Integers Reminder Sheet 2

A positive integer times a negative integer:	A negative times a negative.
Think of repeated addition here: $3 \times (-2) =$ (-2) and (-2)	$(-3) \times 3 =$ $(-3) \times 2 =$ $(-3) \times 1 =$ $(-3) \times 0 =$ $(-3) \times (-1) =$ Complete the pattern on the left. Observe how the products continually increase by 3 in each step.
Or, 4 × (−7) = (−7) + (−7) + (−7) + (−7) = −28. A positive integer times a negative integer:	
Since you can change the order of the factors,	Another 'justification' for this rule can be seen using distributive property:
$(-6) \times 4 = 4 \times (-6) = -24.$	
In general, if <i>m</i> and <i>n</i> are natural numbers, then $m \times (-n)$ is $(-n)$ added repeatedly <i>m</i> times, so is	Distributive property of arithmetic states that $a(b + c) = ab + ac$.
negative. And $(\neg m) \times n$ is the same as $n \times (\neg m)$ and so is negative as well.	So, if a = (-1) , b = 3, and c = (-3) , it should still hold:
both have a negative answer	(-1)(3 + (-3)) = (-1)(3) + (-1)(-3)
	Now, since $3 + (-3)$ is zero, the whole left side is zero. So $(-1)(3) + (-1)(-3)$ must be zero as well.
Dividing a negative integer by a positive.	(-1)(3) is -3. So it follows that $(-1)(-3)$ has to be
Divide these negatives into	the opposite of -3 , or 3.
three groups. $(-6) \div 3 = -2.$	The 'negative times negative makes a positive' rule has to do with the fact that IF we made it to be negative, then all these neat rules and properties of
Dividing a positive integer by a negative.	arithmetic wouldn't hold for negative numbers.
What is $(-15) \div 5$? Let's call the answer Z. Since division and multiplication are opposite operations, $Z \times 5 = -15$. So Z must be -3 .	But mathematicians do want them to hold, since we DO want mathematics to be a very consistent system. So the convention is made that negative times negative is positive.
In general, if <i>m</i> and <i>n</i> are natural numbers, and $(-m) \div n$ is B, then B × n = $(-m)$, and B must be negative.	In a nutshell, whether you are multiplying <i>or</i> dividing:
Dividing a negative integer by a negative.	
Let's say (−21) ÷ (−7) is some number A.	 ÷ (different signs) × yields a negative answer.
It follows that A × $(-7) = (-21)$	÷ 🕂 š
Knowing the multiplication rules, the only number that fits A is 3.	Φ×Φ
In general, if <i>m</i> and <i>n</i> are natural numbers, and $(-m) \div (-n)$ is B, then B × $(-n) = (-m)$, and B must be positive.	 ÷ (same kind of signs) × ÷ yields a positive answer.

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