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### Foreword

Math Mammoth Grade 5 comprises a complete math curriculum for the fifth grade mathematics studies. The curriculum meets (and exceeds) the Common Core standards.

Fifth grade is when we focus on fractions and decimals and their operations in great detail. Students also deepen their understanding of whole numbers, are introduced to the calculator, learn more problem solving and geometry, and study graphing. The main areas of study in Math Mammoth Grade 5 are:

- Multi-digit addition, subtraction, multiplication, and division (including division with two-digit divisors)
- Solving problems involving all four operations;
- The place value system, including decimal place value
- All four operations with decimals and conversions between measurements;
- The coordinate system and line graphs;
- Addition, subtraction, and multiplication of fractions; division of fractions in special cases;
- Geometry: volume and categorizing two-dimensional figures (especially triangles);

This book, 5-B, covers more on decimal arithmetic, in chapter 6. The focus is on decimal multiplication and division, and on conversions between measurement units. Chapter 7 has to do with fraction addition and subtraction, and chapter 8 with fraction multiplication and division. The last chapter (chapter 9) is about geometry. Students classify quadrilaterals and triangles, and learn about volume.

The part 5-A covers the four operations, place value and large numbers, problem solving, decimals, and graphing.

I heartily recommend that you read the full user guide in the following pages.

I wish you success in teaching math! Maria Miller, the author

## **User Guide**

Note: You can also find the information that follows online, at https://www.mathmammoth.com/userguides/ .

#### **Basic principles in using Math Mammoth Complete Curriculum**

Math Mammoth is mastery-based, which means it concentrates on a few major topics at a time, in order to study them in depth. The two books (parts A and B) are like a "framework", but you still have a lot of liberty in planning your child's studies. You can even use it in a *spiral* manner, if you prefer. Simply have your student study in 2-3 chapters simultaneously. In fifth grade, chapter 4 should be studied before chapter 6, and chapter 7 before chapter 8, but you can be flexible with the other chapters and schedule them earlier or later.

Math Mammoth is not a scripted curriculum. In other words, it is not spelling out in exact detail what the teacher is to do or say. Instead, Math Mammoth gives you, the teacher, various tools for teaching:

• The two student worktexts (parts A and B) contain all the lesson material and exercises. They include the explanations of the concepts (the teaching part) in blue boxes. The worktexts also contain some advice for the teacher in the "Introduction" of each chapter.

The teacher can read the teaching part of each lesson before the lesson, or read and study it together with the student in the lesson, or let the student read and study on his own. If you are a classroom teacher, you can copy the examples from the "blue teaching boxes" to the board and go through them on the board.

- There are hundreds of **videos** matched to the curriculum available at https://www.mathmammoth.com/videos/ . There isn't a video for every lesson, but there are dozens of videos for each grade level. You can simply have the author teach your child or student!
- Don't automatically assign all the exercises. Use your judgment, trying to assign just enough for your student's needs. You can use the skipped exercises later for review. For most students, I recommend to start out by assigning about half of the available exercises. Adjust as necessary.
- For each chapter, there is a **link list to various free online games** and activities. These games can be used to supplement the math lessons, for learning math facts, or just for some fun. Each chapter introduction (in the student worktext) contains a link to the list corresponding to that chapter.
- The student books contain some **mixed review lessons**, and the curriculum also provides you with additional **cumulative review lessons**.
- There is a chapter test for each chapter of the curriculum, and a comprehensive end-of-year test.
- The **worksheet maker** allows you to make additional worksheets for most calculation-type topics in the curriculum. This is a single html file. You will need Internet access to be able to use it.
- You can use the free online exercises at https://www.mathmammoth.com/practice/ This is an expanding section of the site, so check often to see what new topics we are adding to it!
- Some grade levels have cut-outs to make fraction manipulatives or geometric solids.
- And of course there are answer keys to everything.

#### How to get started

Have ready the first lesson from the student worktext. Go over the first teaching part (within the blue boxes) together with your child. Go through a few of the first exercises together, and then assign some problems for your child to do on their own.

Sample worksheet from https://www.mathmammoth.com

7

Repeat this if the lesson has other blue teaching boxes. Naturally, you can also use the videos at https://www.mathmammoth.com/videos/

Many students can eventually study the lessons completely on their own — the curriculum becomes self-teaching. However, students definitely vary in how much they need someone to be there to actually teach them.

#### **Pacing the curriculum**

Each chapter introduction contains a suggested pacing guide for that chapter. You will see a summary on the right.

Most lessons are 2 or 3 pages long, intended for one day. Some lessons are 4-5 pages and can be covered in two days. There are also some optional lessons (not included in the tables on the right).

It can also be helpful to calculate a general guideline as to how many pages per week the student should cover in order to go through the curriculum in one school year.

The table below lists how many pages there are for the

student to finish in this particular grade level, and gives you a guideline for how many pages per day to finish, assuming a 180-day (36-week) school year. The page count in the table below *includes* the optional lessons.

#### **Example:**

Grade level	School days	Days for tests and reviews	Lesson pages	Days for the student book	Pages to study per day	Pages to study per week
5-A	89	10	176	79	2.23	11.1
5-B	91	10	182	81	2.25	11.2
Grade 5 total	180	20	358	160	2.24	11.2

The table below is for you to fill in. Allow several days for tests and additional review before tests — I suggest at least twice the number of chapters in the curriculum. Then, to get a count of "pages to study per day", **divide the number of lesson pages by the number of days for the student book**. Lastly, multiply this number by 5 to get the approximate page count to cover in a week.

Grade level	Days for tests and reviews		Days for the student book	Pages to study per day	Pages to study per week
5-A		176			
5-B		182			
Grade 5 total		358			

Now, something important. Whenever the curriculum has lots of similar practice problems (a large set of problems), feel free to **only assign 1/2 or 2/3 of those problems**. If your student gets it with less amount of exercises, then that is perfect! If not, you can always assign the rest of the problems for some other day. In fact, you could even use these unassigned problems the next week or next month for some additional review.

In general, 1st-2nd graders might spend 25-40 minutes a day on math. Third-fourth graders might spend 30-60 minutes a day. Fifth-sixth graders might spend 45-75 minutes a day. If your student finds math enjoyable, they can of course spend more time with it! However, it is not good to drag out the lessons on a regular basis, because that can then affect the student's attitude towards math.

Worktext 5-A			Workte	xt 5-B
Chapter 1	21 days		Chapter 6	22 days
Chapter 2	12 days		Chapter 7	18 days
Chapter 3	9 days		Chapter 8	20 days
Chapter 4	18 days		Chapter 9	12 days
Chapter 5	11 days		TOTAL	72 days
TOTAL	71 days	'		

#### Working space, the usage of additional paper and mental math

The curriculum generally includes working space directly on the page for students to work out the problems. However, feel free to let your students to use extra paper when necessary. They can use it, not only for the "long" algorithms (where you line up numbers to add, subtract, multiply, and divide), but also to draw diagrams and pictures to help organize their thoughts. Some students won't need the additional space (and may resist the thought of extra paper), while some will benefit from it. Use your discretion.

Some exercises don't have any working space, but just an empty line for the answer (e.g.  $200 + \_\_\_ = 1,000$ ). Typically, I have intended that such exercises to be done using MENTAL MATH.

However, there are some students who struggle with mental math (often this is because of not having studied and used it in the past). As always, the teacher has the final say (not me!) as to how to approach the exercises and how to use the curriculum. We do want to prevent extreme frustration (to the point of tears). The goal is always to provide SOME challenge, but not too much, and to let students experience success enough so that they can continue enjoying learning math.

Students struggling with mental math will probably benefit from studying the basic principles of mental calculations from the earlier levels of Math Mammoth curriculum. To do so, look for lessons that list mental math strategies. They are taught in the chapters about addition, subtraction, place value, multiplication, and division. My article at https://www.mathmammoth.com/lessons/practical\_tips\_mental\_math also gives you a summary of some of those principles.

#### Using tests

For each chapter, there is a **chapter test**, which can be administered right after studying the chapter. **The tests are optional.** Some families might prefer not to give tests at all. The main reason for the tests is for diagnostic purposes, and for record keeping. These tests are not aligned or matched to any standards.

In the digital version of the curriculum, the tests are provided both as PDF files and as html files. Normally, you would use the PDF files. The html files are included so you can edit them (in a word processor such as Word or LibreOffice), in case you want your student to take the test a second time. Remember to save the edited file under a different file name, or you will lose the original.

The end-of-year test is best administered as a diagnostic or assessment test, which will tell you how well the student remembers and has mastered the mathematics content of the entire grade level.

#### Using cumulative reviews and the worksheet maker

The student books contain mixed review lessons which review concepts from earlier chapters. The curriculum also comes with additional cumulative review lessons, which are just like the mixed review lessons in the student books, with a mix of problems covering various topics. These are found in their own folder in the digital version, and in the Tests & Cumulative Reviews book in the print version.

The cumulative reviews are optional; use them as needed. They are named indicating which chapters of the main curriculum the problems in the review come from. For example, "Cumulative Review, Chapter 4" includes problems that cover topics from chapters 1-4.

Both the mixed and cumulative reviews allow you to spot areas that the student has not grasped well or has forgotten. When you find such a topic or concept, you have several options:

- 1. Check if the worksheet maker lets you make worksheets for that topic.
- 2. Check for any online games and resources in the Introduction part of the particular chapter in which this topic or concept was taught.

- 3. If you have the digital version, you could simply reprint the lesson from the student worktext, and have the student restudy that.
- 4. Perhaps you only assigned 1/2 or 2/3 of the exercise sets in the student book at first, and can now use the remaining exercises.
- 5. Check if our online practice area at https://www.mathmammoth.com/practice/ has something for that topic.
- 6. Khan Academy has free online exercises, articles, and videos for most any math topic imaginable.

#### **Concerning challenging word problems and puzzles**

While this is not absolutely necessary, I heartily recommend supplementing Math Mammoth with challenging word problems and puzzles. You could do that once a month, for example, or more often if the student enjoys it.

The goal of challenging story problems and puzzles is to **develop the student's logical and abstract thinking and mental discipline**. I recommend starting these in fourth grade, at the latest. Then, students are able to read the problems on their own and have developed mathematical knowledge in many different areas. Of course I am not discouraging students from doing such in earlier grades, either.

Math Mammoth curriculum contains lots of word problems, and they are usually multi-step problems. Several of the lessons utilize a bar model for solving problems. Even so, the problems I have created are usually tied to a specific concept or concepts. I feel students can benefit from solving problems and puzzles that require them to think "out of the box" or are just different from the ones I have written.

I recommend you use the free Math Stars problem-solving newsletters as one of the main resources for puzzles and challenging problems:

#### Math Stars Problem Solving Newsletter (grades 1-8) https://www.homeschoolmath.net/teaching/math-stars.php

I have also compiled a list of other resources for problem solving practice, which you can access at this link:

#### https://l.mathmammoth.com/challengingproblems

Another idea: you can find puzzles online by searching for "brain puzzles for kids," "logic puzzles for kids" or "brain teasers for kids."

#### Frequently asked questions and contacting us

If you have more questions, please first check the FAQ at https://www.mathmammoth.com/faq-lightblue

If the FAQ does not cover your question, you can then contact us using the contact form at the Math Mammoth.com website.

### Chapter 6: Decimals, Part 2 Introduction

This chapter focuses on decimal multiplication and division, and conversions between measurement units.

We start out with the topic of multiplying and dividing decimals by powers of ten, presented with the help of place value charts. This is familiar to students from chapter 2, where they multiplied and divided whole numbers by powers of ten. The number being multiplied or divided *moves* in the place value chart, as many places as there are zeros in the power of ten.

As a shortcut, we can move the decimal point. However, the movement of the decimal point is an "illusion"—that is what seems to happen—but in reality, the number itself got bigger or smaller; thus, its digits actually changed positions in the place value chart.

Next, we study how to multiply decimals by decimals. The common rule (or shortcut) for it says to multiply the numbers without the decimal points, and then add the decimal point to the product (answer) so that it has as many decimal digits as the factors have in total. We justify this rule using the recently learned technique for dividing decimals by powers of ten. Students are also encouraged to use estimation in decimal multiplications, and they solve problems connected to real life.

Then students learn about multiplication as *scaling*. We cannot view decimal multiplications, such as  $0.4 \times 1.2$ , as repeated addition. Instead, they are viewed as scaling—shrinking or enlarging—the number or quantity by a scaling factor. So,  $0.4 \times 1.2$  is thought of as scaling 1.2 by 0.4, or as four-tenths *of* 1.2. You may recognize this as the same as 40% of 1.2.

Next, we go on to decimal divisions that can be done with mental math. Students divide decimals by whole numbers (such as  $0.8 \div 4$  or  $0.45 \div 4$ ) by relating them to equal sharing. They divide decimals by decimals in situations where the divisor goes evenly into the dividend, thus yielding a whole-number quotient (e.g.  $0.9 \div 0.3$  or  $0.072 \div 0.008$ ).

In the lesson *More Division with Decimals*, we review long division with decimals, when the divisor is a whole number.

Then, we study the metric system and how to convert various metric units (within the metric system), such as converting kilograms to grams, or dekaliters to hectoliters. The first of the two lessons mainly deals with very commonly used metric units, and we use the meaning of the prefix to do the conversion. For example, centimeter is a hundredth part of a meter, since the prefix "centi" means 1/100. Knowing that, gives us a means of converting between centimeters and meters.

The second lesson deals with more metric units, even those not commonly used, such as dekaliters and hectograms, and teaches a method for conversions using a chart. These two methods for converting measuring units within the metric system are sensible and intuitive, and help students not to rely on mechanical formulas.

Next, we turn our attention to dividing decimals by decimals, which then completes our study of all decimal arithmetic. The principle here is fairly simple, but it is easy to forget (multiply both the dividend and the divisor by a power of ten, until you have a whole-number divisor).

After learning that, students practice measurement conversions within the customary system and do some generic problem solving with decimals.

Recall that not all students need all the exercises; use your judgment. Problems accompanied by a small picture of a calculator are meant to be solved with the help of a calculator. Otherwise, a calculator should not be allowed.

#### Pacing Suggestion for Chapter 6

This table does not include the chapter test as it is found in a different book (or file). Please add one day to the pacing for the test if you will use it.

The Lessons in Chapter 6	page	span	suggested pacing	your pacing
Multiply and Divide by Powers of Ten, Part 1	13	3 pages	1 day	
Multiply and Divide by Powers of Ten, Part 2	16	3 pages	1 day	
Multiply and Divide by Powers of Ten, Part 3 (optional)	19	(2 pages)	(1 day)	
Multiply Decimals by Decimals 1	21	2 pages	1 day	
Multiply Decimals by Decimals 2	23	3 pages	1 day	
Multiplication as Scaling	26	4 pages	2 days	
Decimal Multiplication — More Practice	30	2 pages	1 day	
Dividing Decimals—Mental Math	32	3 pages	1 day	
More Division with Decimals	35	3 pages	1 day	
The Metric System, Part 1	38	4 pages	2 days	
The Metric System, Part 2	42	3 pages	1 day	
Divide Decimals by Decimals 1	45	3 pages	1 day	
Divide Decimals by Decimals 2	48	4-5 pages	2 days	
Converting Between Customary Units of Measurement	53	4 pages	2 days	
Problem Solving	57	4 pages	2 days	
Mixed Review Chapter 6	61	2 pages	1 day	
Chapter 6 Review	63	5 pages	2 days	
Chapter 6 Test (optional)				
TOTALS		53 pages	22 days	
with optional content		(55 pages)	(23 days)	

### Helpful Resources on the Internet

We have compiled a list of Internet resources that match the topics in this chapter. We heartily recommend you take a look! Many of our customers love using these resources to supplement the bookwork. You can use these resources as you see fit for extra practice, to illustrate a concept better and even just for some fun. Enjoy!

### https://l.mathmammoth.com/gr5ch6



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7-7-7

## Multiply and Divide by Powers of Ten 1

Remember? The number system we use is based on number 10. Therefore, each place value unit is always ten times the previous unit: 10 ones makes a ten, 10 tens makes a hundred, 10 hundreds makes a thousand. Because of this, when a number is multiplied by ten, the digits of the number essentially *move* in the place value chart!

**Example 1.** When 215 is multiplied by 10, each of its digits <u>moves one slot</u> to the left in the place value chart.

- The "2" in the hundreds place, signifying 200, becomes 2,000.
- The "1" in the tens place, signifying 10, becomes 100.
- The "5" in the ones place (signifying 5) becomes 50.

It works the same way with decimals: each place value unit is ten times the previous unit.

**Example 2.** 10 hundredths makes a tenth (or  $10 \times 0.01 = 0.1$ ).

Using the place value chart, the digit one (signifying one hundredth) *moves* in the chart one slot to the left.

What if 0.01 was multiplied by 100?

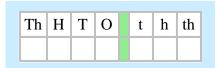
**Example 3.** Since  $10 \times 0.01 = 0.1$ , it follows that 10 times *seven* hundredths equals seven tenths. The digit 7 moves in the place value chart one step to the left.

What if seven hundredths was multiplied by 100? By 1,000?

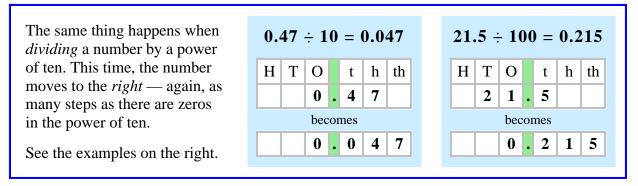
What if there were other digits?

- 1. **a.** Using this technique, what happens to 7 thousandths when it is multiplied by 100? Explain, using the place value chart.
  - **b.** What happens to 0.35 when it is multiplied by 1,000? Explain.

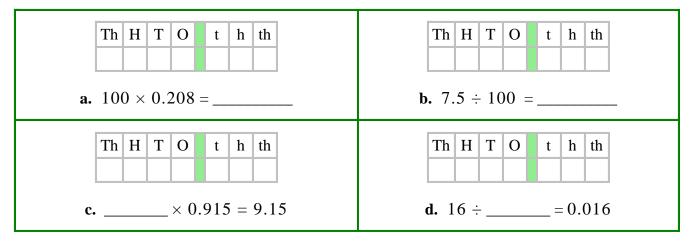




When you multiply a number by a power of ten (10, 100, 1000, etc.), each digit of the number *moves* in the place value chart as many steps as there are zeros in the power of ten.



2. Fill in the missing numbers. Use the place value charts to help.



3. Multiply and divide. Notice the patterns. You can use the place value charts to help.

<b>a.</b> 10 × 0.04 =	<b>b.</b> 450 ÷ 10 =	Th H T O t h th
100 × 0.04 =	450 ÷ 100 =	
1,000 × 0.04 =	450 ÷ 1,000 =	Th H T O t h th
10,000 × 0.04 =	450 ÷ 10,000 =	
0.5.10	10 0056	Th H T O t h th
<b>c.</b> $0.5 \div 10 =$	<b>d.</b> $10 \times 0.056 =$	
$0.5 \div 100 =$	$100 \times 0.056 =$	Th H T O t h th
<b>e.</b> $2 \div 100 =$	<b>f.</b> $100 \times 2.3 =$	
2 ÷ 1,000 =	1,000 × 2.3 =	ThHTOththIIIIIII
<b>g.</b> × 0.89 = 89	<b>h.</b> 78.6 ÷ = 0.786	Th H T O t h th
× 0.209 = 2.09	24 ÷ = 0.024	

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### **Converting Between Customary Units of Measurement**

<u>Units of weight</u>			Units of weightUnits of volume			Units	s of length	
	(short) ton	Т		gallon	gal	1700	mile	mi
	pound	lb	$4 \rightarrow$	quart	qt		yard	yd
16 (	ounce	OZ		pint	pt		foot	ft
				cup	С		inch	in
				(fluid) ounce	fl. oz.			

To convert from one neighboring unit to another, either **multiply** or **divide by the conversion factor.** 

If you don't know which, THINK if the result needs to be a smaller or a bigger number.

**Example 1.** Convert 53 fluid ounces into cups.

The conversion factor we need is 8, because 8 (fluid) ounces makes a cup (look at the chart). And, ounces are smaller units than cups, so 53 ounces as cups will make *fewer* cups (you need fewer cups since they are the bigger units). So, we need to divide by the factor 8:

We get  $53 \div 8 = 6$  R5. This result means 53 fluid ounces is 6 cups and 5 (leftover) ounces.

You can also think of it this way: since eight ounces makes a cup, we need to figure how many cups or how many "8 ounce servings" there are in 53 ounces. How many 8s are in 53? That is solved by division.

1. Convert.

<b>a.</b> 6 ft = in.	<b>b.</b> 25 in = ft in	<b>c.</b> 13 ft 7 in = in
7 ft 5 in = in.	45 in = ft in	71 in = ft in

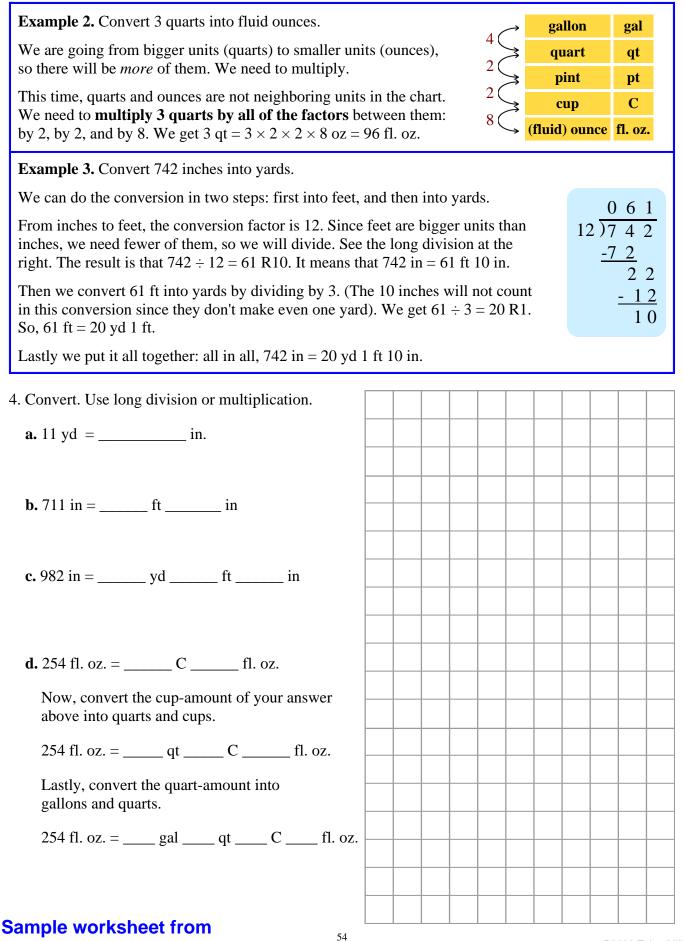
2. Convert.

<b>a.</b> 2 lb 8 oz = oz	<b>b.</b> 8 lb = oz	<b>c.</b> 43 oz = lb oz
45 oz = lb oz	56 oz = lb oz	90 oz = lb oz

3. Convert.

<b>a.</b> $3 C = $ fl. oz.	<b>b.</b> 4 C = pt	<b>c.</b> 7 gal = qt
55 fl. oz. = C fl. oz.	3 pt = C	45 qt = gal qt





#### https://www.mathmammoth.com

T

lb

0Z

(short) ton

pound

ounce

**Example 4.** Convert 4.52 lb into ounces.

We are going from bigger units (pounds) to smaller units (ounces), so there will be lots more of them. We need to *multiply*.

Using a calculator, we get  $4.52 \times 16 = 72.32$  oz.

**Example 5.** How many miles is 8,400 feet?

Since one mile is 5,280 feet, then 8,400 feet would be somewhere between 1 and 2 miles. To find out exactly, use division, and round the answer:  $8,400 \div 5,280 = 1.59090909... \approx 1.59$  miles.

5. Convert. Use a calculator. Round your answer to two decimal digits, if necessary.

<b>a.</b> 7.4 mi = ft	<b>b.</b> 1,500 ft = yd	1,760
16,000 ft = mi	7,500 yd = mi	$3 \xrightarrow{\text{yard}} \text{yd}$ $3 \xrightarrow{\text{foot}} \text{ft}$
<b>c.</b> 900 ft = mi 2.56 mi = vd	<b>d.</b> $12.54 \text{ mi} = \text{ft}$	$12 \rightarrow \text{inch}$ in
$2.56 \text{ mi} = \ \text{yd}$	82,000 ft = mi	1  mile = 5,280  feet

6. Convert. Use a calculator. Round your answer to two decimal digits, if necessary.

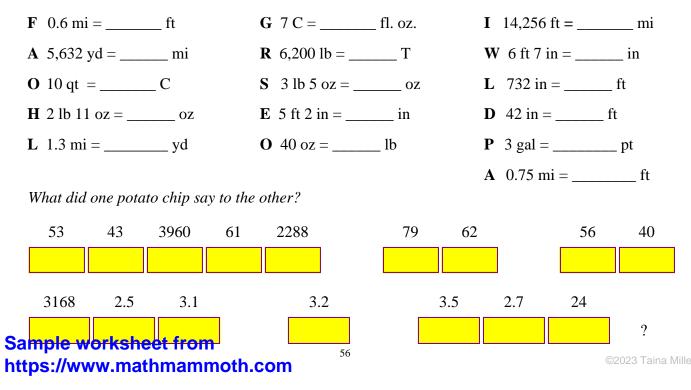
<b>a.</b> 15.2 lb = oz	<b>b.</b> $4.78 \text{ T} = \ \text{lb}$	<b>c.</b> 78 oz = lb
655 oz = lb	7,550 lb = T	0.702 T = lb

7. How many 8-inch pieces can you cut out of 9 3/4 ft of ribbon?

- 8. A road maintenance crew completed 0.7 mi of road on Monday, 0.65 mi on Tuesday, and 0.5 mi on each of the remaining three weekdays. Find how much road they completed in the week, both in miles and in feet.
- 9. Mount McKinley is 20,320 feet tall. The International Space Station flies 211.3 miles above the Earth. How many mountains the height of Mt. McKinley would you need to stack on top of each other in order to reach the altitude of the International Space Station?

#### 10. Solve.

- **a.** If you serve 1-cup servings of juice to 30 people, how many *whole* gallons of juice will you need?
- **b.** A bottle of shampoo weighs 13 oz, and there are 20 of them in a box. The box itself weighs 8 oz. How much does the box with the bottles of shampoo weigh in total, in pounds and ounces?
- **c.** Mark drinks three 5-ounce servings of coffee a day. Find how much coffee he drinks in a month (30 days). Give your answer in bigger units, not in fluid ounces.
- **d.** Erica lost 5 lb of weight over 4 weeks of time. How much weight did she lose daily, on average?
- 11. For more practice, solve the riddle. Use a calculator for the problems you cannot solve in your head.



### **Problem Solving**

Example 1. John spent 3/10 of his money and had \$45.57 left. How much did John have initially?		
John spent 3/10 of his money, which means his money is divided into <u>10 parts</u> . We draw a bar model where the bar represents all of his money (the total) and is divided into 10 parts.		
He spent 3 parts, so <i>seven</i> parts are left! The money he has left (\$45.57) is seven parts in the model. Simply divide \$45.57 by seven to get one part (1/10) of John's initial money. Then multiply that number by 10, and you get how much he had in the beginning:		
$45.57 \div 7 = 6.51$ . Then, $10 \times 6.51 = 65.10$ . John had $65.10$ initially.		

Drawing a bar model can help. Use a notebook for calculations.

- 1. Amy cut off 2/9 of a board. The remaining piece was 4.69 m long.
  - **a.** How long was the board originally?
  - **b.** How long was the piece she cut off?

- 2. The price of a bouquet of tulips is 3/4 of the price of a bouquet of roses. The bouquet of tulips costs \$15.60.
  - a. How much does a bouquet of roses cost?
  - **b.** Find the total price of buying two bouquets of tulips and three bouquets of roses.

Read carefully the different ways to solve this simple problem:

Example 2. A rake cost \$29.50 but the price was reduced by 1/10. What is the new price?

#### Solution 1:

We find 1/10 of the price and subtract that from the original price. Find 1/10 of \$29.50 by dividing:

 $29.50 \div 10 = 2.95.$ 

The new price is: \$29.50 - \$2.95 = \$26.55.

#### **Solution 2:**

Notice that 9/10 of the price will be "left." To find 9/10 of the price, divide the current price by 10 and multiply what we get by 9:

 $29.50 \div 10 = 2.95.$ 

 $9 \times \$2.95 = \$26.55$ 

#### Solution 3:

Again, 9/10 of the price will be "left," and 9/10 is 0.9.

9/10 *of* the price becomes 0.9 *times* the price:

 $0.9 \times \$29.50 = \$26.55$ 

All three solutions are correct, but in my opinion, solution 3 is the most "elegant" because it takes the least effort. When solving problems, you should also consider what is the shortest or most efficient way.

3. Find the discounted price when a table that costs \$44.50 is discounted by 2/10 of its price.

- 4. The shoe store had a sale with all shoes discounted by 3/10 of their price. Marsha bought a pair of sandals and a pair of tennis shoes. The sandals had originally cost \$12.50 and the tennis shoes \$25.90.
  - a. How much do the discounted sandals cost?
  - **b.** How much do the discounted tennis shoes cost?
  - **c.** What was the total cost?

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### Chapter 7: Fractions: Add and Subtract Introduction

In 5th grade, students study most aspects of fraction arithmetic: addition, subtraction, multiplication, and then in some special cases, division. Division of fractions is studied in more detail in 6th grade.

This chapter starts out with a review lesson on mixed numbers, and then with lessons on various ways to add and subtract mixed numbers. These are meant partially to review and partially to develop speed in fraction calculations. The lesson *Subtracting Mixed Numbers 2* presents an optional way to subtract, where we use a negative fraction. This is only meant for students who can easily grasp subtractions such as (1/5) - (4/5) = -3/5, and is not intended to become a "stumbling block." Simply skip it if necessary.

Students have already added and subtracted *like* fractions in fourth grade. Now it is time to "tackle" the more complex situation of *unlike* fractions (with different denominators). To that end, students learn how to convert fractions into other equivalent fractions. These lessons first use a visual model of splitting pie pieces further, and from that, we develop the common procedure for equivalent fractions.

This skill is used immediately in the next lessons about adding and subtracting unlike fractions. We begin this topic by using visual models, and then gradually advance toward the abstract. Several lessons are devoted to understanding and practicing the basic concept, and also to applying this new skill to mixed numbers.

The lesson *Comparing Fractions* reviews some mental math methods for comparing fractions. Students also learn a "brute force" method based on converting fractions to equivalent fractions.

The chapter ends with lessons on measuring in inches, using units as small as 1/16 of an inch.

#### Pacing Suggestion for Chapter 7

This table does not include the chapter test as it is found in a different book (or file). Please add one day to the pacing for the test if you will use it.

The Lessons in Chapter 7	page	span	suggested pacing	your pacing
Fraction Terminology	69			
Review: Mixed Numbers	70	3 pages	1 day	
Adding Mixed Numbers	73	3 pages	1 day	
Subtracting Mixed Numbers 1	76	4 pages	2 days	
Subtracting Mixed Numbers 2 (optional)	80	(2 pages)	(1 day)	
Equivalent Fractions 1	82	3 pages	1 day	
Equivalent Fractions 2	85	2 pages	1 day	
Adding and Subtracting Unlike Fractions	87	3 pages	1 day	
Finding the (Least) Common Denominator	90	3 pages	1 day	
Add and Subtract: More Practice	93	3 pages	1 day	
Adding and Subtracting Mixed Numbers	96	3 pages	1 day	
Comparing Fractions	99	5 pages	2 days	
Word Problems	104	2 pages	1 day	
Measuring in Inches	106	4 pages	2 days	

The Lessons in Chapter 7	page	span	suggested pacing	your pacing
Line Plots and More Measuring	109	2.5 pages	1 day	
Mixed Review Chapter 7	112	3 pages	1 day	
Chapter 7 Review	115	2.5 pages	1 day	
Chapter 7 Test (optional)				
TOTALS		46 pages	18 days	
with optional content	Į	(48 pages)	(19 days)	

#### Helpful Resources on the Internet

We have compiled a list of Internet resources that match the topics in this chapter, including pages that offer:

- online practice for concepts;
- online games, or occasionally, printable games;
- animations and interactive illustrations of math concepts;
- **articles** that teach a math concept.

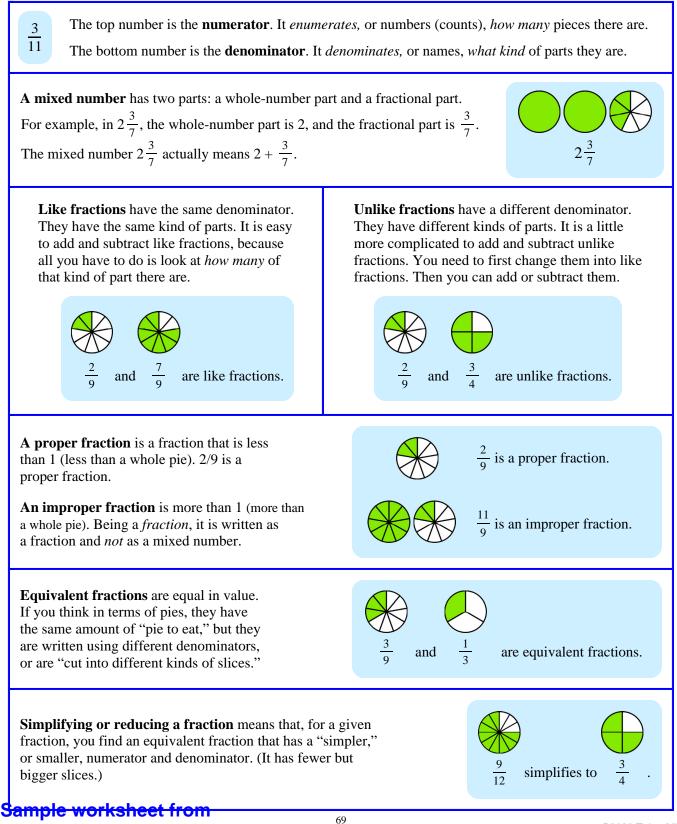
We heartily recommend you take a look! Many of our customers love using these resources to supplement the bookwork. You can use these resources as you see fit for extra practice, to illustrate a concept better and even just for some fun. Enjoy!

https://l.mathmammoth.com/gr5ch7



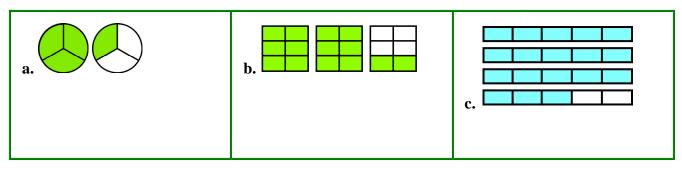
# **Fraction Terminology**

As we study fraction operations, it is important that you understand the terms, or words, that we use. This page is for reference. You can post it on your wall or even make your own fraction poster based on it. Some of the terms below you already know; some we will study in this chapter.



### **Review: Mixed Numbers**

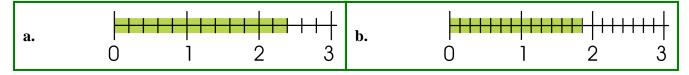
1. Write the mixed numbers that these pictures illustrate.



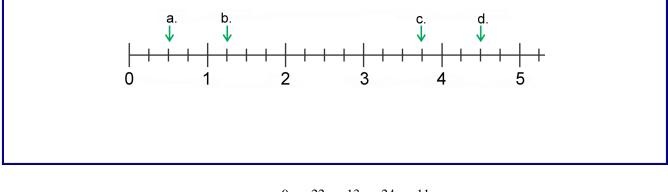
#### 2. Draw pictures that illustrate these mixed numbers.

<b>a.</b> $3\frac{2}{6}$	<b>b.</b> $4 \frac{7}{8}$

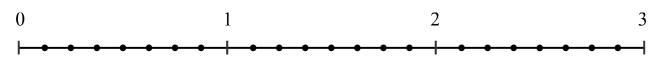
#### 3. Write the mixed number that is illustrated by each number line.



#### 4. Write the fractions and mixed numbers that the arrows indicate.



5. Mark the fractions on the number line.  $\frac{9}{8}$ ,  $\frac{22}{8}$ ,  $\frac{13}{8}$ ,  $\frac{24}{8}$ ,  $\frac{11}{8}$ 



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 $3\frac{11}{8} \implies 4\frac{3}{8}$ 

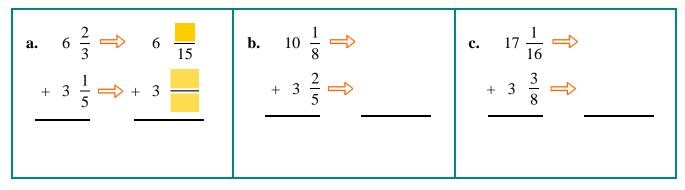
## **Adding and Subtracting Mixed Numbers**

In this lesson, we will be adding and subtracting **mixed numbers with unlike fractional parts.** Here's how: 1. First convert the unlike fractional parts into like fractions. Example 1. $2 \frac{1}{2} \implies 2 \frac{4}{8}$  $+ 1 \frac{7}{8} \implies + 1 \frac{7}{8}$  $3 \frac{11}{8}$ 

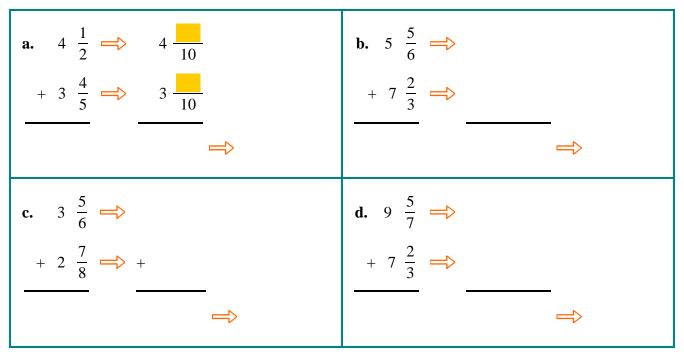
2. Then add or subtract the mixed numbers.

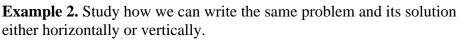
Notice that the answer,  $3 \, 11/8$ , has a fractional part that is more than one (an improper fraction). Therefore, we need to write it as  $4 \, 3/8$ .

1. First convert the fractional parts into like fractions, then add.



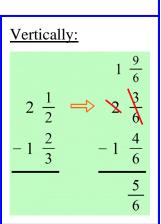
2. First convert the fractional parts into like fractions, then add. Lastly, change your final answer so that the fractional part is not an improper fraction.



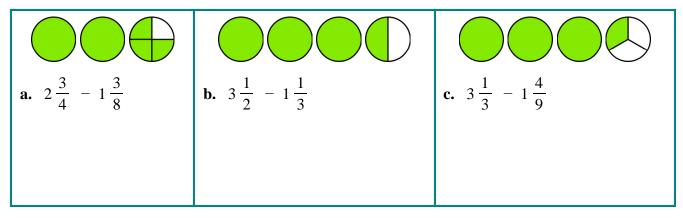


Horizontally:  $2\frac{1}{2} - 1\frac{2}{3} = 2\frac{3}{6} - 1\frac{4}{6}$  $=1\frac{9}{6}-1\frac{4}{6}=\frac{5}{6}$ Notice how 2 3/6 is renamed as 1 9/6. This is the

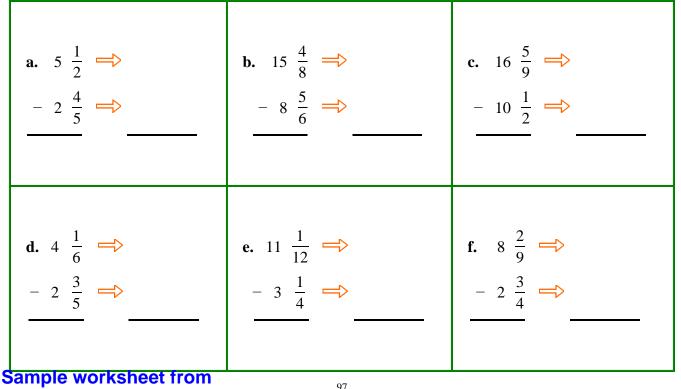
same process as regrouping in the vertical solution.



3. Solve. You can use the pies to help.



4. First convert the fractional parts into like fractions, then subtract. You may need to regroup.



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5. Spot the unreasonable answers, and correct them.

<b>a.</b> <sup>1</sup> ⁄ <sub>2</sub> kg of meat and another <sup>1</sup> ⁄ <sub>4</sub> kg of meat makes 2/6 kg of meat.	<ul> <li>b. Mike: "As of today, <sup>1</sup>/<sub>5</sub> of the job is done, and tomorrow I'll do half of it. That means 6/5 of it will be done."</li> </ul>
<b>c.</b> <sup>3</sup> / <sub>8</sub> cups of flour and another <sup>1</sup> / <sub>2</sub> cup of flour will make <sup>7</sup> / <sub>8</sub> cups of flour.	d. Mia: "Last week I jogged 9 ½ km, and this week 7 ¾ km. So, last week I jogged 1 ¾ km more than this week."

6. Sally needs 1 1/4 meters of material to make a blouse and 8/10 of a meter to make a skirt.

**a.** Find how many meters of material she needs for both of them.

**b.** Now use *decimals* to solve the same problem. Which way do you feel is easier?

- 7. Henry's two heaviest school books weigh 1 3/4 lb and 1 11/16 lb.
  - **a.** What is their total weight in *pounds*?

**b.** Remember that 1 lb = 16 oz. Now change the total weight into pounds and ounces.

#### Sample worksheet from https://www.mathmammoth.com

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### Chapter 8: Fractions: Multiply and Divide Introduction

This is another chapter devoted solely to fractions. It rounds out our study of fraction arithmetic. If you feel that your student(s) would benefit from taking a break from fractions, you could have them study chapter 9 (geometry) in between chapters 7 and 8.

We start out by simplifying fractions. Since this process is the opposite of making equivalent fractions, studied in chapter 7, it should be relatively simple for students to understand. We also use the same visual model, just backwards: this time the pie pieces are joined together instead of split apart.

Next we study multiplying a fraction and a whole number. The lesson shows how, for example,  $3 \times (4/5)$  can be seen as three copies of 4/5 — as repeated addition. In this case, all that is needed is find the number of fifths (number of slices), and that is simply  $3 \times 4$ .

We also delve into the idea of interpreting a fraction times a whole number as a fractional part of a quantity. For example,  $(2/3) \times 18$  is seen as two-thirds of 18 (say 18 km or \$18). In this sense, the word "of" as if "translates" into the multiplication symbol.

The next lesson continues to build on this idea, explaining the multiplication of a fraction by a fraction as taking a certain part of a fraction. The lesson also shows the usual shortcut for the multiplication of fractions.

Then, we study the area of a rectangle with fractional side lengths, and show that the area is the same as it would be found by multiplying the side lengths. Students multiply fractional side lengths to find areas of rectangles, and represent fraction products as rectangular areas.

Simplifying before multiplying is a process that is not absolutely necessary for fifth graders. I have included it here because it prepares students for the same process in future algebra studies, and also because it makes fraction multiplication easier. I have also included explanations of *why* we are allowed to simplify before multiplying, so that students can become familiar with mathematical reasoning (actually, proofs).

Students also multiply mixed numbers, and study how multiplication can be seen as resizing or scaling.

Next, we study division of fractions in special cases. The first one is seeing fractions *as* divisions; in other words recognizing that 5/3 is the same as  $5 \div 3$ . This gives us a means of dividing whole numbers in such a manner that the answer has a fractional part (for example,  $20 \div 6 = 32/6$ ).

The next case is sharing divisions—divisions that can be interpreted as equal sharing. For example, if 4/5 of a pie is shared equally between two people, how much does each person get? In particular, we look at dividing a unit fraction by a whole number (e.g.  $(1/4) \div 3$ ) in this context of equal sharing. Students work with visual models, and via their work, find a shortcut for these types of divisions.

The following lesson then focuses on "measurement divisions", where we think how many times the divisor "fits into" the dividend. Again, visual models help a lot. The focus is on dividing a whole number by a unit fraction (e.g.  $3 \div (1/4)$ ).

The last lesson, on the shortcut for fraction division, is optional. It reveals the common rule for fraction division: each division is actually changed into a *multiplication* by the reciprocal of the divisor. In 5th grade, students are not required to master fraction division in all cases, and that is why this is an optional lesson. This rule is studied in 6th grade in detail.

#### **Pacing Suggestion for Chapter 8**

This table does not include the chapter test as it is found in a different book (or file). Please add one day to the pacing for the test if you will use it.

The Lessons in Chapter 8	page	span	suggested pacing	your pacing
* Simplifying Fractions 1	121	3 pages	1 day	
* Simplifying Fractions 2	124	3 pages	1 day	
Multiply Fractions and Whole Numbers, Part 1	127	2 pages	1 day	
Multiply Fractions and Whole Numbers, Part 2	129	2 pages	1 day	
Multiplying Fractions by Fractions, Part 1	131	3 pages	1 day	
Multiplying Fractions by Fractions, Part 2	134	2 pages	1 day	
Fraction Multiplication and Area	136	6 pages	2 days	
* Simplifying Before Multiplying	142	3 pages	1 day	
Multiply Mixed Numbers	145	3 pages	1 day	
Multiplication as Scaling/Resizing	148	3 pages	2 days	
Fractions Are Divisions	151	4 pages	2 days	
Dividing Fractions: Sharing Divisions	155	3 pages	1 day	
Dividing Fractions: Fitting the Divisor	158	3 pages	1 day	
Dividing Fractions: Summary	161	2 pages	1 day	
* Dividing Fractions: The Shortcut (optional)	163	(3 pages)	(1 day)	
Mixed Review Chapter 8	166	3 pages	1 day	
Chapter 8 Review	169	4 pages	2 days	
Chapter 8 Test (optional)				
TOTALS		49 pages	20 days	
with optional content		(52 pages)	(21 days)	

#### Helpful Resources on the Internet

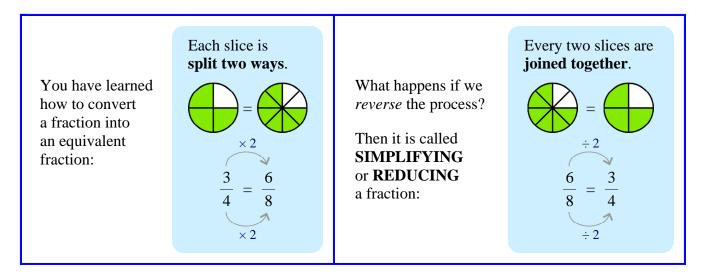
We have compiled a list of Internet resources that match the topics in this chapter, including pages that offer:

- online practice for concepts;
- online **games**, or occasionally, printable games;
- animations and interactive illustrations of math concepts;
- **articles** that teach a math concept.

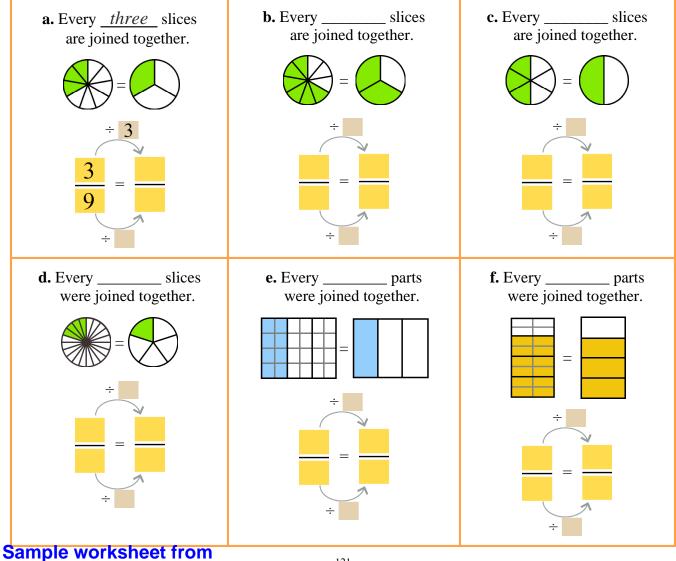
## https://l.mathmammoth.com/gr5ch8



## **Simplifying Fractions 1**



1. Simplify the following fractions, filling in the missing parts.



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## **Multiplying Mixed Numbers**

Multiplying mixed numbers is not difficult at all.  $1\frac{2}{3} \times 2\frac{5}{6}$ • First, change the mixed numbers to fractions. • Then multiply the fractions.  $\frac{5}{3}$  ×  $\frac{17}{6} = \frac{85}{18} = 4\frac{13}{18}$ • Give your answer as a mixed number and in lowest terms. The most difficult part of this is to remember not to multiply Estimation:  $12/3 \times 3 = 5$ . the mixed numbers until you have first changed them The answer is fairly close to 5, into fractions. so it is reasonable. Optionally, if you know how, it can really help to simplify  $4\frac{2}{9} \times 3\frac{3}{8}$ before multiplying, because then the numerators and the denominators become smaller numbers. 19 Note: simplify ONLY after you have changed the 38 mixed numbers to fractions, not before. You can always use estimation to check that your Estimation:  $4 \times 3\frac{1}{2} = 14$ . The answer answer is reasonable (not too big or too small).  $14 \frac{1}{4}$  is close to that, so it makes sense.

1. Multiply. Don't forget: After you change the mixed numbers into fractions, you can simplify crisscross to make things easier for yourself! Use estimation to **check that your answer is reasonable** (not too big or too small).

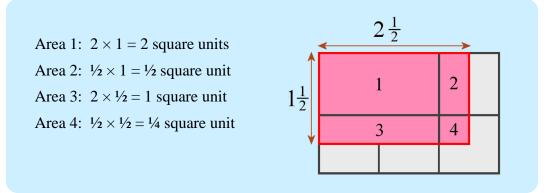
**a.** 
$$2\frac{1}{4} \times 1\frac{1}{2}$$
**b.**  $5\frac{1}{5} \times \frac{1}{6}$ 
 $\downarrow$ 
 $\downarrow$ 
 $\downarrow$ 
 $\downarrow$ 
**c.**  $4\frac{1}{2} \times 1\frac{1}{5}$ 
**d.**  $3\frac{1}{3} \times 2\frac{1}{10}$ 

2. **a.** A carpet is 5 ½ feet wide and 7 ½ feet long. How many square feet does it cover?

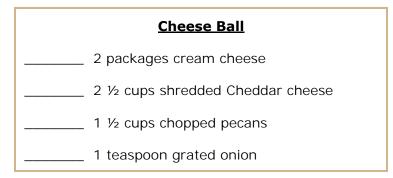
- **b.** A room is 12 ft by 20 ft. *About* what part of the floor area does the carpet cover? Use estimation (rounded numbers).
- 3. An student solved  $2\frac{1}{2} \times 1\frac{1}{2}$  wrongly like this:

"First, I multiply the whole numbers:  $2 \times 1 = 2$ . Then I multiply the fractional parts:  $\frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$ . Lastly, I add those to get 2 <sup>1</sup>/<sub>4</sub>."

Study the visual model and the calculations below. Then use the model to explain why the above method is wrong.



Alice is going to make this recipe
 1 ½ times. Calculate the new amount of each ingredient for her. Write the new amounts on the lines in front of the numbers in the recipe.

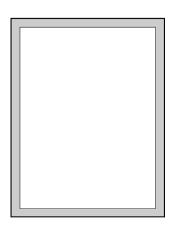


<b>a.</b> $2 \times 7\frac{1}{3}$	<b>b.</b> $2\frac{1}{9} \times \frac{1}{3}$
<b>c.</b> $7 \times 2\frac{4}{7}$	<b>d.</b> $\frac{7}{8} \times 2\frac{1}{5}$
<b>e.</b> $3\frac{3}{10} \times 2\frac{1}{3}$	<b>f.</b> $1\frac{1}{8} \times 2\frac{4}{5}$

5. Practice some more. Change any mixed numbers into fractions before multiplying.

- 6. In the US "letter" size paper measures 8  $\frac{1}{2}$  inches  $\times$  11 inches.
  - **a.** What is the area of this kind of paper in square inches?

**b.** If you use <sup>1</sup>/<sub>2</sub>-inch margins on all four sides, what is the real writing area in square inches?



### **Multiplication as Scaling/Resizing**

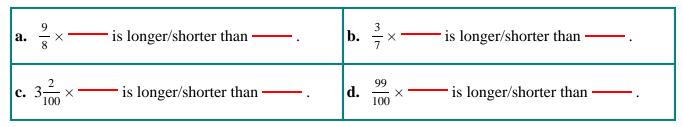
You know that <b>scaling</b> means <b>expanding or shrinking something</b> by some factor. We use <b>multiplication</b> to accomplish this. The number we multiply by is called the <b>scaling factor</b> .			
<b>Example 1.</b> When a stick 40 pixels long is scaled to be 3/5 as long as it was, it will shrink!			
$\longrightarrow$ $\longrightarrow$			
We could write this type of a multiplication equation: $(3/5) \times =$ .			
Using the length of 40 pixels, we write $(6/10) \times 40$ px = 24 px or $0.6 \times 40$ px = 24 px.			
<b>Example 2.</b> The multiplication $(1 \ 2/3) \times 18$ km means taking the distance of 18 km one and two-thirds times. We're scaling the quantity 18 km by the factor 1 2/3.			
To calculate it, we can multiply in parts: take $1 \times 18$ km, and $(2/3) \times 18$ km, and add those. Since two-thirds of 18 km is 12 km, then $(1 \ 2/3) \times 18$ km is $18$ km + $12$ km = $30$ km.			

1. The stick and other quantities are being scaled—either expanded or shrunk. Find the quantity after scaling. Compare the problems in each box.

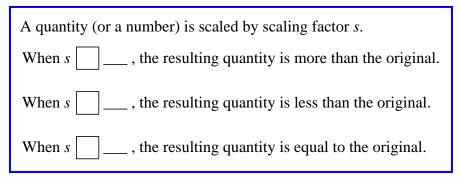
<b>a.</b>	<b>b.</b>	<b>c.</b>
$\frac{1}{2} \times =$	$\frac{1}{4} \times \frac{1}{4} = -$	5% × 400 km =
$\frac{1}{2} \times 50 \text{ px} = \text{ px}$	$\frac{1}{4} \times 40 \text{ px} = \_ \text{px}$	2 5% × 400 km =
$1 \frac{1}{2} \times \underline{\qquad} = \underline{\qquad}$ $1 \frac{1}{2} \times 50 \text{ px} = \underline{\qquad} \text{px}$	$2\frac{1}{4} \times \frac{1}{4} = \frac{1}{2\frac{1}{4} \times 40 \text{ px}} = \frac{1}{2} \text{ px}$	$     d.     \frac{3}{5} \times \$600 = \_\_\     3 \frac{3}{5} \times \$600 = \_\_\ $

- 2. A 1200 $\times$ 800 photo (in pixels) is scaled by scaling factor *s*.
  - **a.** If you want the resulting photo to be slightly smaller than the original, what kind of number would you use for *s*?
  - **b.** If s = 2 <sup>3</sup>/<sub>4</sub>, calculate the dimensions of the resulting photo.

3. Will the resulting stick be longer or shorter than the original—or equally long? You do not have to calculate anything. Compare.



- 4. Let *s* be the scaling factor. For what kind of values of *s* will  $s \times $500$  be more than \$500? For what kind of values will it be less?
- 5. Write  $\langle , \rangle$ , or = in the boxes. Fill in a number on the empty lines.



- 6. Scaling is also the concept we use when calculating prices. Find the total cost. Use either fractions or decimals, depending on what makes most sense.
  - **a.** Nuts cost \$8.50 per pound. You buy  $1\frac{1}{2}$  pounds.

**b.** Rent is \$350 per month (30 days). You stay for 12 days.

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### **Chapter 9: Geometry** Introduction

The focus of this chapter is on two topics: classifying two-dimensional shapes, and volume.

The chapter starts out with a lesson that reviews the topic of angles from fourth grade. The next lesson (Polygons) covers the concept of a polygon and the names of several common ones. Students classify figures into polygons and non-polygons, and also into regular polygons versus non-regular polygons.

The next topic is classifying quadrilaterals. The focus is on understanding the classification, and understanding that attributes defining a certain quadrilateral also belong to all the "children" (subcategories) of that type of quadrilateral. For example, squares are also rhombi, because they have four congruent sides (the defining attribute of a rhombus).

A possible confusion point is the definition of a trapezoid. There exist two possible definitions:

- (Exclusive definition:) A trapezoid has exactly one pair of parallel sides.
- (Inclusive definition:) A trapezoid has at least one pair of parallel sides.

Both definitions are legitimate, but lead to different analysis when classifying quadrilaterals. Under the exclusive definition, a parallelogram is not a trapezoid, but under the inclusive definition, it is. Most college-bound textbooks favor the *inclusive* definition, and that is what is used in this text, also.

Then we study the classification of triangles. Students are now able to classify triangles both in terms of their sides and also in terms of their angles.

The second focus topic of this chapter is volume. Students learn that a cube with the side length of 1 unit, called a "unit cube," is said to have "one cubic unit" of volume, and can be used to measure volume. They find the volume of right rectangular prisms by "packing" them with unit cubes and by using formulas. They recognize volume as additive and solve both geometric and real-word problems involving volume.

The chapter includes three optional lessons listed in the end: area and perimeter problems, star polygons, and circles. Use them as time allows. The lesson on area and perimeter can be important for those students who tend to forget these concepts. The lesson on star polygons is intended as a fun artistic topic. The lesson on circles involves the usage of a compass, which may be hard for some children at this age. Those who can master it will probably find the exercises involving multiple circles fascinating.

Note: Any problem marked with " " means the exercise should be done in a notebook or on blank paper.

#### Pacing Suggestion for Chapter 9

This table does not include the chapter test as it is found in a different book (or file). Please add one day to the pacing for the test if you will use it.

The Lessons in Chapter 9	page	span	suggested pacing	your pacing
Geometry Vocabulary Reference Sheet	175			
Review: Angles	176	3-4 pages	1 day	
Polygons	180	3 pages	1 day	
Classifying Quadrilaterals 1	183	3 pages	1 day	
Classifying Quadrilaterals 2	186	3 pages	1 day	
Classifying Quadrilaterals 3 (optional) Sample worksheet from	189	(2 pages)	(1 day)	
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The Lessons in Chapter 9	page	span	suggested pacing	your pacing
Classifying Triangles 1	191	3 pages	1 day	
Classifying Triangles 2	194	3 pages	1 day	
Volume	196	5 pages	2 days	
Volume of Rectangular Prisms	201	3 pages	1 day	
Volume is Additive	204	3 pages	1 day	
* Area and Perimeter Problems (optional)	207	(5 pages)	(2 days)	
* Star Polygons (optional)	212	(2 pages)	(1 day)	
Mixed Review Chapter 9	214	3 pages	1 day	
Chapter 9 Review	217	3 pages	1 day	
Chapter 9 Test (optional)				
TOTALS		35 pages	12 days	
with optional content		(45 pages)	(16 days)	

\* These lessons exceed the Common Core Standards (CCS) for 5th grade.

#### Helpful Resources on the Internet

We have compiled a list of Internet resources that match the topics in this chapter, including pages that offer:

- online practice for concepts;
- online games, or occasionally, printable games;
- animations and interactive illustrations of math concepts;
- articles that teach a math concept.

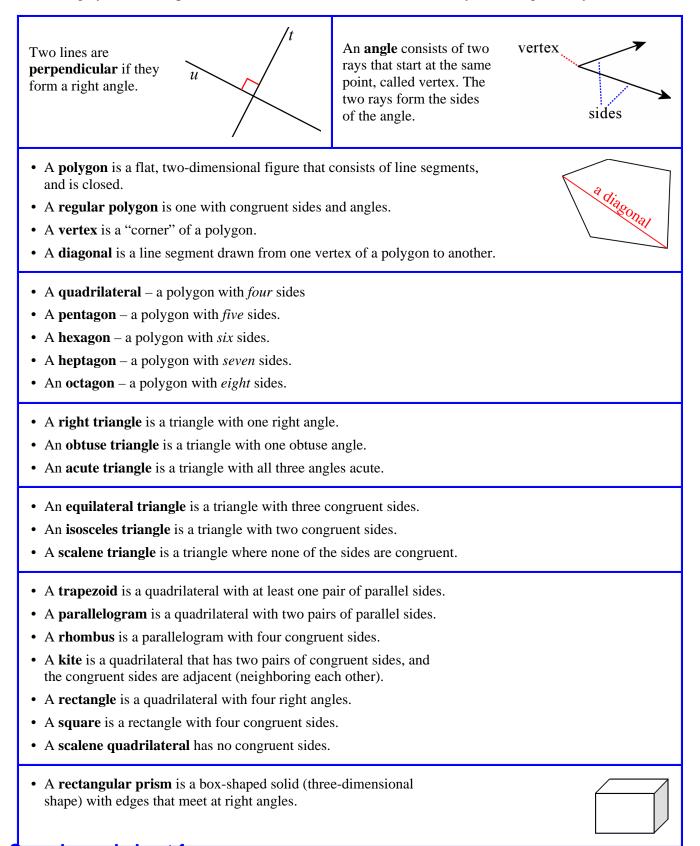
We heartily recommend you take a look! Many of our customers love using these resources to supplement the bookwork. You can use these resources as you see fit for extra practice, to illustrate a concept better and even just for some fun. Enjoy!



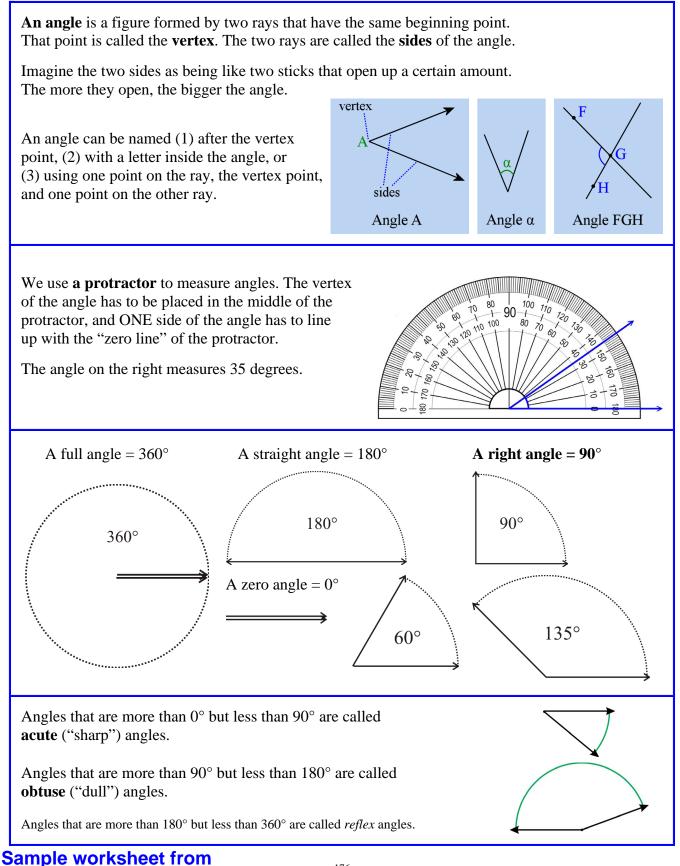


### **Geometry Vocabulary Reference Sheet**

I encourage you to draw pictures to illustrate the terms, or even make your own geometry notebook!



### **Review:** Angles



1. Measure these angles with a protractor. If necessary, continue the sides of the angle with a ruler.

2. a. Draw any acute angle, and measure it.

**b.** Draw any obtuse angle, and measure it.

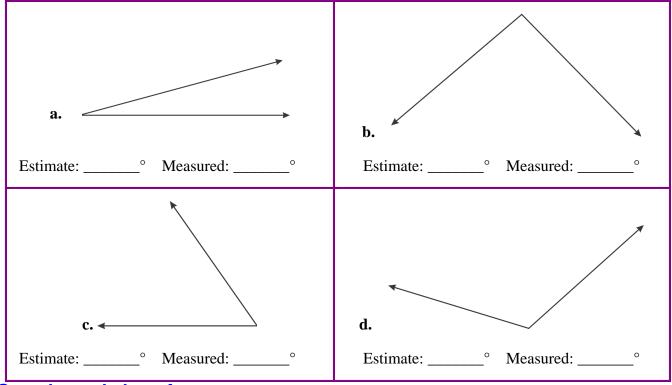
3. Draw three dots on a blank paper and join them to form a triangle. Draw the dots far enough apart so that the triangle nearly fills the page. Then, measure the angles of your triangle.

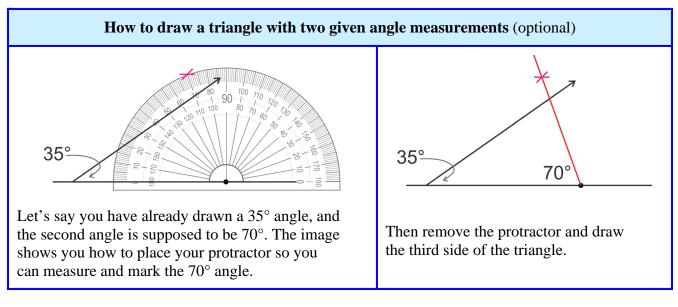
The angles of my triangle are: \_\_\_\_\_°, \_\_\_\_\_°, and \_\_\_\_\_°.

Classify each angle as acute, right, or obtuse.

4. You see a line and a point on it. The point will be the vertex of an angle. Draw the other side of the angle from the vertex so that the angle measures 76°. Use a protractor.

- 5. Follow the procedure above to draw acute angles with the following measures:
  a. 30° b. 60° c. 45°
- 6. Draw obtuse angles with these measures: **a.**  $135^{\circ}$  **b.**  $100^{\circ}$  **c.**  $150^{\circ}$
- 7. Estimate the measure of these angles. Measure to check (you may need to continue the sides).





#### 8. (optional)

**a.** Draw a triangle with 50° and 75° angles. It can be of any size — smaller or bigger. *Hint*: Start out by drawing a (long) horizontal line, and two dots on it which mark the two vertices of the triangle.

**b.** Measure the third angle. It measures \_\_\_\_\_°.

c. Label each angle in the triangle as acute, obtuse, or right.

9. (optional)

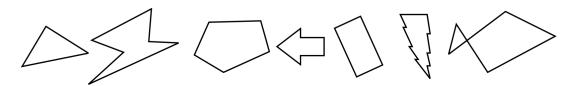
**a.** Draw a triangle with  $110^{\circ}$  and  $35^{\circ}$  angles.

**b.** Measure the third angle. It measures \_\_\_\_\_°.

c. Label each angle in the triangle as acute, obtuse, or right.

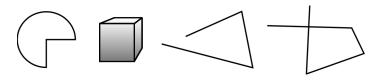
### Polygons

A polygon is a flat, two-dimensional figure that consists of line segments, and is *closed*.



The boundary of a polygon is allowed to cross itself, like in the polygon above at the right. However, in this chapter we will mostly deal with *simple* polygons where such does not happen.

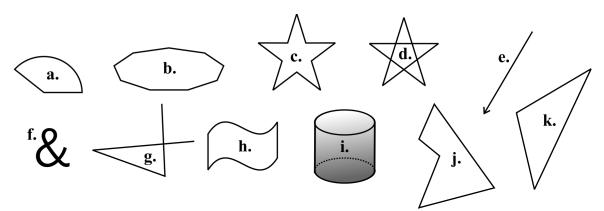
These figures are not polygons. Notice how each figure either is not closed, does not consist of line segments, or is not a flat, two-dimensional figure:



Polygons are named after the number of vertices they have. Most of the names for polygons in English have their roots in Greek, using a number and the Greek word "*gonia*" which means "angle".

Vertices	Name	Greek/Latin
3	triangle	tri = three
4	quadrilateral	quadri (Latin) = four
5	pentagon	pente = five
6	hexagon	hex = six
7	heptagon	hepta = seven
8	octagon	okto = eight

1. Classify each figure as a polygon, or not a polygon.



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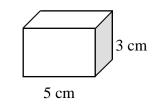
### **Volume of Rectangular Prisms**

Study the two formulas for the volume of a rectangular prism:	1.	$\mathbf{V} = \boldsymbol{w} \times \boldsymbol{d} \times \boldsymbol{h}$	(volume is width $\times$ depth $\times$ height) Some people use width, <u>length</u> , and height instead.		
roomigum promi	2.	$\mathbf{V} = \mathbf{A}_{\mathbf{b}} \times \boldsymbol{h}$	(volume is area of the bottom $\times$ height)		
The width, depth, and height need to be in the <u>same</u> kind of unit of length (such as meters). The volume will then be in corresponding cubic units (such as cubic meters).					
<b>Example 1.</b> A room me What is the area of the r		12 ft by 8 ft, and i	it is 8 ft high. What is the volume of the room?		
To find the area, we simply multiply the two given dimensions: $A = 12 \text{ ft} \times 8 \text{ ft} = 96 \text{ ft}^2$ . To find the volume, we can multiply the area by the height: $V = 96 \text{ ft}^2 \times 8 \text{ ft} = 768 \text{ ft}^3$ .					
<b>a.</b> Find the volume of a box that is 2 inches high, 5 inches wide, and 7 inches deep. Include the					
units! $V = 5 in$	×_	×	=		
<b>b.</b> Find the area and volum	ne of a	room that is 25 ft	$\times$ 20 ft, and 9 feet high. Include the units!		
A =×		=			
V = ×		×	=		
Find the volume of the bo in the same measurement unit l		U U	nsions. (Remember that all the dimensions need to be .)		

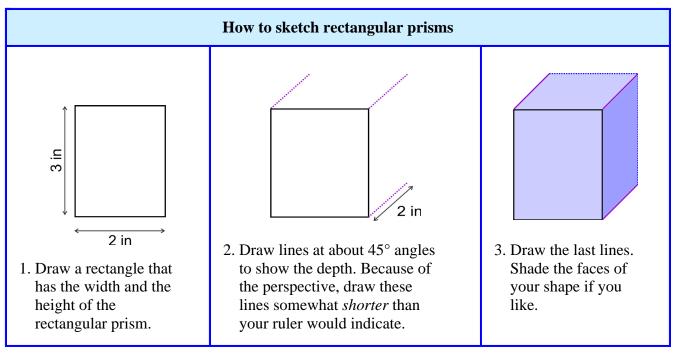
- a. 20 cm wide, 30 cm deep, and 0.6 meters high
- **b.** 16 square inches on the bottom, and half a foot tall
- 3. The volume of this box is 30 cm<sup>3</sup>. What is its depth?

1.

2.



4. *Optional*. Measure the width, height, and depth of a dresser and/or a fridge. Find out its volume (in cubic feet or cubic meters).



5. Sketch a box that is 6 cm wide, 5 cm tall, and 4 cm deep. What is its volume?

6. Sketch a box that is 50 cm wide, 80 cm tall, and 90 cm deep. What is its volume?

7. The length and width of a rectangular box are 5 inches and 6 inches. Its volume is 180 cubic inches. How tall is it?



Sample worksheet from https://www.mathmammoth.com

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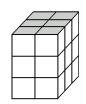
©2023 Taina Miller

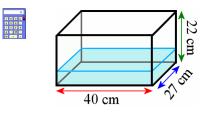
8. The picture shows an aquarium that is 1/4 filled with water. Find the volume of the water in it.

- 9. a. Design a box (give its width, height, and depth) with a volume of 64 cubic inches.
  - **b.** Design a water tank, in the form of a rectangular prism, that can hold 960,000 cm<sup>3</sup> of water (which equals 960 liters).
- 10. Amber built this prism with little cubes. Then she built another, with a volume that was four times the volume of the little prism.
  - **a.** What is the volume of the larger prism?
  - **b.** What could its dimensions be?
- 11. John's room is 12 ft  $\times$  18 ft, and it is 9 ft high. The family plans to *lower* the ceiling by 1 foot.
  - **a.** What will the volume of the room be after that?
  - **b.** How much volume will the room lose?

A truck delivered two cubic yards of gravel to Tom. Calculate how many **cubic feet** of gravel Tom got.

Hint: Design a box with a volume of two cubic yards.





Chapter 9: Volume of Rectangular Prisms

### **Volume Is Additive**

Volume is **additive**. What we mean by that is that we can ADD to find the total volume of a shape that is in several parts.

To find the total volume of the shape on the right, first find the volume of the top box, then the volume of the bottom box, and add the two volumes.

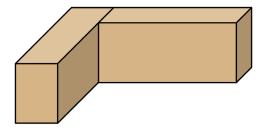
1. Find the total volume of the shape in the teaching box above. Show your work, and organize your work carefully, to avoid mistakes.

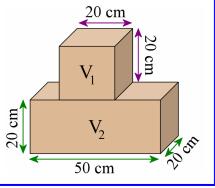
 $V_1 =$ 

 $V_2 =$ 

 $V_{total} = V_1 + V_2 =$ 

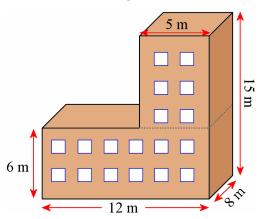
- 2. This is a two-part kitchen cabinet. Its height is 2 ft and depth 1 ft. One part is 5 ft long, and the other is 4 ft long.
  - **a.** Mark the given dimensions in the picture.
  - **b.** Calculate the volume.



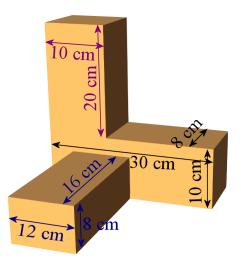


Chapter 9: Volume is Additive

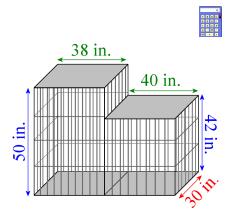
3. Find the volume of this building.



4. Find the total volume.



5. **a.** Find the volume of this two-part bird cage.



**b.** One cubic foot is 1,728 cubic inches. Convert your answer from (a) into cubic feet, to three decimals.



The volume of the larger cube is 1,000 cubic inches. The edge length of the smaller cube is half of the edge length of the larger cube.

What is the combined volume of the two cubes?