{81 b^{4}}{c^{20}}$ |

3. a. $1.93 \cdot 10^{8}$
b. $3.0805 \cdot 10^{12}$
c. $4.6 \cdot 10^{-4}$
d. $9 \cdot 10^{-7}$
4. $\frac{6.0 \cdot 10^{24} \mathrm{~kg}}{1.0 \cdot 10^{26} \mathrm{~kg}}=\frac{6.0}{10^{2}}=6 / 100=3 / 50$. The earth's mass is (about) $3 / 50$ of Neptune's mass.
5. We need to divide to find out how many gold atoms "fit" into 99 grams of gold:
$\frac{9.9 \cdot 10^{1} \mathrm{~g}}{3.3 \cdot 10^{-22} \mathrm{~g}}=3 \cdot 10^{23}$. There are about $3 \cdot 10^{23}$ gold atoms in 99 grams of gold.

## Irrational Numbers


7.

$\begin{array}{lll}\text { 8. a. } x=\sqrt{54} \text { or } x=-\sqrt{54} & \text { b. } n=7 \text { or } n=-7 & \text { c. } z=4\end{array}$
9. Let $x=0 . \overline{71}$. Then $100 x=71 . \overline{71}$. Subtracting those, we get:

$$
\begin{aligned}
100 x & =71.717171 \ldots \\
-\quad x & =\frac{0.717171 \ldots}{71} \\
\hline 99 x & = \\
x & =\underline{71 / 99}
\end{aligned}
$$

## Geometry

10. Answers will vary. Check the student's answer. For example:

First, dilate triangle ABC from point A with scale factor 2/3. Then translate it 8 units to the right.
Lastly, reflect it in the horizontal line $y=-1.5$.
(See the image on the right.)
But there are many possible answers. Here is another one.
First, reflect the triangle ABC in the horizontal line $y=-1.5$. Then, translate it 8 units to the right.
Lastly, dilate it from point A" with scale factor 2/3.
Another one:
First, translate the triangle ABC 8 units to the right.
Then dilate it from point A' with scale factor $2 / 3$.
Lastly, reflect it in the horizontal line $y=-1.5$.

11. Answers will vary. Check the student's answer. For example:

First, rotate trapezoid ABCD $90^{\circ}$ counterclockwise around the origin.
Then, dilate it from point C' with scale factor $1 / 2$.
(See the image on the right.)
Another way:
First, dilate trapezoid ABCD from point C with scale factor 1/2. Then rotate it $90^{\circ}$ counterclockwise around the origin.

12. The bottom row of the table gives the coordinates after all the transformations.

| Position | Vertices |  |  |
| :--- | :---: | :---: | :---: |
| Original | $\mathrm{A}(-2,5)$ | $\mathrm{B}(-5,4)$ | $\mathrm{C}(-3,0)$ |
| After reflection in $y$-axis | $\mathrm{A}^{\prime}(2,5)$ | $\mathrm{B}^{\prime}(5,4)$ | $\mathrm{C}^{\prime}(3,0)$ |
| After translation (2 units down, 1 to the left) | $\mathrm{A}^{\prime \prime}(1,3)$ | $\mathrm{B} "(4,2)$ | C "(2, -2$)$ |
| After rotation (90 ${ }^{\circ}$ clockwise around the origin) | A '"(3, -1$)$ | $\mathrm{B} "(2,-4)$ | $\mathrm{C} "(-2,-2)$ |

13. Since the sum of the angles in a triangle is $180^{\circ}$, in triangle CDE, angle $a=180^{\circ}-52^{\circ}-51^{\circ}=77^{\circ}$.
Similarly, in triangle ABC, angle $b=180^{\circ}-52^{\circ}-59^{\circ}=69^{\circ}$.
Angles $a, x$, and $b$ form a straight angle, so, $x=180^{\circ}-a-b$
$=180^{\circ}-77^{\circ}-69^{\circ}=\underline{34^{\circ}}$.

14. a. Angle $\mathrm{BAC}=180-(x+26)=154-x$. Now, the angle sum of triangle ABC is $180^{\circ}$, so, we can write an equation using that fact, and then solve for $x$ :

$$
\begin{aligned}
\angle \mathrm{BAC}+\angle \mathrm{ABC}+\angle \mathrm{BCA} & =180 \\
154-x+x-48+x-7 & =180 \\
x+99 & =180 \\
x & =81
\end{aligned}
$$

b. Since $m$ and $n$ are parallel, angles $y$ and BAC are corresponding angles, thus congruent.

So, $y=154^{\circ}-x=154^{\circ}-81^{\circ}=\underline{73^{\circ}}$.
15. $\mathrm{V}=(4 / 3) \cdot \pi(3.0 \mathrm{in})^{3} \cdot(2 / 3) \approx 75.398$ cubic inches. In cups, this is 5.2 cups or about $51 / 4$ cups.
16. Let $h$ be the height of the cup. Then, the volume is given by $\mathrm{V}=\pi(3.1 \mathrm{~cm})^{2} \cdot h=340 \mathrm{ml}$. This is an equation that we can use to solve for $h$. Since $1 \mathrm{ml}=1$ cubic centimeter, the equation becomes $\pi(3.1 \mathrm{~cm})^{2} \cdot h=340 \mathrm{~cm}^{3}$, from which $h=\left(340 \mathrm{~cm}^{3}\right) /\left(\pi \cdot 3.1^{2} \mathrm{~cm}^{2}\right) \approx \underline{11.3 \mathrm{~cm}}$.

## Linear Equations

17. 

| a. | $\begin{aligned} 10 s+8 & =7 s-2(s-5) \\ 10 s+8 & =7 s-2 s+10 \\ 10 s+8 & =5 s+10 \\ 5 s & =2 \\ s & =2 / 5 \end{aligned}$ | b. | $\begin{aligned} 20-3(x+4) & =14-5 x \\ 20-3 x-12 & =14-5 x \\ 8-3 x & =14-5 x \\ 2 x & =6 \\ x & =3 \end{aligned}$ |
| :---: | :---: | :---: | :---: |

18. 


19.

$$
\text { a. } \quad \begin{aligned}
6 x-1 & =6(x-1) \\
6 x-1 & =6 x-6 \\
-1 & =-6
\end{aligned}
$$

No solutions.
b. $\quad-5 x+1=6(x-1)-5$
$-5 x+1=6 x-6-5$
$-5 x+1=6 x-11$
$-11 x=-12$
$x=12 / 11$
One solution.

$$
\text { c. } \quad \begin{aligned}
6 x-12 & =6(x-2) \\
6 x-12 & =6 x-12 \\
0 & =0
\end{aligned}
$$

An infinite number of solutions. Any value of $x$ is a solution.
20. Let $d$ be the amount of discount. The non-discounted blocks cost $3000(\$ 1.35)=\$ 4,050$.

The discounted blocks cost $1500(1.35-d)$. The total of these equals $\$ 5,775$.

$$
\begin{aligned}
4050+1500(1.35-d) & =5775 \\
4050+2025-1500 d & =5775 \\
6075-1500 d & =5775 \\
-1500 d & =-300 \\
d & =3 / 15=1 / 5=0.2
\end{aligned}
$$

The discount was $\$ 0.20$ per block. In other words, he paid $\$ 1.15$ each for the 1500 blocks.
21. Let $x$ be the first one of the four consecutive numbers. Then:

$$
\begin{aligned}
x+(x+1)+(x+2)+(x+3) & =2342 \\
4 x+6 & =2342 \\
4 x & =2336 \\
x & =584
\end{aligned}
$$

The numbers are $584,585,586$, and 587.
22. Let $p$ be the original price of the item. Then:

$$
\begin{aligned}
1.06(0.73 p) & =34.82 \\
0.7738 p & =34.82 \\
p & \approx 44.9987
\end{aligned}
$$

The item cost $\$ 45.00$ originally.

## Functions

23. a. Because 3 is mapped to two different outputs: to 0 and to 3 .
b. The number 6 works. If you place either 3 or 9 there, then you will have the same input mapping to two distinct outputs, which would make it not a function.
24. a. Farm B's pricing system is a linear function. $C=6.25 w$.
b. For Farm A, the rate of change is $(21.5-15) /(3-2)=6.5$, or $\$ 6.50$ per kg. For Farm B, the change of rate is 6.25 , or $\$ 6.25$ per kg.
c. At Farm A, 4 kg will cost about $\$ 27$, and at Farm B, $\$ 25$. So, Farm B has the better deal. For 7 kg , Farm B charges you $\$ 40$ and Farm B $\$ 43.75$, so, Farm A has the better deal.
25. a. \$10.
b. That there is an initial fee of $\$ 10$ just to get to go riding.
c. $\$ 1$ per minute.
d. Horse riding will cost you $\$ 1$ per minute, on top of the $\$ 10$ initial fee.
e. cost $=10+t$, where $t$ is the number of minutes you will go riding.
26. a. From $x=0$ to $x=4$ : linear and increasing

From $x=4$ to $x=8$ : nonlinear and decreasing
From $x=8$ to $x=11$ : linear and decreasing
From $x=11$ to $x=15$ : nonlinear and increasing

c. $y=-(5 / 4) x+30$
d. For the function in green: the rate of change is $-5 / 3$. For the function in red, it is $-5 / 4$.

## Graphing Linear Equations

27. a. $y=(-2 / 3) x+4$
b. $y=-3$
c. $y=5 x-25$
28. a. Fridge 1 ( 120 kWh versus 100 kWh ). It consumes 20 kWh more than Fridge 2.
b. Fridge 1 : $\mathrm{E}=40 t$. Fridge 2 : $\mathrm{E}=(100 / 3) t$. It is also acceptable to write it with a rounded decimal, as $\mathrm{E}=33.3 t$.
c. energy

29. 


30. The slope of this line can be calculated using the two given points. It is $(-6-14) /(-7-3)=-20 /(-10)=2$. The equation of this line is therefore of the form $y=2 x+b$. Substituting $(3,14)$ into it, we get $14=2(3)+b$, from which $b=8$. So, the equation is $y=2 x+8$. Since point $(a, 2)$ is on this line, let's substitute those values into the equation of the line:

$$
\begin{aligned}
2 & =2 a+8 \\
-6 & =2 a \\
a & =-3
\end{aligned}
$$

So, $\underline{a=-3}$. There are also other ways to arrive to the final answer, such as using the formula for the slope.

## The Pythagorean Theorem

31. Using the Pythagorean Theorem, we get:
a. $r^{2}+17.5^{2}=26.6^{2}$
$r^{2}=26.6^{2}-17.5^{2}$
$r^{2}=401.31$
$r=\sqrt{401.31} \approx 20.0$

We ignore the negative root since this is a length of a side. The unknown side measures 20.0 units.
b. $x^{2}+x^{2}=(\sqrt{70})^{2}$
$2 x^{2}=70$
$x^{2}=35$
$x=\sqrt{35}$

We ignore the negative root since this is a length of a side. The unknown side measures $\sqrt{35}$ units.
32. The rafter, the height of 1 ft 10 in , and half of the 6 ft 8 in span form a right triangle. In this triangle, using inches instead of feet and inches, the two legs measure 22 in and 40 in . Now, let $r$ be the length of the rafter. According to the Pythagorean Theorem:

$$
\begin{aligned}
r^{2} & =22^{2}+40^{2} \\
r^{2} & =2,084 \\
r & =\sqrt{2,084} \approx 45.651
\end{aligned}
$$

The decimal portion, 0.651 inches, can be converted into 16th parts of an inch this way. Let $x$ be the number of 16 th parts of an inch that equals 0.651 . Then, $x / 16=0.651$, from which $x=0.651(16)=10.416$.
So, the rafter measures 3 ft 9 10/16 in.
33. a. To find the height, we will use the right triangle ABC. First, we need to find the length of the diagonal of the bottom square (d). From the Pythagorean Theorem:

$$
\begin{aligned}
d^{2} & =36.0^{2}+36.0^{2} \\
d^{2} & =2592 \\
d & =\sqrt{2592}
\end{aligned}
$$

Next, we apply the Pythagorean Theorem to triangle ABC. Note that one of its legs is $d / 2$ (half of the diagonal), the other leg is the height of the pyramid (h),
 and the hypotenuse is the $33-\mathrm{cm}$ edge of the pyramid.

$$
\begin{aligned}
h^{2}+(\sqrt{2592} / 2)^{2} & =33.0^{2} \\
h^{2}+2592 / 4 & =1,089 \\
h^{2} & =1,089-648 \\
h & =\sqrt{441}=21
\end{aligned}
$$

The height of the pyramid is 21.0 cm .
b. The volume is $V=36.0 \mathrm{~cm} \cdot 36.0 \mathrm{~cm} \cdot 21.0 \mathrm{~cm} / 3=\underline{\underline{9}, 072 \mathrm{~cm}^{3}}$.

## Systems of Linear Equations

34. 


35. a. No solutions. b. One solution. c. An infinite number of solutions.
36. Let $x$ be the number of tables that seat 4 , and $y$ be the number of tables that seat 6 .

We can write this system of equations: $\left\{\begin{array}{l}x+y=106 \\ 4 x+6 y=500\end{array}\right.$
Solving for $y$ from the top equation, we get $y=106-x$. Substituting that in the bottom equation, we get:

$$
\begin{aligned}
4 x+6(106-x) & =500 \\
4 x+636-6 x & =500 \\
636-2 x & =500 \\
-2 x & =-136 \\
x & =68
\end{aligned}
$$

Then, $y=106-x=106-68=38$. The restaurant has 68 tables that seat 4 , and 38 tables that seat 6.
37. Let $G$ be Greta's age and $S$ be Susan's age. Then: $\left\{\begin{array}{l}G+10=(3 / 4)(S+10) \\ G+S=127\end{array}\right.$

From the bottom equation, we can solve that $G=127-S$. Substituting that in the top equation, we get:

$$
\begin{aligned}
127-S+10 & =(3 / 4)(S+10) & \\
137-S & =(3 / 4) S+7.5 & \cdot \mathbf{4} \\
548-4 S & =3 S+30 & +4 S \\
548 & =7 S+30 & -30 \\
518 & =7 S & \div 7 \\
S & =74 &
\end{aligned}
$$

Then, $G=127-74=53$. Greta is 53 and Susan is 74.

## Bivariate Data

38. a. Nonlinear and decreasing association. b. No association. c. Linear and increasing association.
39. There is no association between the variables. For each age group, there is about an equal number of people who exercise and who do not exercise. (In other words, in each age group the relative frequencies for "Exercises" and "Does not exercise" would be close to $50 \%$.).
40. a. 6
b. 24
c. 3
41. a. Answers will vary. Check the student's answer. For example:

b. Answers will vary. Check the student's answer. The line above goes through ( 6,45 ), and $(10,54)$.

Therefore, its slope is $9 / 4=2.25$, and its equation is of the form $y=2.25 x+b$. Substituting $(10,54)$ into this allows us to solve for $b$ : $54=2.25(10)+b$, from which $b=31.5$. So, the equation is $y=2.25 x+31.5$.
c. It means that each 1-year increment of age is associated with a 2.1-inch increment in height. In other words, boys tend to grow 2.1 inches per year.
d. The $y$-intercept of 32.6 inches means that this equation predicts a newborn baby to be 32.6 inches tall. However, we know newborns are not that tall; they are typically between 18-22 inches tall. They grow very fast during the first year. Then from about age 2 onward, the growth follows fairly closely a linear pattern. This shows us that we cannot extrapolate backwards all the way to zero years using this data and this equation.
e. We solve the equation $50.5=2.1 x+32.6$ for $x$ :

$$
\begin{aligned}
50.5 & =2.1 x+32.6 \\
50.5 & =2.1 x+32.6 \\
17.9 & =2.1 x \\
x & =8.52
\end{aligned}
$$

The equation predicts the age of about 8.5 years for a boy that is 50.5 inches tall.

