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Foreword

Math Mammoth Grade 7 comprises a complete math curriculum for the seventh grade mathematics studies. It follows the Common Core Mathematics Standards (CCS) for 7th grade. Those standards are so constructed that students can continue to a traditional algebra 1 curriculum after studying this. However, you also have the option of following this course with Math Mammoth Grade 8, which provides a gentler and slower transition to high school math.

The main areas of study in Math Mammoth Grade 7 are:

- The basics of algebra (expressions, linear equations and inequalities);
- The four operations with integers and with rational numbers (including negative fractions and decimals);
- Ratios, proportions, and percent;
- Geometry;
- Probability and statistics.

This book, 7-A, covers the language of algebra (chapter 1), integers (chapter 2), one-step equations (chapter 3), rational numbers (chapter 4), and equations and inequalities (chapter 5). The rest of the topics are covered in the 7-B worktext.

I heartily recommend that you read the full user guide in the following pages.

I wish you success in teaching math! Maria Miller, the author

User Guide

Note: You can also find the information that follows online, at https://www.mathmammoth.com/userguides/ .

Basic principles in using Math Mammoth Complete Curriculum

Math Mammoth is mastery-based, which means it concentrates on a few major topics at a time, in order to study them in depth. The two books (parts A and B) are like a "framework", but you still have a lot of liberty in planning your student's studies. You can even use it in a *spiral* manner, if you prefer. Simply have your student study in 2-3 chapters simultaneously.

In seventh grade, the first five chapters should be studied in order. Also, chapter 7 (Percent) should be studied before studying any of the chapters 8, 9, or 10 (Geometry, Probability, Statistics). You can be flexible with the rest of the scheduling.

Math Mammoth is not a scripted curriculum. In other words, it is not spelling out in exact detail what the teacher is to do or say. Instead, Math Mammoth gives you, the teacher, various tools for teaching:

• The two student worktexts (parts A and B) contain all the lesson material and exercises. They include the explanations of the concepts (the teaching part) in blue boxes. The worktexts also contain some advice for the teacher in the "Introduction" of each chapter.

The teacher can read the teaching part of each lesson before the lesson, or read and study it together with the student in the lesson, or let the student read and study on his own. If you are a classroom teacher, you can copy the examples from the "blue teaching boxes" to the board and go through them on the board.

- There are hundreds of **videos** matched to the curriculum available at https://www.mathmammoth.com/videos/. There isn't a video for every lesson, but there are dozens of videos for each grade level. You can simply have the author teach your student!
- Don't automatically assign all the exercises. Use your judgment, trying to assign just enough for your student's needs. You can use the skipped exercises later for review. For most students, I recommend to start out by assigning about half of the available exercises. Adjust as necessary.
- For each chapter, there is a **link list to various free online games** and activities. These games can be used to supplement the math lessons, for learning math facts, or just for some fun. Each chapter introduction (in the student worktext) contains a link to the list corresponding to that chapter.
- The student books contain some **mixed review lessons**, and the curriculum also provides you with additional **cumulative review lessons**.
- There is a **chapter test** for each chapter of the curriculum, and a comprehensive end-of-year test.
- The **worksheet maker** allows you to make additional worksheets for most calculation-type topics in the curriculum. This is a single html file. You will need Internet access to be able to use it.
- You can use the free online exercises at https://www.mathmammoth.com/practice/ This is an expanding section of the site, so check often to see what new topics we are adding to it!
- Some grade levels have cut-outs to make fraction manipulatives or geometric solids.
- And of course there are answer keys to everything.

How to get started

Have ready the first lesson from the student worktext. Go over the first teaching part (within the blue boxes) together with your student. Go through a few of the first exercises together, and then assign some problems for your student to do on their own.

Repeat this if the lesson has other blue teaching boxes. Naturally, you can also use the videos at https://www.mathmammoth.com/videos/

Many students can eventually study the lessons completely on their own — the curriculum becomes self-teaching. However, students definitely vary in how much they need someone to be there to actually teach them.

Pacing the curriculum

Each chapter introduction contains a suggested pacing guide for that chapter. You will see a summary on the right. (This summary does not include time for optional tests.)

Most lessons are 3 or 5 pages long, intended for one day. Some 5-page lessons can take two days. There are also a few optional lessons.

It can also be helpful to calculate a general guideline as to how many pages per week the student should cover in order to go through the curriculum in one school year.

Worktext 7-A			Worktext 7-B		
Chapter 1	8 days		Chapter 6	17 days	
Chapter 2	13 days	Chapter 7		12 days	
Chapter 3	9 days	Chapter 8 23		23 days	
Chapter 4	16 days	Chapter 9		10 days	
Chapter 5	16 days	Chapter 10		12 days	
TOTAL	62 days		TOTAL	74 days	

The table below lists how many pages there are for the

student to finish in this particular grade level, and gives you a guideline for how many pages per day to finish, assuming a 180-day (36-week) school year. The page count in the table below *includes* the optional lessons.

-						
Grade level	School days	Days for tests and reviews	Lesson pages	Days for the student book	Pages to study per day	Pages to study per week
7-A	81	9	197	72	2.74	13.7
7-B	99	10	244	89	2.74	13.7
Grade 7 total	180	19	441	161	2.73	13.7

Example:

The table below is for you to use.

Grade level	School days	Days for tests and reviews	Lesson pages	Days for the student book	Pages to study per day	Pages to study per week
7-A			197			
7-B			244			
Grade 7 total			441			

Let's say you determine that your student needs to study about 2.5 pages a day, or 12-13 pages a week on average in order to finish the curriculum in a year. As the student studies each lesson, keep in mind that sometimes most of the page might be reserved for workspace to solve equations or other problems. You might be able to cover more than the average number of pages on such a day. Some other day you might assign the student only one page of word problems.

Now, something important. Whenever the curriculum has lots of similar practice problems (a large set of problems), feel free to **only assign 1/2 or 2/3 of those problems**. If your student gets it with less amount of exercises, then that is perfect! If not, you can always assign the rest of the problems for some other day. In fact, you could even use these unassigned problems the next week or next month for some additional review.

In general, seventh graders might spend 45-90 minutes a day on math. If your student finds math enjoyable, they can of course spend more time with it! However, it is not good to drag out the lessons on a regular basis, because that can then affect the student's attitude towards math.

Working space, the usage of additional paper and mental math

The curriculum generally includes working space directly on the page for students to work out the problems. However, feel free to let your students to use extra paper when necessary. They can use it, not only for the "long" algorithms (where you line up numbers to add, subtract, multiply, and divide), but also to draw diagrams and pictures to help organize their thoughts. Some students won't need the additional space (and may resist the thought of extra paper), while some will benefit from it. Use your discretion.

Some exercises don't have any working space, but just an empty line for the answer (e.g. $200 + ___ = 1,000$). Typically, I have intended that such exercises to be done using MENTAL MATH.

However, there are some students who struggle with mental math (often this is because of not having studied and used it in the past). As always, the teacher has the final say (not me!) as to how to approach the exercises and how to use the curriculum. We do want to prevent extreme frustration (to the point of tears). The goal is always to provide SOME challenge, but not too much, and to let students experience success enough so that they can continue enjoying learning math.

Students struggling with mental math will probably benefit from studying the basic principles of mental calculations from the earlier levels of Math Mammoth curriculum. To do so, look for lessons that list mental math strategies. They are taught in the chapters about addition, subtraction, place value, multiplication, and division. My article at https://www.mathmammoth.com/lessons/practical_tips_mental_math also gives you a summary of some of those principles.

Using tests

For each chapter, there is a **chapter test**, which can be administered right after studying the chapter. **The tests are optional.** Some families might prefer not to give tests at all. The main reason for the tests is for diagnostic purposes, and for record keeping. These tests are not aligned or matched to any standards.

The end-of-year test is best administered as a diagnostic or assessment test, which will tell you how well the student remembers and has mastered the mathematics content of the entire grade level.

Using cumulative reviews and the worksheet maker

The student books contain mixed review lessons which review concepts from earlier chapters. The curriculum also comes with additional cumulative review lessons, which are just like the mixed review lessons in the student books, with a mix of problems covering various topics. These are found in their own folder in the digital version, and in the Tests & Cumulative Reviews book in the print version.

The cumulative reviews are optional; use them as needed. They are named indicating which chapters of the main curriculum the problems in the review come from. For example, "Cumulative Review, Chapter 4" includes problems that cover topics from chapters 1-4.

Both the mixed and cumulative reviews allow you to spot areas that the student has not grasped well or has **Sample Workshiedstrom**pic or concept, you have several options:

https://www.mathmammoth.com

- 1. Check if the worksheet maker lets you make worksheets for that topic.
- 2. Check for any online games and resources in the Introduction part of the particular chapter in which this topic or concept was taught.
- 3. If you have the digital version, you could simply reprint the lesson from the student worktext, and have the student restudy that.
- 4. Perhaps you only assigned 1/2 or 2/3 of the exercise sets in the student book at first, and can now use the remaining exercises.
- 5. Check if our online practice area at https://www.mathmammoth.com/practice/ has something for that topic.
- 6. Khan Academy has free online exercises, articles, and videos for most any math topic imaginable.

Concerning challenging word problems and puzzles

While this is not absolutely necessary, I heartily recommend supplementing Math Mammoth with challenging word problems and puzzles. You could do that once a month, for example, or more often if the student enjoys it.

The goal of challenging story problems and puzzles is to **develop the student's logical and abstract thinking and mental discipline**. I recommend starting these in fourth grade, at the latest. Then, students are able to read the problems on their own and have developed mathematical knowledge in many different areas. Of course I am not discouraging students from doing such in earlier grades, either.

Math Mammoth curriculum contains lots of word problems, and they are usually multi-step problems. Several of the lessons utilize a bar model for solving problems. Even so, the problems I have created are usually tied to a specific concept or concepts. I feel students can benefit from solving problems and puzzles that require them to think "out of the box" or are just different from the ones I have written.

I recommend you use the free Math Stars problem-solving newsletters as one of the main resources for puzzles and challenging problems:

Math Stars Problem Solving Newsletter (grades 1-8) https://www.homeschoolmath.net/teaching/math-stars.php

I have also compiled a list of other resources for problem solving practice, which you can access at this link:

https://l.mathmammoth.com/challengingproblems

Another idea: you can find puzzles online by searching for "brain puzzles for kids," "logic puzzles for kids" or "brain teasers for kids."

Frequently asked questions and contacting us

If you have more questions, please first check the FAQ at https://www.mathmammoth.com/faq-lightblue

If the FAQ does not cover your question, you can then contact us using the contact form at the Math Mammoth.com website.

Chapter 1: The Language of Algebra Introduction

In the first chapter of *Math Mammoth Grade* 7 we both review basic algebra topics from sixth grade and also go deeper into them, plus study the basic properties of the four operations. Since a good part of this chapter is review, it serves as a gentle introduction to 7th grade math, laying a foundation for the rest of the year. For example, when we study integers in the next chapter, students will once again simplify expressions, just with negative numbers. When we study equations in chapters 3 and 5, and also in subsequent grade levels, students will use the skills from this chapter (such as simplifying expressions, using the distributive property) in solving equations.

The main topics are the order of operations, writing and simplifying expressions, and the properties of the four operations, including the distributive property. Students have studied most of these in 6th grade. The main principles are explained and practiced both with visual models and in abstract form, and the lessons contain varying practice problems that approach the concepts from various angles.

Please note that it is not recommended to assign all the exercises by default. Use your judgment, and strive to vary the number of assigned exercises according to the student's needs. See the user guide at the beginning of this book or at https://www.mathmammoth.com/userguides/ for some further thoughts on using and pacing the curriculum.

You can find matching videos for topics in this chapter at https://www.mathmammoth.com/videos/ (choose grade 7).

Good Mathematical Practices

• The student is embarking on a wonderful journey into algebra — learning to do arithmetic with letters. The familiar properties of the four operations still hold, just like they do with numbers. Algebra is such a wonderful tool because it allows us to abstract a given situation and represent it symbolically, and then manipulate the representing symbols as if they have a life of their own. It is the foundational tool that allows us to model real-world situations with mathematics.

Pacing Suggestion for Chapter 1

This table does not include the chapter test as it is found in a different book (or file). Please add one day to the pacing for the test if you use it.

The Lessons in Chapter 1	page	span	suggested pacing	your pacing
Exponents and the Order of Operations	13	4 pages	1 day	
Expressions and Equations	17	3 pages	1 day	
Properties of the Four Operations	20	4 pages	1 day	
Simplifying Expressions	24	4 pages	1 day	
Growing Patterns 1	28	3 pages	1 day	
The Distributive Property	31	5 pages	2 days	
Chapter 1 Review	36	2 pages	1 day	
Chapter 1 Test (optional)				
TOTALS	5	25 pages	8 days	

Games at Math Mammoth Online Practice

Hexingo Game — Order of Operations

Practice the order of operations with the four basic operations, parentheses, and exponents. https://www.mathmammoth.com/practice/order-operations#num=3&operations=add,sub,mult,div,exponents,parens

Expression Exchange

This online activity includes THREE separate work areas where you can explore how simple algebraic expressions work, and then one game. In the work areas, you can learn how to add and subtract simple algebraic terms in order to form an expression. In the game, you will go through practice exercises, forming the asked expressions from parts.

https://www.mathmammoth.com/practice/expression-exchange

Helpful Resources on the Internet

We have compiled a list of Internet resources that match the topics in this chapter, including pages that offer:

- online practice for concepts;
- online **games**, or occasionally, printable games;
- animations and interactive illustrations of math concepts;
- articles that teach a math concept.

We heartily recommend you take a look! Many of our customers love using these resources to supplement the bookwork. You can use these resources as you see fit for extra practice, to illustrate a concept better and even just for some fun. Enjoy!





Exponents and the Order of Operations

Let's review! Exponen repeated multiplication	ts are a shorthand for writing as by the same number.		exponent			
For example, $0.9 \cdot 0.9$	$\cdot 0.9 \cdot 0.9 \cdot 0.9$ is written 0.9^5 .		$\underbrace{12^{4}}_{=20,736} = 12 \times 12 \times 12 \times 12 \times 12$			
	r is called the exponent . mes the base number is multip	lied by itself.	= 20,736			
The expression 2^5 is re	ad as "two to the fifth power,"	' "two to the fifth,"	or "two raised to the fifth power."			
Similarly, 0.7 ⁸ is read a	as "seven tenths to the eighth j	power" or "zero po	int seven to the eighth."			
The "powers of 6" are and 6^{99} are powers of 6		raised to some po	wer: for example, 6^3 , 6^4 , 6^{45} ,			
	xponent 2 are usually read as s t is because it gives us the <u>area</u>		ed." For example, 11 ² is read as ides 11 units long.			
	ent is 3, the expression is usua cubed" because it is the volur		word " cubed. " For example, 1.5^3 is in edge 1.5 units long.			
1. Evaluate.						
a. 4^3	b. 10 ⁵		c. 0.1^2			
d. 0.2^3	e. 1 ¹⁰⁰		f. 100 cubed			
2. Write these expression	ns using exponents. Find their	values.				
a. $0 \cdot 0 \cdot 0 \cdot 0 \cdot 0$		b. 0.9 · 0.9				
$\mathbf{c.} \ 5 \cdot 5 \cdot 5 \ + \ 2 \cdot 2 \cdot$	$2 \cdot 2 \cdot 2$					
d. $6 \cdot 10 \cdot 10 \cdot 10 \cdot 10$	$0 \cdot 10 \cdot 10 - 9 \cdot 10 \cdot 10 \cdot 10 \cdot$	10				
The expression (5	m) ^{3} means that we multiply 5	meters by itself th	ree times:			
	$(5 \text{ m})^3 = 5 \text{ m} \cdot 5 \text{ m} = 125 \text{ m}^3$					
	is different from 5 m ³ . The lat 3) applies only to the unit "m"		eses, so the			
3. Find the value of the e	expressions. Include the prope	r unit.				
a. $(2 \text{ cm})^3$	b. $(11 \text{ ft})^2$	c. $(1.2 \text{ km})^2$	d. $(6 \text{ in})^2$			
. Match each of (a) and	(b) with one expression on the	e right.				
a. The volume of a cu	ube with edges 2 cm long.		2 2			
b. The volume of a cuample workshee	ube with edges 8 cm long. et from	(i)	8 cm^3 (ii) $(8 \text{ cm})^3$ (iii) 512 cm			

13

https://www.mathmammoth.com

 <u>The Order of Operations — PE[MD][AS]</u> 1) Solve what is within parentheses (P). 2) Solve exponents (E). 	Example 1 . In $15 - 2 + 3 \cdot 3$, we do $3 \cdot 3$ first, then the subtraction, and lastly the addition.
 3) Solve the multiplicative operations — this includes both multiplications (M) and divisions (D) — from left to right. 4) Solve the additive operations — this includes both additions (A) and subtractions (S) — from left to right. 	You can remember PEMDAS with the silly mnemonic <i>Please Excuse My Dear Aunt Sally.</i> Or make up your own!

5. Find the value of each expression.

a. $120 - (9 - 4)^2$	c. $4 \cdot 5^2$	e. $10 \cdot 2^3 \cdot 5^2$
b. $120 - 9 - 4^2$	d. $(4 \cdot 5)^2$	f. $10 + 2^3 \cdot 5^2$
g. $(0.2+0.3)^2 \cdot (5-5)^4$	h. $0.7 \cdot (1 - 0.3)^2$	i. $20 + (2 \cdot 6 + 3)^2$

Example 2. Simplify $(10 - (5 - 2))^2$.	Example 3. Simplify $2 + \frac{1+5}{40-6^2}$.
Here we have double parentheses. First calculate what is within the <i>inner</i> parentheses: $5 - 2 = 3$. Then the expression becomes $(10 - 3)^2$.	The fraction line works just like parentheses, as a grouping symbol, grouping both what is above the line and also what is below it. Therefore, first solve what is in the numerator and in the denominator (in either order).
The rest is easy: $(10-3)^2 = 7^2 = 49.$	$2 + \frac{1+5}{40-6^2} = 2 + \frac{6}{4} = 2 + \frac{2}{3} = \frac{8}{3}$

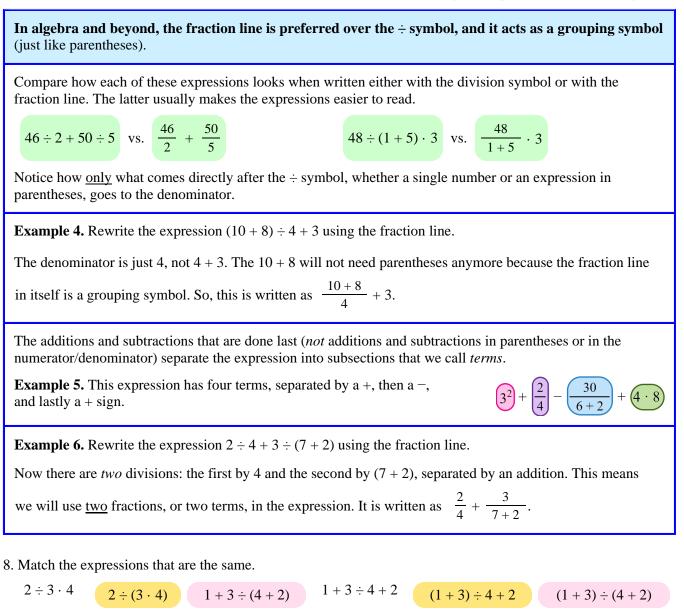
6. Find the value of each expression.

a. $(12 - (9 - 4)) \cdot 5$	b. $12 - (9 - (4 + 2))$	c. $(10 - (8 - 5))^2$	d. $3 \cdot (2 - (1 - 0.4))$

7. Find the value of each expression.

a. $\frac{4\cdot 5}{2} \cdot \frac{9}{3}$	b. $\frac{4 \cdot 5}{2} + \frac{9}{3}$	c. $\frac{4+5}{2} + \frac{9}{3-1}$
Sample worksheet from		

https://www.mathmammoth.com



 $1 + \frac{3}{4} + 2$ $\frac{1+3}{4+2}$ $\frac{2}{3} \cdot 4$ $\frac{2}{3 \cdot 4}$ $\frac{1+3}{4} + 2$ $1 + \frac{3}{4+2}$

9. Rewrite each expression using the fraction line and then find its value.

a. 56 ÷ 7 + 6	b. $7 \div (2+6)$	c. $16 \div (2+6) - 2$	d. $4 \div 5 - 1 \div 3$
Sample workshee	t from		
https://www.mathi	mammoth.com		

To evaluate an expression means to find (calculate) its value.

Example 7. Evaluate the expression $x^2 - \frac{2+y}{y}$ when x is 10 and y is 3.

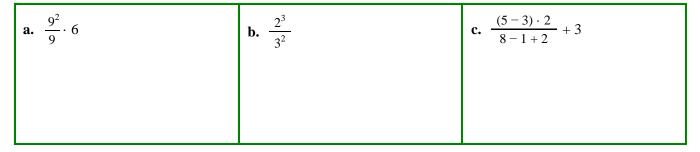
This means we substitute 10 for x and 3 for y in the expression and then calculate its value according to the order of operations:

$$x^{2} - \frac{2+y}{y} = 10^{2} - \frac{2+3}{3} = 100 - \frac{5}{3} = 98 \frac{1}{3}$$

However, in algebra and beyond, it is customary to *not* give answers as mixed numbers but as fractions, to avoid confusion. After all, 98 1/3 could easily be mistaken for 981/3. So let's go back to the expression 100 - (5/3) and simplify it so it becomes a fraction:

$$100 - \frac{5}{3} = \frac{300}{3} - \frac{5}{3} = \frac{295}{3}$$
 (This is the final value as a fraction.)

10. Find the value of these expressions. (When applicable, give your answer as a fraction, not as a decimal.)



11. Evaluate the expressions. (When applicable, give your answer as a fraction, not as a decimal.)

a.
$$2x^2 - x$$
, when $x = 4$
b. $\frac{3s}{5} - \frac{2t}{5}$, when $s = 10$ and $t = 4$
c. $\frac{x^2}{x+1}$, when $x = 3$
d. $\frac{a+b}{b} + 2$, when $a = 1$ and $b = 3$

12. Why is it wrong to write the expression $2 + 5 \cdot 2 \div 4$ as $\frac{2 + 5 \cdot 2}{4}$?

Expressions and Equations

Expressions in mathematics consist of:

- numbers;
- mathematical operations $(+, -, \cdot, \div, +)$;
- and letter variables, such as *x*, *y*, *a*, T, and so on.

Note: Expressions do not have an "equals" sign!

Examples of expressions: 5 $\frac{xy^4}{2}$ T - 5 + $\frac{x}{7}$

What do we do with expressions?

We can find the *value* of an expression (*evaluate* it). If the expression contains variables, we cannot find its value unless we know the value of the variables.

For example, to find the value of the expression 2x when x is 6/7, we simply substitute 6/7 in place of x. We get $2x = 2 \cdot (6/7) = 12/7$.

<u>Note:</u> When we write $2x = 2 \cdot (6/7) = 12/7$, the equals sign is *not* signaling an equation to solve. (In fact, we already know the value of *x*!) It is simply used to show that the value of the expression 2x here is the same as the value of $2 \cdot (6/7)$, which is in turn the same as 12/7.

1. This is a review. Write an expression.

- **a.** 2x minus the sum of 40 and x.
- **b.** The quantity 3 times *x*, cubed.
- c. s decreased by 6
- **d.** five times *b* to the fifth power
- **e.** seven times the quantity x minus y
- f. the difference of t squared and s squared
- **g.** x less than 2 cubed
- **h.** the quotient of 5 and *y* squared
- i. 2 less than x to the fifth power
- j. x cubed times y squared
- **k.** the quantity 2x plus 1 to the fourth power

Sample worksheet from https://www.mathmammoth.com

An equation has two expressions separated by an equals sign: (expression 1) = (expression 2)

Examples: 0 = 0 2(a-6) = b

$9 = -8 \qquad \frac{x+3}{2} = 1.5$ (a false equation)

What do we do with equations?

If the equation has a variable (or several) in it, we can try to *solve* the equation. This means we find the values of the variable(s) that make the equation <u>true</u>.

For example, we can solve the equation 0.5 + x = 1.1 for the unknown *x*.

The value 0.6 makes the equation true: 0.5 + 0.6 = 1.1. We say x = 0.6 is the **solution** or the **root** of the equation.

To read the expression 2(x + y), use the word *quantity*: "two times the quantity *x* plus *y*."

There are other ways, as well, just not as common:

"two times the sum of *x* and *y*," or "the product of 2 and the sum *x* plus *y*." (This page intentionally left blank.)

Integers

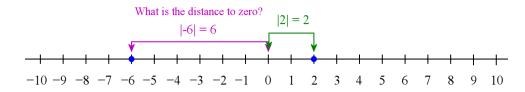
-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 1 2 3 4 5 6 7 8 9 10
The counting numbers are 1, 2, 3, 4, 5, and so on. They work for addition. But counting numbers do not allow us to perform all possible subtractions; for example, the answer to the problem $2 - 7$ is not any of them. That is when we come to the <i>negatives</i> of the counting numbers: -1 , -2 , -3 , -4 , -5 , and so on.
Together with zero, all these form the set of integers : $\{, -4, -3, -2, -1, 0, 1, 2, 3, 4,\}$. Note: Zero is neither positive nor negative.
Read -1 as "negative one" and -5 as "negative five." Some people read -5 as "minus five." That is very common, and it is not wrong, but be sure that you do not confuse it with subtraction.
Often, we need to put parentheses around negative numbers in order to avoid confusion with other symbols. Therefore, $^{-}5$, $^{-}5$, and $(^{-}5)$ all mean "negative five."
Which is more, $-30 \text{ or } -5^\circ$ Which is <i>warmer</i> , -30° C or -5° C? Clearly -5° C is. $-30 -20 -10 0 10 20 30$ Temperatures get colder and colder the more they move towards the negative numbers. We can write a comparison: -30° C $< -5^\circ$ C.
Similarly, we can write $-\$500 < -\200 to signify that to owe $\$500$ is a worse situation than to owe $\$200$.
Or, in elevation, $-15 \text{ m} > -50 \text{ m}$ means that 15 m below sea level is higher than 50 m below sea level.
1. Write comparisons using $>$, $<$, and integers. Don't forget to include the units!
a. The temperature at 5 AM was 12°C below zero. Now, at 9 AM, it is 8°C below zero.
b. I owe my mom \$12, and my sister owes her \$25.
c. The bottom of the Challenger Deep trench is 11,033 m below sea level.Mt. Everest reaches to a height of 8,848 m.
d. The total electric charge of five electrons is $-5e$. The total electric charge of 5 protons is $+5e$. (The symbol <i>e</i> means elementary charge, or a charge of a single proton.)
e. Dean has \$55, whereas Jack owes \$15.
2. Which integer is
a. 3 more than -7 b. 8 more than -3 c. 7 less than 2 d. 5 less than -11

3. Write the numbers in order from the least to the greatest.

a. -5 -56 51 -15

b. 3 0 -31 -13

The **absolute value** of a number is its distance to zero.



We denote the absolute value of a number by putting vertical bars on either side of it. So |-4| means "the absolute value of 4," which is 4. Similarly, |87| = 87. In an expression we treat the absolute value bars like parentheses and solve them first.

Example 1. Simplify |-4| - |1|. First simplify the absolute values. We get 4 - 1 = 3.

Let's say someone's account balance is -\$1,000. That person is in debt. The absolute value of the debt is written as |-\$1000| and means that the *size* of the debt is \$1,000.

If a diver is at a depth of -22 m, the absolute value |-22 m | tells us how far he is from the surface (22 m).

4. Simplify.

a. -11	b. +7	c. 0	d. -46
e. -5 + -2		f. -5 - 2	
g. -5 + -2 + 8		h. 5 + -2 - -1	

5. Answer, using the absolute value notation.

a. What is the distance between -153 and zero on a number line?

b. What is the distance between *x* and zero on a number line?

6. Interpret the absolute value in each situation.

a. A fishing net is at the depth of 15 feet. $|-15 \text{ ft}| = __ft$

Here, the absolute value shows _____

b. The temperature is -5° C. $|-5^{\circ}$ C |= _____°C

Here, the absolute value shows _____

c. Eric's balance is -\$7. |-\$7| = \$_____

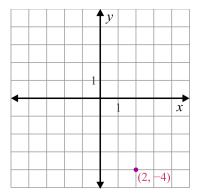
The absolute value shows _____

d. A point is drawn in the coordinate grid at (2, -4). |-4| =_____

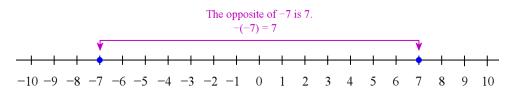
Here, the absolute value shows _____

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The **opposite** of a number is the number that is on the opposite side of zero at the same distance from zero.



We denote the opposite of a number using the minus sign. For example, the opposite of 4 is written as -4. The opposite of -2 is written as -(-2), which is of course 2. So, -(-2) = 2.

The opposite of zero is zero itself. In symbols, -0 = 0.

"But wait," you might ask, "doesn't -4 mean 'negative four,' not 'the opposite of four'?"

It can mean either! Sometimes the context will help you tell which is which. Other times it isn't necessary to differentiate, because, after all, the opposite of four is negative four, or -4 = -4.

In the expression -(4 + 5), the minus sign means the opposite of the sum 4 + 5, which equals negative nine.

Example 2. -|7| means the opposite of the absolute value of seven. It simplifies to -7.

Notice that there are *three* different meanings for the minus sign:

- 1. To indicate subtraction, as in 7-2.
- 2. To indicate negative numbers: "negative 7" is written -7.
- 3. To indicate the opposite of a number: -(n + 1) is the opposite of n + 1.

7. Write using symbols, and simplify if possible.

.

a. the opposite of 6	b. the opposite of -11
c. the opposite of the absolute value of 12	d. the absolute value of negative 12
e. the opposite of the sum $6 + 8$	f. the opposite of the difference $9 - 7$
g. the absolute value of the opposite of 8	h. the absolute value of the opposite of -2

8. Simplify.

b. -(-9) **c.** -|-7| **d.** -0 **e.** -(-(-100))**a.** -|8|

9. Write with symbols. Use a variable for "a number" or "a certain number".

a. The absolute value of a number is equal to 6.

b. The opposite of a certain number is less than negative 2.

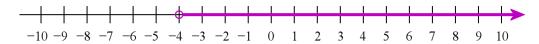
- c. The absolute value of a certain number is greater than 15.
- **d.** The opposite of *n* is equal to to the sum 56 + 5.

10. Daniel owed \$5. Then he borrowed \$10 more. Next, he paid off \$7 of his debts. Lastly Sample worksheet from 54. Write one integer to express Daniel's money situation now. https://www.mathmammoth.com

Remember **inequalities?** The number line below illustrates the inequality $x \ge -8$. Notice the arrow on the right, which shows that the ray continues to infinity. The closed circle denotes that -8 belongs to the solution set.

-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 1 2 3 4 5 6 7 8 9 10

The inequality x > -4 is plotted on the number line below. The open circle indicates that -4 is not part of the solution set.



11. Plot these inequalities on the number line. Don't forget the arrow on the open end.

-8 -7 -6 -5 -4 -3 -2 -1 0 1 2 3 4	-8 -7 -6 -5 -4 -3 -2 -1 0 1 2 3 4
a. $x < -3$	b. $x > -1$
-8 -7 -6 -5 -4 -3 -2 -1 0 1 2 3 4	-8 -7 -6 -5 -4 -3 -2 -1 0 1 2 3 4
c. $x \ge -2$	d. $x \le 2$

12. **a.** Solve the inequality x < 2 in the set $\{-3, -2, -1, 0, 1, 2, 3\}$.

b. Solve the inequality $x \ge -5$ in the set $\{-10, -8, -6, -2, -1, 0, 5\}$.

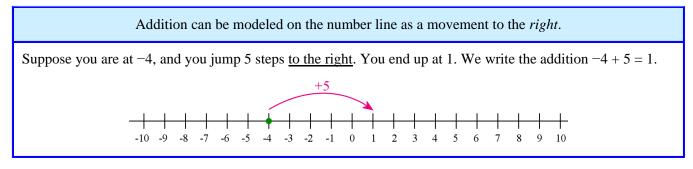
13. Write an inequality. Use negative integers where appropriate.

- **a.** The pit is at most 10 m deep.
- **b.** The pit is at least 12 m deep.
- **c.** Tim's debt is no more than \$500.
- **d.** Nora owes at least \$100.
- e. For the skiing contest to take place, the temperature has to be warmer than 15 degrees below zero.
- f. The freezer temperature should be colder than 10 degrees below zero.

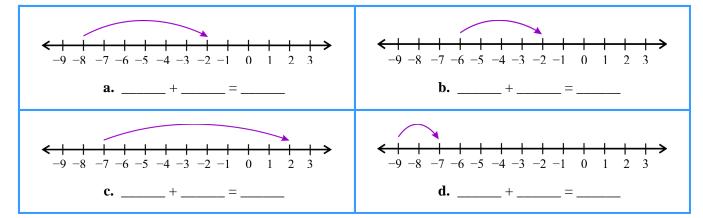


Let *a* and *b* be two negative integers, with b > a. What is the distance between them on the number line? Write an expression.

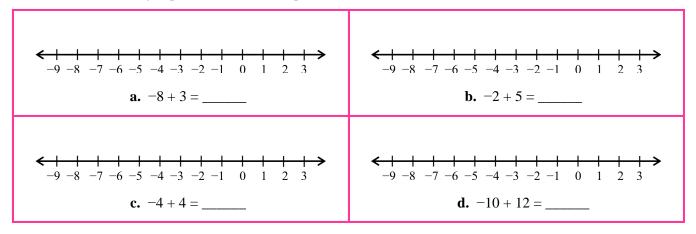
Addition and Subtraction on the Number Line 1



1. Write an addition equation to match each number line jump.



2. Draw a number line jump for each addition equation and solve.



3. What about adding more than one number? How could these additions be illustrated by number line jumps?

a.
$$-4+2+3$$

 $-11-10-9-8-7-6-5-4-3-2-1$ 0 1 2 3 4 5

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Solving Equations

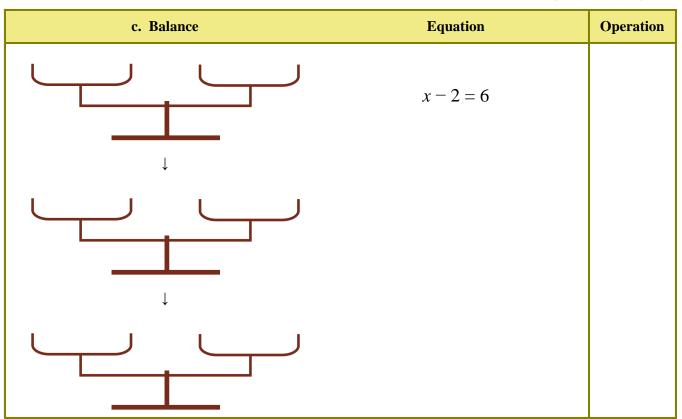
	(expression) =	= (expression)			
To solve an equation, we can					
 add the same quantity to be subtract the same quantity		· ·	both sides by the same th sides by the same nu		
Notice that in any of these operati remain equal, even though the exp	· ·		right sides of the equa	tion will	
Example 1. We will manipulate t the operation that is going to be d		3 = 5 in these fo	ur ways. We will write	in the m	nargi
Let's add six to both sides.			2+3 =	5	+ 6
Now, both sides equal 11. Next,	we multiply both sides	by 8.	2 + 3 + 6 =	11	· 8
Now, both sides equal 88. Next,	we subtract 12 from bo	oth sides.	16 + 24 + 48 =	88	- 1
Now both sides equal 76. Next, v	ve divide both sides by	2.	16 + 24 + 48 - 12 =	76	÷ 2
Now both sides equal 38.			8 + 12 + 24 - 6 =	38	
Your goal is to isolate the unknow We can model an equation with a hem, thus the sides are balanced	vn, or leave it by itself pan balance . Both sid (not tipped to either sid	, on one side. Th	en the equation is solve	ed.	
Your goal is to isolate the unknow We can model an equation with a them, thus the sides are balanced Example 2. Solve the equation $x = \frac{1}{2}$	wn, or leave it by itself pan balance . Both sid (not tipped to either sid -2 = 3.	f, on one side. Th les (pans) of the b le).	en the equation is solve palance will have an <i>eq</i>	ed. <i>ual</i> weig	ht ir
Of course, you do not usually won Your goal is to isolate the unknow We can model an equation with a them, thus the sides are balanced Example 2. Solve the equation $x +$ We can write this equation as $x +$ Here x is accompanied by	wn, or leave it by itself pan balance . Both sid (not tipped to either sid -2 = 3. (-2) = 3 and model it the	c, on one side. Th les (pans) of the b le). using negative an	en the equation is solve palance will have an <i>eq</i>	ed. <i>ual</i> weig he balan	ht in ce.
Your goal is to isolate the unknow We can model an equation with a them, thus the sides are balanced Example 2. Solve the equation $x +$ We can write this equation as $x +$	wn, or leave it by itself pan balance . Both sid (not tipped to either sid -2 = 3.	f, on one side. Th les (pans) of the b le).	en the equation is solve palance will have an <i>eq</i>	ed. <i>ual</i> weig he balan m	ht in ce.
Your goal is to isolate the unknow We can model an equation with a them, thus the sides are balanced Example 2. Solve the equation $x +$ We can write this equation as $x +$ Here x is accompanied by two negatives on the left side. Adding two <u>positives</u> to both sides will cancel those two negatives. We denote that by	wn, or leave it by itself pan balance . Both sid (not tipped to either sid -2 = 3. (-2) = 3 and model it the	c, on one side. Th les (pans) of the b le). using negative an	en the equation is solve balance will have an <i>eq</i> d positive counters in t x + (-2) = 3	ed. <i>ual</i> weig he balan m	,ht in ce. argin

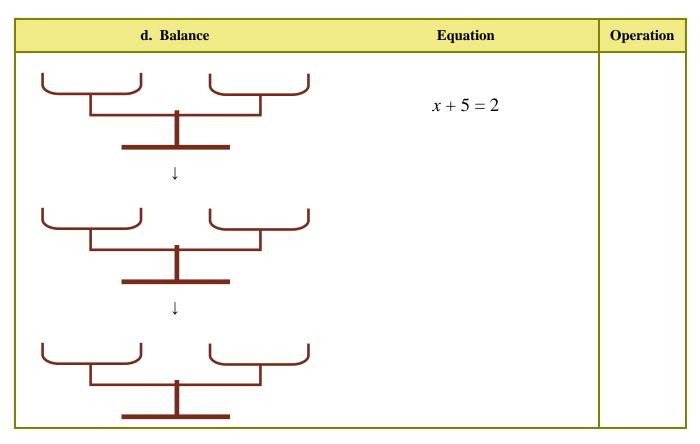
a. Balance	Equation	Operation to do to both sides
	x + 1 = -4	

1. Solve the equations	Write in the margin	what operation	you do to both sides.
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b. Balance	Equation	Operation to do to both sides
	x - 1 = -3	
Sample worksheet from		

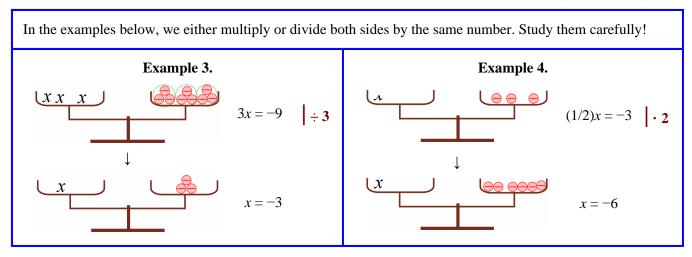
d. x + 5 = -4



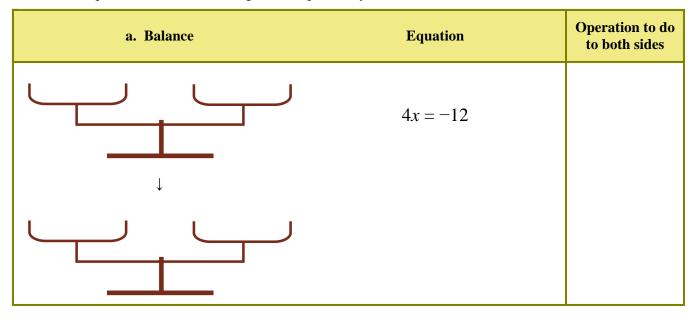


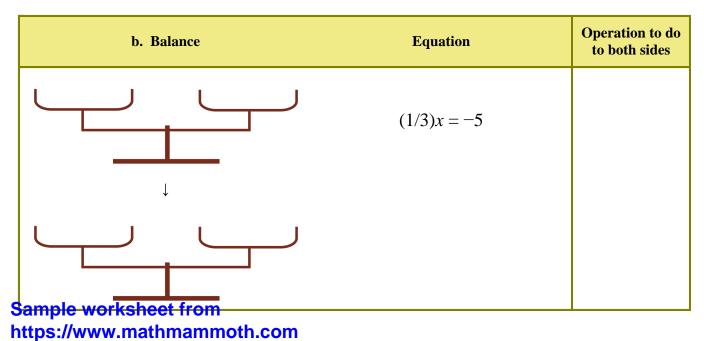
2. If you need more practice, solve the following equations also. Draw a balance in your notebook to help you.

Sample worksheet from b. x + (-3) = -4**c.** x + 6 = -1**https://www.mathmammoth.com**

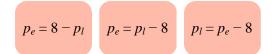


3. Solve the equations. Write in the margin what operation you do to both sides.





- 4. Let's review a little! Which equation matches the situation?
 - **a.** A stuffed lion costs \$8 less than a stuffed elephant. Note: p_l signifies the price of the lion and p_e the price of the elephant.



b. A shirt is discounted by 1/5 of its price, and now it costs \$16.

$$p - 1/5 = \$16$$
 $\frac{4p}{5} = \$16$ $\frac{p}{5} = \$16$ $p - p/5 = \$16$ $\frac{5p}{4} = \$16$

5. Find the roots of the equation $\frac{6}{x+1} = -3$ in the set $\{2, -2, 3, -3, 4, -4\}$.

6. Write an equation, then solve it using guess and check. Each root is between -20 and 20.

a. 7 less than x equals 5.
b. 5 minus 8 equals x plus 1
c. The quantity x minus 1 divided by 2 is equal to 4.
d. x cubed equals 8
u. <i>x</i> cubed equals 8
e. -3 is equal to the quotient of 15 and y
f. Five times the quantity x plus 1 equals 10.
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Chapter 3 Mixed Review

1. Write an expression.

a. 10 less than *x* squared.

(Expressions and Equations/Ch1)

b. The quotient of 154 and *k* cubed.

c. The quantity *x* plus 2 to the fifth power.

d. *x* plus 2 to the fifth power.

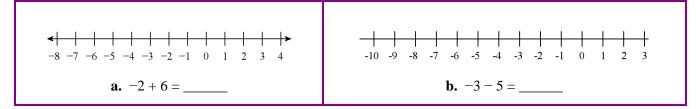
2. The sides of a square are (x + 2) long. (Simplifying Expressions/Ch1)

- a. Sketch the square.
- **b.** Write an expression for the area of the square.

c. Write an expression for the perimeter of the square.

d. Evaluate your expression for the area of the square when x = 1.5.

3. Draw a number line jump for each addition or subtraction. (Addition and Subtraction on the Number Line 1/Ch2)



4. Draw counters for the addition 3 + (-5). Explain how to perform the addition using the counters. (More Addition of Integers/Ch2)

5. Solve. (More Addition of Integers/Ch2)

a. 89 + (-35) =	b. -45 + (-29) =	c. $-78 + 60 =$
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6. Change each addition into a subtraction or vice versa. Then solve whichever is easier. (Subtraction of Integers/Ch2)

a. -2 + (-18)	b. 56 – (–34)	c. -14 + (-24)	d. 2 + 9
\downarrow	\downarrow	\downarrow	\downarrow
Sample worksheet f	+=	==	==

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- 7. Write comparisons using >, <, and integers. Include the units, too. (Integers/Ch2)
 - **a.** The temperature at the North Pole is -34 degrees Celsius, whereas in New York, it is -8 degrees Celsius.
 - **b.** The total electric charge of 12 electrons is -12e. The total electric charge of 3 protons is +3e.
- 8. Name the property of arithmetic illustrated by the equation $2x = x \cdot 2$. (Properties of the Four Operations/Ch1)
- 9. Evaluate the expression |a b| for the given values of *a* and *b*. Check that the answer you get is the same as if you had used a number line to figure out the distance between the two numbers. (Distance Between Numbers/Ch2)

a. <i>a</i> is 8 and <i>b</i> is 54	b. a is -12 and b is -5

- 10. Describe a situation where one person has a positive account balance and (Integers/Ch2) another has a negative balance, and the one person's balance is \$30 more.
- 11. Use the distributive property "backwards" to write the expression as a product. (The Distributive Property/Ch1)

a. $42s + 28 = (_ + _)$ **b.** $54z - 18 = (_ - _)$

12. Find the missing numbers. (Various lessons/Ch2)

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a. \div (-5) = 35	b. $35 \div ___= -5$	c. $5 \cdot ___ = -35$
d. $2 + (-5) = _$ + 7	e. $2 \cdot 9 = -3 \cdot$	f. $40 \div ___= -5 \cdot 4$

13. Write the equation and then solve it using "guess and check." Each root is between -20 and 20. (Expressions and Equations/Ch1)

a. 2 plus 14 equals x minus 1
b. x cubed equals 27
Sample worksheet from

14. Add or subtract. (Various lessons/Ch2)

a. (-9) + (-18) =	b. $-21 - (-3) = $	c. $17 - 51 =$
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15. Give a real-life situation for the sum 3 + (-10). (Various lessons/Ch2)

16. Simplify. (Integers/Ch2)

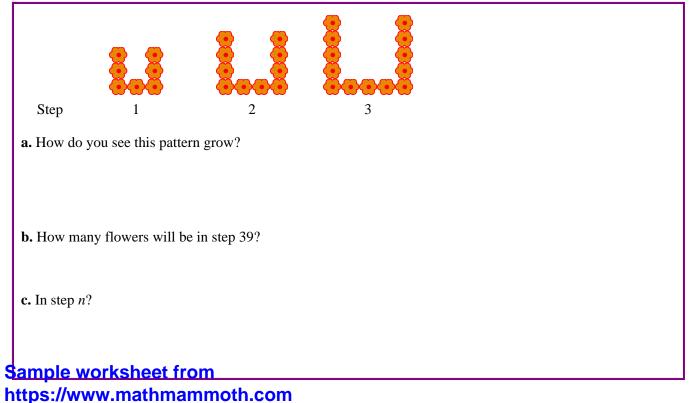
a. |-2| **b.** -(-2) **c.** -|2| **d.** -0

17. Find the value of the expressions when x = -2 and y = 8. (Multiplying Integers 2/Ch2)

a. $5x^2$	b. $-5y + 6$	c. $-(y + x)$

 Jeremy is 2 years older than Larry. Write an expression for Larry's age, if Jeremy is y years old. (Expressions and Equations/Ch1)

19. Here is a growing pattern. Draw the steps 4 and 5 and answer the questions. (Growing Patterns 1/Ch1)



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Rational Numbers

If you can write a number as a *ratio of two integers*, it is a **rational number**. For example, 4.3 is a rational number because we can write it as the ratio $\frac{43}{10}$ or 43:10. Note: To represent rational numbers, we usually indicate the ratio with a fraction line rather than a colon. **Examples of rational numbers** Since -10 can be written as $\frac{-10}{1}$, it is a rational number. It can also be written as $\frac{10}{-1}$. Since 0.1 can be written as $\frac{10}{10}$, it is a rational number. Since 3.24 can be written as $\frac{324}{100}$, it, too, is a rational number. **Negative fractions** The ratio of the integers 7 and -10 gives us the fraction $\frac{7}{-10}$. As we studied earlier, we usually write this as $-\frac{7}{10}$ and read it as "negative seven tenths." **Obviously, all fractions, whether negative or positive, are rational numbers.**

Negative fractions give us negative decimals.

For example, $-\frac{8}{10}$ is written as a decimal as -0.8, and $-5\frac{21}{100} = -5.21$.

You can write a rational number as a ratio of two integers in many ways.

For example, the decimal -1.4 can be written as a ratio of two integers in all these ways (and more!):

$$-1.4 = \frac{-14}{10} = \frac{-28}{20} = \frac{28}{-20} = \frac{42}{-30} = \frac{-42}{30} = \frac{-7}{5}$$

So -1.4 is *definitely* a rational number! \bigcirc But the same holds true for all rational numbers—you can always write them as a ratio of two integers in multitudes of ways.

1. Write these numbers as a ratio (fraction) of two integers.

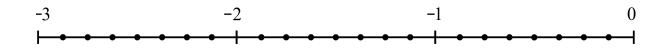
a. 6	b. -100	c. 0	d. 0.21
e. –1.9	f. –5.4	g. –0.56	h. 0.022

2. Are all percents, such as 34% or 5%, rational numbers? Justify your answer.

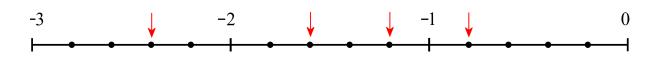
3. Form a fraction from the two given integers. Then convert it into a decimal.

a. 8 and 5	b. -4 and 10	c. 89 and -100
d. –5 and 2	e. 91 and –1000	f. −1 and −4

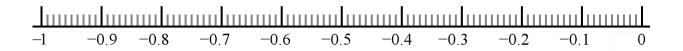
4. Mark the fractions and mixed numbers on the number line below: $-\frac{1}{2}$, $-\frac{7}{8}$, $-1\frac{5}{8}$, $-\frac{9}{4}$, $-2\frac{3}{4}$



5. Write the fractions marked by the arrows.



6. Mark the decimals on the number line: -0.11, -0.58, -0.72, -0.04



7. Sketch a number line from -3 to 0, with tick marks at every tenth. Then mark the following numbers on your number line: -0.2, -1.5, -2.8, -3/5, and -5/2.

8. Write these rational numbers as ratios of two integers (fractions) in a lot of different ways.

a.
$$-2 = -\frac{2}{1} =$$

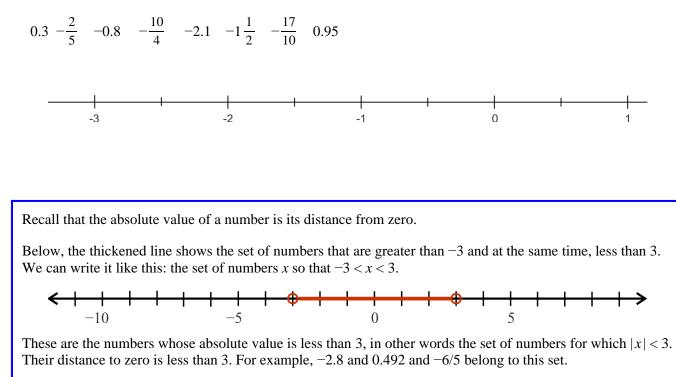
b. $0.6 = \frac{6}{10} =$

9. Compare, writing $\langle or \rangle$ in between the numbers.

10. Order these rational numbers in order, from the smallest to the greatest.

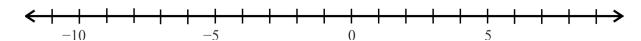
$$2.1 \quad -\frac{1}{8} \quad -1 \quad -\frac{7}{3} \quad -2.01 \quad 1 \quad \frac{1}{3} \quad -0.5$$

11. Mark the decimals *and* the fractions on the number line, approximately.



Note that 3 and -3 are not part of this set; that is why we use an open circle at 3 and -3.

12. **a.** Show on the number line the set of numbers *x* for which |x| < 1.5



b. List three rational numbers in that set that are not integers.

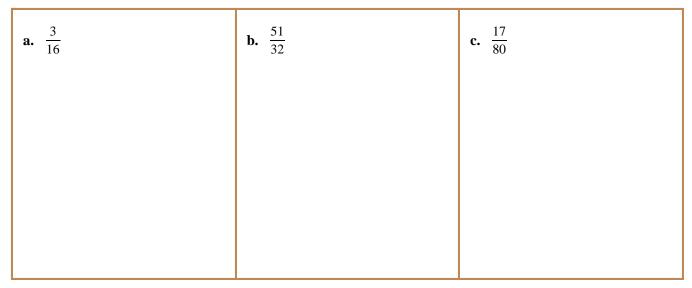
13. List three rational numbers *r* so that |r| < 2 and r > -1.

Repeating Decimals

As you already know, sometimes it is easy to write a fraction as a decimal. For example, 3/10 = 0.3 and 1/4 = 0.25. However, if you don't know of any other way to to find the decimal equivalent of a fraction, the technique that works all the time is to **treat the fraction as a division** and divide.

Example 1. Write $\frac{31}{40}$ as a decimal.	$\begin{array}{r} 0 \ 0.7 \ 7 \ 5 \\ 40 \ 3 \ 1.0 \ 0 \ 0 \ 0 \end{array}$
We will use long division. Note how we add many decimal zeros to the dividend (31) so that we can continue the division into the decimal digits.	$\frac{-280}{300}$
This division terminates (comes out even) after just three decimal digits.	$\frac{-280}{200}$
We get $\frac{31}{40} = 0.775$. This is a terminating decimal .	$\frac{-200}{0}$

1. Write as decimals, using long division. Continue the division until it terminates.



2. Use long division to write these fractions as decimals. Continue the division to at least 6 decimal digits. Notice what happens!

a. $\frac{2}{3}$	b. $\frac{7}{11}$	c. $\frac{8}{9}$
Sample worksheet from		

Example 2. Write $\frac{18}{11}$ as a decimal.	$\begin{array}{r} 0 \ 1.6 \ 3 \ 6 \ 3 \\ 11 \ \overline{) 1 \ 8.0 \ 0 \ 0 \ 0} \end{array}$
We write 18 as 18.0000 in the long division "corner" and divide by 11. Notice how the digits "63" in the quotient and the remainders 40 and 70 start repeating.	<u>-1 1</u> 7 0 <u>- 6 6</u>
So $\frac{18}{11} = 1.636363$. We can use an ellipsis (three dots, or "") to indicate	$\frac{-66}{40}$
that the decimal is non-terminating. A better notation is to draw a bar (a line) over the digits that repeat: $1.636363 = 1.\overline{63}$.	7 0 <u>- 6 6</u> 4 0
This number is called a repeating decimal because the digits "63" repeat forever!	$\frac{-33}{7}$

The decimal form of ANY rational number is either a terminating decimal or a repeating decimal.

This is an important fact. It says that when you write any fraction as a decimal, there are only two possibilities: either the decimal terminates or it repeats.

The converse is also true: if a decimal terminates or is a repeating decimal, it *can* be written as a fraction, thus is a rational number.

Example 3. The repeating decimal 1.9051050505... is written as $1.9051\overline{05}$. Notice that the bar marks only the digits that repeat ("05"). The digits "9051" that don't repeat are not included under the bar. (If you're curious, as a fraction, this number is 1,886,054/990,000.)

The repeating part is the digits "384615". So, $5/13 = 0.\overline{384615}$.

Example 5. The decimal 0.095 is a terminating decimal, but we *can* write it with an unending decimal expansion if we write zeros for all the decimal places after thousandths:

0.095 = 0.09500000000...

In other words, we can think of it as repeating the digit zero. In that sense, $0.095 = 0.095\overline{0}$. However, as you know, we normally write terminating decimals without the extra zeros.

3. Write each decimal using a line over the repeating part.

a. 0.09090909	b. 5.6843434343	c. 0.198666666666
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4. Do it the other way around: write the repeating digits several times followed by an ellipsis (three dots).

a. 0.0887 **b.** 0.2456 **c.** 2.17234

5. Which decimal is greater?

a. Which is more, $0.\overline{3}$ or 0.3 ?	b. Which is more, $0.\overline{55}$ or $0.\overline{5}$?
How much more?	How much more?
c. Which is more, 0.450 or 0.45? How much more? Sample worksheet from	d. Which is more, 0.12 or 0.12? How much more?

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Two-Step Equations, Part 1

In two-step equations, we need to apply two different operations to both sides of the equation.

Example 1. On the side of the unknown (left), there is a multiplication by 2 and an addition of 3. To isolate the unknown, we need to undo those two operations, in two steps.

$$3x + 2 = 25 - 2
3x = 23 + 3
x = 23/3$$

Check:

$$3 \cdot (23/3) + 2 \stackrel{?}{=} 25$$

 $23 + 2 \stackrel{?}{=} 25$
 $25 = 25$

0

What if you divide first? That is possible:

$$3x + 2 = 25
\frac{3x + 2}{3} = \frac{25}{3}
x + \frac{2}{3} = \frac{25}{3}
x = 23/3$$

$$\dot{z} = \frac{2}{3} - \frac{2}{3}$$

Note that this leads to fractions in the middle of the solution process which is more error-prone. Then, the 2 on the left side <u>also has to be divided by 3</u> (to become 2/3). This is something that is easy to forget and is therefore another reason why subtracting first is the "safer" way, in this case.

If this was a real-life application, we would probably give the answer as a decimal, rounded to a reasonable accuracy. Since it is a mathematical problem, we leave the answer as a fraction. (Why not as a mixed number? It is not wrong, but fractions are less likely to be misread. The mixed number 7 2/3 can easily be misread as 72/3.)

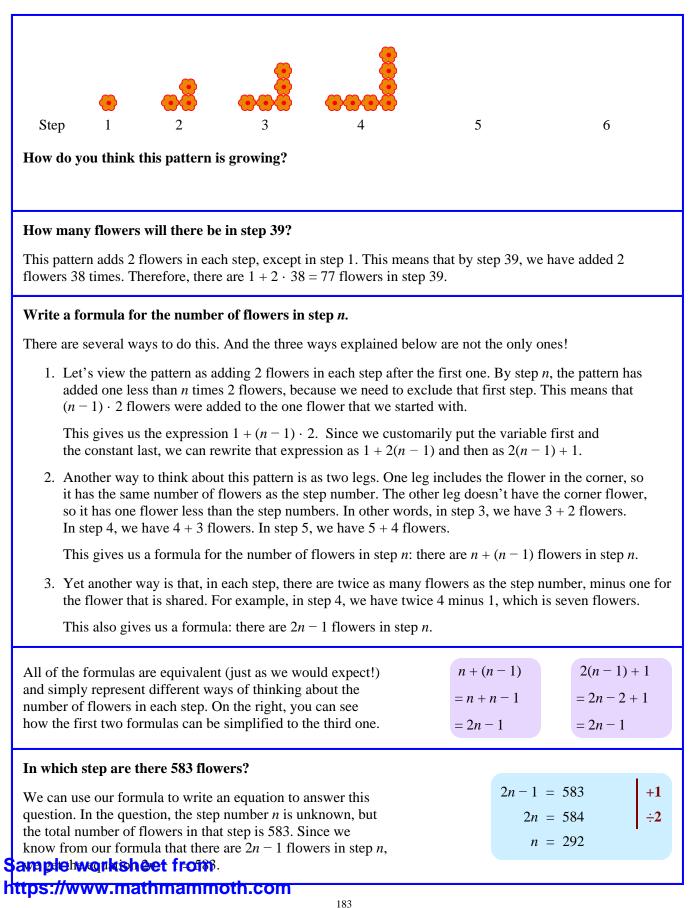
1. Solve. Check your solutions (as always!).

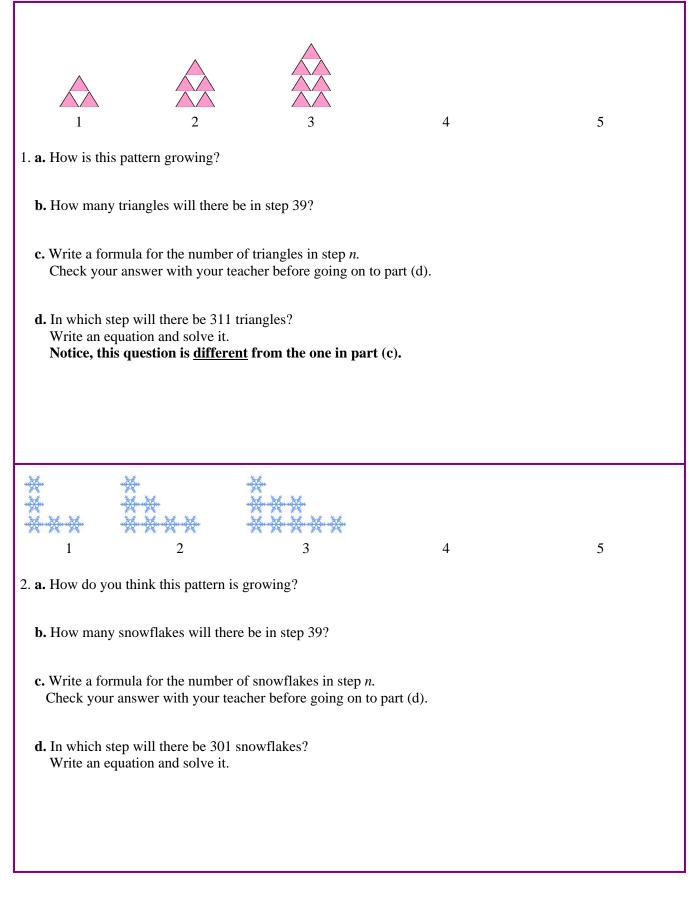
a.	5x + 2 = 67	b. $3y-2 = 70$	c. $3x + 11 = 74$
d.	8z - 2 = 98	e. 75 = $12x + 3$	f. 55 = $4z - 11$
	worksheet from		

https://www.mathmammoth.com

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Growing Patterns 2





Instead of showing the steps of the pattern horizontally, like in the previous exercises, we can also show them like the illustration on the right:

Now, each row of flowers is one step of the pattern.

- 3. A section of a flower garden has rows of flowers as shown on the right.
 - **a.** Write a formula that tells the gardener the number of flowers in row *n*.
 - **b.** How many flowers are in the 28th row?
 - **c.** In which row will there be 97 flowers? Write an equation and solve it.

- 4. Here, we have labeled the first row as "row 0."
 - **a.** Write a formula that tells the gardener the number of flowers in row *n*.
 - **b.** In which row will there be 97 flowers? Write an equation and solve it.

Step

1

What is the pattern of growth here?

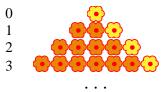
How many squares will there be in step 59?



2









5

3

4

Using the Distributive Property

Sometimes we need to use the distributive property to remove parentheses.	Example 1. $5(x+9) = 76$ 5x + 45 = 76	- 45
Depending on the context, this answer might also be given as the decimal 6.2.	5x = 31 $x = 31/5$	÷ 5

1. Solve. Give your answers as fractions or whole numbers.

a.	5(x+2) = 85	b.	9(y-2) = 66	c.	2(x-3) = 13
d.	70 9(, 0) 2		200 20(12) + 15		10(0) 0 10
u.	70 = 8(z+9) - 3z	e.	300 = 20(s - 12) + 15s	f.	10(x-9)-2 = 18
u.	70 = 8(z+9) - 3z	e.	300 = 20(s - 12) + 15s	f.	10(x-9)-2 = 18
u.	70 = 8(z+9) - 3z	e.	300 = 20(s - 12) + 15s	f.	10(x-9)-2 = 18
u.	70 = 8(z+9) - 3z	e.	300 = 20(s - 12) + 15s	f.	10(x-9)-2 = 18
	70 = 8(z+9) - 3z	e.	300 = 20(s - 12) + 15s	f.	10(x-9)-2 = 18

2. Solve. Now give your answers as decimals, rounded to three decimal digits.

-	a. $0.4(x+3) = 1.2$	b. $30(v - 0.4) = -1$	c.	0.98 = 3(x - 0.07) + 0.9x
Sa	ample worksheet from			

https://www.mathmammoth.com