End-of-the-Year Test Grade 4

This test is quite long, so I do not recommend that your child/student does all of it in one sitting. Break it into parts and administer them on several days. Use your judgment.

This is to be used as a diagnostic test. Thus, you may even skip those areas and concepts that you already know for sure your student has mastered.

The test does not cover every single concept that is covered in the Math Mammoth Grade 4 Complete Curriculum, but all the major concepts and ideas are tested here. This test is evaluating the child's ability in the following content areas:

- addition and subtraction
- early algebraic thinking
- the order of operations
- graphs
- large numbers and place value
- rounding and estimating
- multi-digit multiplication
- word problems
- some basic conversions between measuring units
- measuring length
- time calculations
- long division
- the concept of remainder
- factors
- area and perimeter
- measuring and drawing angles
- classifying triangles according to their angles
- adding and subtracting fractions and mixed numbers (like fractional parts)
- equivalent fractions
- comparing fractions
- multiplying fractions by whole numbers
- the concept of a decimal (tenths/hundredths)
- comparing decimals

In order to continue with the Math Mammoth Grade 5 Complete Curriculum, I recommend that the child gain a score of 80% on this test, and that the teacher or parent review with him any content areas where he is weak. Children scoring between 70 and 80% may also continue with grade 5, depending on the types of errors (careless errors or not remembering something, vs. the lack of understanding). The most important content areas to master are multi-digit multiplication, long division, place value, and word problems. Again, use your judgment.
**Instructions to the student:**

Do not use the calculator. Answer each question in the space provided.

**Instructions to the teacher:**

My suggestion for grading is below. The total is 192 points. A score of 154 points is 80%.

### Question | Max. points | Student score | Question | Max. points | Student score
--- | --- | --- | --- | --- | ---
**Addition, Subtraction, Patterns, and Graphs**
1 | 2 points |  | 22 | 2 points |  
2a | 1 point |  | 23 | 1 point |  
2b | 2 points |  | 24 | 3 points |  
3 | 2 points |  | 25 | 2 points |  
4 | 6 points |  | 26 | 6 points |  
5 | 4 points |  | 27 | 6 points |  
6 | 2 points |  | 28 | 2 points |  
7 | 4 points |  | 29 | 1 point |  
8 | 3 points | **subtotal** / 26 | 30 | 2 points |  
**Large Numbers and Place Value**
9 | 3 points |  | 31 | 4 points |  
10 | 2 points |  | 32 | 3 points |  
11 | 3 points |  | 33 | 4 points |  
12 | 3 points |  | 34a | 3 points |  
13 | 2 points |  | 34b | 2 points |  
14 | 3 points |  | 35 | 6 points |  
15 | 3 points |  | 36 | 4 points |  
16 | 4 points | **subtotal** / 23 | 37 | 2 points |  
17 | 6 points |  | 38 | 4 points |  
18 | 3 points |  | 39 | 2 points |  
19 | 8 points |  | 40 | 2 points |  
20 | 3 points |  | 41 | 3 points |  
21a | 3 points |  | 42 | 2 points |  
21b | 2 points |  | 43 | 2 points |  
21c | 2 points |  | 44 | 1 point |  
21d | 3 points | **subtotal** / 30 | 45 | 2 points |  
**Time and Measuring**
22 | 2 points |  | 46 | 3 points |  
23 | 1 point | **subtotal** / 25 |  
24 | 3 points |  
25 | 2 points |  
26 | 6 points |  
27 | 6 points |  
28 | 2 points |  
29 | 1 point |  
30 | 2 points |  
**Division and Factors**
31 | 4 points |  
32 | 3 points |  
33 | 4 points |  
34a | 3 points |  
34b | 2 points |  
35 | 6 points |  
36 | 4 points |  
37 | 2 points |  
38 | 4 points | **subtotal** / 32 |  
39 | 2 points |  
40 | 2 points |  
41 | 3 points |  
42 | 2 points |  
43 | 2 points |  
44 | 1 point |  
45 | 2 points |  
46 | 3 points | **subtotal** / 17 |  
**Geometry**
39 | 2 points |  
40 | 2 points |  
41 | 3 points |  
42 | 2 points |  
43 | 2 points |  
44 | 1 point |  
45 | 2 points |  
46 | 3 points | **subtotal** / 17 |
<table>
<thead>
<tr>
<th>Question</th>
<th>Max. points</th>
<th>Student score</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fractions and Decimals</td>
<td></td>
<td></td>
</tr>
<tr>
<td>47</td>
<td>1 point</td>
<td></td>
</tr>
<tr>
<td>48</td>
<td>1 point</td>
<td></td>
</tr>
<tr>
<td>49</td>
<td>3 points</td>
<td></td>
</tr>
<tr>
<td>50</td>
<td>2 points</td>
<td></td>
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<tr>
<td>51</td>
<td>4 points</td>
<td></td>
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<tr>
<td>52</td>
<td>4 points</td>
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<tr>
<td>53</td>
<td>2 points</td>
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<tr>
<td>54</td>
<td>1 point</td>
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<td>55</td>
<td>3 points</td>
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<tr>
<td>56</td>
<td>4 points</td>
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<tr>
<td>57</td>
<td>4 points</td>
<td></td>
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<tr>
<td>58</td>
<td>4 points</td>
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<tr>
<td>59</td>
<td>4 points</td>
<td></td>
</tr>
<tr>
<td>60</td>
<td>2 points</td>
<td></td>
</tr>
<tr>
<td><strong>subtotal</strong></td>
<td></td>
<td>/ 39</td>
</tr>
<tr>
<td><strong>TOTAL</strong></td>
<td></td>
<td>/ 192</td>
</tr>
</tbody>
</table>
Addition, Subtraction, Patterns, and Graphs

1. Subtract. Check by adding.

\[ 5,200 - 2,677 - 543 \]

Add to check:

2. a. Round the prices to the nearest dollar. Use the rounded prices to estimate the total bill.

crackers $1.28, cheese $8.92, jam $3.77, butter $9.34.

b. Now, use the exact prices (not rounded prices). Mrs. Wood buys the items listed above and pays with $30. What is her change?
3. *Estimate* the cost of buying five notebooks for $0.87 each and two pencil cases for $1.24 each.

4. Calculate in the right order.

| a. $3 \times (4 + 6) = \underline{\text{______}}$ | b. $3 \times 3 + 8 \div 4 = \underline{\text{______}}$ | c. $20 \times 3 + 80 \div 1 = \underline{\text{______}}$ |
| 100 – 4 \times 4 = \underline{\text{______}} | (7 – 3) \times 3 + 2 = \underline{\text{______}} | 15 + 2 \times (8 – 6) = \underline{\text{______}} |

5. Circle the number sentence that fits the problem. Then solve for *x*.

| a. Alice had $35. Then she earned more money (*x*). Now she has $92. | b. Eric gave 24 of the cookies he had baked to a friend and now he has 37 cookies left. |
| $35 + x = 92 \quad \text{OR} \quad 35 + 92 = x$ | $37 – 24 = x \quad \text{OR} \quad x – 24 = 37$ |

6. a. Continue this pattern for four more numbers:

2,000  1,750  1,500  1,250

b. Write a list of six numbers that follows this pattern: Start at 200, and add 300 each time.

7. These numbers are the students' quiz scores. 2 5 8 7 6 6 7 10 10 4 7 8 6 8 5 9 9 8 6 6 5 7 9

Make a frequency table and a bar graph.

<table>
<thead>
<tr>
<th>Quiz score</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td></td>
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<tr>
<td>7</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td></td>
</tr>
<tr>
<td>9</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td></td>
</tr>
</tbody>
</table>

![Bar graph]

students

quiz score
8. Write an addition or a subtraction with an unknown (x or ?). Solve it. The bar model can help.

Rubber boots used to cost $27.95 but now the price is $21.45. How much is the discount?

______________________________
______________________________

Large Numbers and Place Value

9. Subtract from whole thousands.

<table>
<thead>
<tr>
<th>a. 2,000 − 1 = _____</th>
<th>b. 5,000 − 20 = _____</th>
<th>c. 6,000 − 300 = _____</th>
</tr>
</thead>
</table>

10. Write the numbers in the normal form.

   a. 800 thousand 50
   b. 25 thousand 4 hundred 7

11. Find the missing numbers.

<table>
<thead>
<tr>
<th>a. 30,550 = 50 + __________ + 500</th>
<th>b. 809,100 = 800,000 + 100 + __________</th>
</tr>
</thead>
<tbody>
<tr>
<td>c. 725,608 = 20,000 + 700,000 + 8 + __________ + 5,000</td>
<td></td>
</tr>
</tbody>
</table>

12. Compare, writing <, >, or = between the numbers.

   a. 54,500  55,400
   b. 108,882  108,828
   c. 71,600  61,700

13. Write the numbers in order from the smallest to the greatest.

   217,200  227,712  27,200  227,200

14. Round the numbers as the dashed line indicates (to the underlined digit).

   a. 436,102 ≈
   b. 89756 ≈
   c. 27,529 ≈

15. Round to the nearest ten thousand.

   a. 426,889 ≈
   b. 495,304 ≈
   c. 7,345 ≈
16. Calculate. Line up all of the place value units carefully.

\[
\begin{align*}
a. \quad 476,708 + 24,392 + 563 & \quad b. \quad 405,112 - 81,424 \\
\end{align*}
\]

Multi-Digit Multiplication

17. Multiply, and find the missing factors.

\[
\begin{array}{ccc}
a. \quad 70 \times 3 & \quad b. \quad 6 \times 800 & \quad c. \quad 40 \times 80 \\
d. \quad \_ \times 3 & = 360 & \quad e. \quad 50 \times \_ & = 4,000 \\
f. \quad \_ \times 300 & = 21,000 \\
\end{array}
\]

18. Ed earns $20 per hour.
   a. How much will he earn in an 8-hour workday? ______________________________________
   b. How much will he earn in a 40-hour workweek? ______________________________________
   c. How many days will he need to work in order to earn at least $600? ______________________

19. Multiply. Estimate the answer on the line.

\[
\begin{array}{cccc}
a. \quad 5 \times 196 & \quad b. \quad 35 \times 38 & \quad c. \quad 7 \times 3,188 & \quad d. \quad 89 \times 22 \\
\approx \__ & \quad \approx \__ & \quad \approx \__ & \quad \approx \__ \\
\end{array}
\]
20. Write the area of the whole rectangle as a SUM of the areas of the smaller rectangles. Lastly, add to find the total area.

\[
\text{Area} = 8 \times 127 \\
= \underline{\phantom{0}} \times \underline{\phantom{0}} + \underline{\phantom{0}} \times \underline{\phantom{0}} + \underline{\phantom{0}} \times \underline{\phantom{0}} \\
= \underline{\phantom{0}}
\]

21. Solve the problems. Write a number sentence or several for each problem.

a. Find the change, if Sally buys 26 shirts for $14 each, and pays with $400.

___________________________________

___________________________________

Estimate: ___________________________

b. How many minutes are there in a day (24 hours)?

___________________________________

___________________________________

c. One side of a square is 375 cm. What is its perimeter?

___________________________________

___________________________________

d. Bicycles that cost $277 were discounted by $58. A store bought eight. What was the total cost?

___________________________________

___________________________________
Time and Measuring

22. Measure the lines below to the nearest eighth of an inch and also in centimeters and millimeters.

   a. _______ in. or ______ cm ______ mm

   b. _______ in. or ______ cm ______ mm

23. How much time passes from 10:54 a.m. till 5:06 p.m.?

24. Luis kept track of how long it took him to do his homework:

<table>
<thead>
<tr>
<th>Monday</th>
<th>Tuesday</th>
<th>Wednesday</th>
<th>Thursday</th>
<th>Sunday</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 h 45 min</td>
<td>50 min</td>
<td>1 h 15 min</td>
<td>2 h 15 min</td>
<td>55 min</td>
</tr>
</tbody>
</table>

   How much time did he spend with homework in total?
   ________________________________

25. A teacher started her workday at 7:00 am, and stopped it at 3:35 pm. But in between, she had a 45-minute lunch break, and another break of 20 minutes. How many hours/minutes did she actually work?

26. Convert between the different measuring units.

   a. 6 lb = _________ oz  
   2 lb 11 oz = _________ oz

   b. 5 gal = _________ qt  
   2 qt = _________ cups

   c. 4 ft 2 in. = _________ in.  
   7 yd = _________ ft
27. Convert between the different measuring units.

<table>
<thead>
<tr>
<th></th>
<th>a.</th>
<th></th>
<th>b.</th>
<th></th>
<th>c.</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>2 kg = __________ g</td>
<td>5 L 200 ml = __________ ml</td>
<td>8 cm 2 mm = __________ mm</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>11 kg 600 g = __________ g</td>
<td>3 m = __________ cm</td>
<td>10 km = __________ m</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

28. George jogs daily on a track through the woods that is 3 km 800 m long. What is the total distance he runs in four days?

29. Alice drank 350 ml of a 2-liter bottle of water. How much is left?

30. The long sides of a rectangle measure 5 ft 6 in, and the short sides are 3 ft 4 in. What is the perimeter? _____ ft _______ in

**Division and Factors**

31. Divide. Check each problem by multiplying.

<table>
<thead>
<tr>
<th></th>
<th>a. 567 ÷ 9 Check:</th>
<th>b. 8,564 ÷ 4 Check:</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
32. Solve.

| a. $47 \div 5 = _____ R ___ | b. $25 \div 3 = _____ R ___ | c. $57 \div 9 = _____ R ___ |

33. Solve.

a. Amy put 48 photographs into an online photo album. On each page she could fit nine photos. How many photos were on the last page? How many pages were full?

b. You bought a 50-foot roll of chain-link fence that cost $150. Then you sold 12 feet of it to your neighbor. How much did your neighbor pay?

34. Solve.

a. Joe had saved $264. He spent $3/8 of that to buy a camera. How much did the camera cost?

b. Mary packed 117 muffins into bags of six. How many bags does Mary need for them?

35. Mark an X if the number is divisible by the given numbers.

<table>
<thead>
<tr>
<th>number</th>
<th>divisible by 1</th>
<th>divisible by 2</th>
<th>divisible by 3</th>
<th>divisible by 4</th>
<th>divisible by 5</th>
<th>divisible by 6</th>
<th>divisible by 7</th>
<th>divisible by 8</th>
<th>divisible by 9</th>
<th>divisible by 10</th>
</tr>
</thead>
</table>
36. Fill in.

<table>
<thead>
<tr>
<th>a. Is 5 a factor of 60?</th>
<th>b. Is 7 a divisor of 43?</th>
</tr>
</thead>
<tbody>
<tr>
<td>_____, because _____ × _____ = _______</td>
<td>_____, because _____ ÷ _____ = _________</td>
</tr>
<tr>
<td>c. Is 96 divisible by 4?</td>
<td>d. Is 34 a multiple of 7?</td>
</tr>
<tr>
<td>_____, because ___________________________</td>
<td>_____, because ___________________________</td>
</tr>
</tbody>
</table>

37. List three prime numbers.

38. Find all the factors of the given numbers.

<table>
<thead>
<tr>
<th>a. 56</th>
<th>b. 78</th>
</tr>
</thead>
<tbody>
<tr>
<td>factors:</td>
<td>factors:</td>
</tr>
</tbody>
</table>

**Geometry**

39. Measure this angle.

40. Draw here an angle of 65°.
41. Draw here any obtuse triangle, and measure its angles.

42. Write an addition sentence about the angle measures. Use an unknown \((x)\) for one angle measure.

Then solve it.

\[
\begin{align*}
\text{Angle } \alpha &= 29^\circ \\
\text{Angle } x &= \text{ unknown angle}
\end{align*}
\]

43. Sketch here any rectangle. Then draw a diagonal line in it (a line from corner to corner). What kind of triangles are formed?

44. Sketch here two line segments that are perpendicular to each other.
45. Draw as many different symmetry lines as you can into these shapes.

46. This picture shows the floor of a room with a carpet on the floor. The room itself measures 28 feet by 12 feet. The carpet is 6 ft by 10 ft. Find the area of floor outside the carpet (not including the carpet).

Fractions and Decimals

47. Write an addition to match the picture:

48. Erica did 1/4 of a puzzle, and Mom did another fourth of it. How much of the puzzle is still left to do?

49. Add and subtract. Give your final answer as a whole number or as a mixed number if possible.

<table>
<thead>
<tr>
<th></th>
<th>a. ( \frac{4}{5} + \frac{3}{5} = )</th>
<th>b. ( 1\frac{1}{6} - \frac{2}{6} = )</th>
<th>c. ( 3\frac{6}{8} + 2\frac{2}{8} = )</th>
</tr>
</thead>
</table>

50. Split the existing pieces. Fill in the missing parts.

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>a. Each piece is split into 2 new ones.</td>
<td>b. Each piece is split into ____ new ones.</td>
<td></td>
</tr>
<tr>
<td>( \frac{4}{5} = )</td>
<td>( \frac{6}{9} = )</td>
<td></td>
</tr>
</tbody>
</table>
51. Write the equivalent fractions.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>a.</td>
<td>( \frac{2}{3} = \frac{\phantom{00}}{15} )</td>
</tr>
<tr>
<td>b.</td>
<td>( \frac{3}{5} = \frac{\phantom{00}}{9} )</td>
</tr>
<tr>
<td>c.</td>
<td>( \frac{1}{6} = \frac{\phantom{00}}{12} )</td>
</tr>
<tr>
<td>d.</td>
<td>( \frac{1}{3} = \frac{\phantom{00}}{9} )</td>
</tr>
</tbody>
</table>

52. Compare the fractions.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>a.</td>
<td>( \frac{2}{3} ) ( \frac{3}{8} )</td>
</tr>
<tr>
<td>b.</td>
<td>( \frac{6}{5} ) ( \frac{7}{8} )</td>
</tr>
<tr>
<td>c.</td>
<td>( \frac{11}{12} ) ( \frac{11}{10} )</td>
</tr>
<tr>
<td>d.</td>
<td>( \frac{1}{3} ) ( \frac{5}{12} )</td>
</tr>
</tbody>
</table>

53. Write these fractions in order, from the smallest to the greatest: \( \frac{5}{4} \) \( \frac{7}{10} \) \( \frac{65}{100} \)

54. A recipe calls for \( \frac{3}{4} \) cup of flour. If you triple the recipe, how much flour do you need?

55. Fill in.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>a.</td>
<td>( \frac{3}{8} = 3 \times \frac{\phantom{00}}{} )</td>
</tr>
<tr>
<td>b.</td>
<td>( 4 \times \frac{2}{5} = )</td>
</tr>
<tr>
<td>c.</td>
<td>( 7 \times \frac{2}{12} = )</td>
</tr>
</tbody>
</table>

56. Mark on the number line the following decimals: 0.55 0.08 0.27 0.80

57. Write the fractions and mixed numbers as decimals.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>a.</td>
<td>( \frac{3}{10} )</td>
</tr>
<tr>
<td>b.</td>
<td>( 3\frac{9}{10} )</td>
</tr>
<tr>
<td>c.</td>
<td>( \frac{9}{100} )</td>
</tr>
<tr>
<td>d.</td>
<td>( 7\frac{45}{100} )</td>
</tr>
</tbody>
</table>

58. Write the decimals as fractions or mixed numbers.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>a.</td>
<td>0.6</td>
</tr>
<tr>
<td>b.</td>
<td>6.7</td>
</tr>
<tr>
<td>c.</td>
<td>0.21</td>
</tr>
<tr>
<td>d.</td>
<td>5.05</td>
</tr>
</tbody>
</table>
59. Compare.

   a. 0.17 □ 0.2    b. 1.6 □ 1.56    c. 13.09 □ 13.9    d. 9.80 □ 9.8

60. Add and subtract.

   a. 7.81 + 5.2

   b. 6.1 − 2.36